# **HINTS & SOLUTIONS**

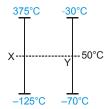
## EXERCISE - 1

### **Single Choice**

1. For centigrade and Fahrenheit scale

$$\frac{F-32}{212-32} = \frac{C-0}{100-0} \implies C = \frac{100}{180} \times (140-32) = 60^{\circ}\text{C}$$

2. Let  $\theta$  = temperature on X-scale corresponding to 50°C on Y-scale



$$\Rightarrow \frac{X - (-125)}{375 - (-125)} = \frac{50 - (-70)}{-30 - (-70)} \Rightarrow X = 1375$$

3. Slope of line AB

$$=\frac{\Delta C}{\Delta F}=\frac{100-0}{212-32}-\frac{100}{180}=\frac{5}{9}$$

4.  $\frac{X - LFP}{UFP - LFP}$  = constant (for all temperature scales)

 $LFP \rightarrow lower fixed point UFP \rightarrow Upper fixed point$ 

$$\frac{X - (-5)}{95 - (-5)} = \frac{C - 0}{100 - 0} \Rightarrow \frac{60 + 5}{95 + 5} = \frac{C}{100} \Rightarrow C = 65^{\circ}C$$

5. If we take two fixed points as tripe point of water and 0 K.
Then

$$\frac{T_x - 0}{200} = \frac{T_y - 0}{450} \Rightarrow 450 T_x = 200 T_y \Rightarrow 9T_x = 4T_y$$

6. Let at temperature  $\theta$ , volume increases by 2% then according to question

$$100 = 98 [1+3.3 \times 10 (\theta - 4)] \Rightarrow \theta = 60.4 + 4 = 64.4 \text{ }^{\circ}\text{C}$$

7. Expansions of a metal is same as photographic enlargement.  $\Rightarrow$  d<sub>1</sub> will increase by 0.3%

8. 
$$\Delta L = 6 \times 10^{-5} = L\alpha\theta \Rightarrow \theta = \frac{6 \times 10^{-5}}{1 \times 12 \times 10^{-6}} = 5^{\circ}C$$

9.  $\Delta L = \Delta L_{\text{thermal}} - \Delta L_{\text{contact force}} = 0 \Rightarrow \alpha_1 L \theta = \frac{FL}{AY_1} \text{ (rod - 1)}$ 



$$\alpha_2 L\theta = \frac{FL}{AY_2} (rod - 2) \Rightarrow Y_1 \alpha_1 = Y_2 \alpha_2$$

Coefficient of linear expansion of brass is greater than that of steel.

11. Pressure at the bottom in both arms will be equal

$$\left(\frac{\rho_0}{1+\gamma t_1}\right).\ell_1 = \left(\frac{\rho_0}{1+\gamma t_2}\right)\ell_2 \implies \gamma = \frac{\ell_1-\ell_2}{\ell_2 t_1-\ell_1 t_2}$$

12. Strain

$$t = \frac{\Delta \ell}{\ell} = -\alpha \Delta \theta = -12 \times 10^{-6} \times (75 - 25) = -6 \times 10^{-4}$$

13. Clearance = R'-R but  $2\pi R' = 2\pi R (1 + \alpha_s \Delta T)$   $\Rightarrow R' - R = R\alpha_s \Delta T$ = (6400) (1.2 × 10<sup>-5</sup>) (30) = 2.3 km

**14.**  $\ell = \ell_0 (1 + \alpha \Delta T) \implies \ell - \ell_0 = \ell_0 \alpha \Delta T$ 

$$\Rightarrow \frac{\ell_0 \alpha_A \Delta T}{\ell_0 \alpha_B \Delta T} = \frac{104 - 100}{106 - 100} = \frac{4}{6} \Rightarrow \frac{\alpha_A}{\alpha_B} = \frac{2}{3}$$

**15.** For rod A  $\Delta \ell = \ell_0 \alpha_A(100)$ 

For rod B 
$$\frac{\Delta \ell}{2} = 2\ell_0 \alpha_B (100)$$

For rod C  $2\Delta \ell = x\alpha_{\Delta}(100) + (3\ell_0 - x)\alpha_{B}(100)$ 

$$\Rightarrow$$
 x =  $\frac{5}{3} \ell_0 \& 3\ell_0 - x = \frac{4}{3} \ell_0$ 

16.  $\mathbf{x} = \ell_{A}' - \ell_{B}' = \ell_{A} (1 + \alpha_{A} \Delta T) - \ell_{B} (1 + \alpha_{B} \Delta T) = \ell_{A} - \ell_{B}$   $\Rightarrow \ell_{A} \alpha_{A} = \ell_{B} \alpha_{B}$ 

17. 
$$\Delta \ell = \int \text{ Expansion in } dx = \int \left[ \left( \alpha_0 + \alpha_1 x \right) dx \right] \Delta T$$

$$= 100 \int_0^2 (1.76 \times 10^{-5} + 1.2 \times 10^{-6} x) dx$$

$$= 100 \left[ \left( 1.76 \times 10^{-5} \right) x + \left( 1.2 \times 10^{-6} \right) \left( \frac{x^2}{2} \right) \right]_0^2$$

$$= 3.76 \text{ mm}$$

18. For simple pendulum  $T = 2\pi$ 

$$\sqrt{\frac{\ell}{g}} \implies T \propto \ell^{1/2} \implies \frac{\Delta T}{T} = \frac{1}{2} \frac{\Delta \ell}{\ell} = \frac{1}{2} \alpha \Delta \theta$$

Assuming clock gives correct time at temperature

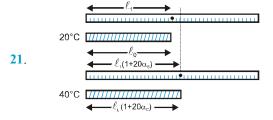
$$\theta_0 \Rightarrow \frac{6}{24 \times 3600} = \frac{1}{2} \alpha (\theta_0 - 20) \& \frac{6}{24 \times 3600}$$

$$= \frac{1}{2} \alpha \left(40 - \theta_0\right) \implies \theta_0 = 30 \text{°C} \implies \alpha = 1.4 \times 10^{-5} \text{ °C}^{-1}$$

19. 
$$\therefore d\ell = \alpha \ell_0 dT$$
  $\therefore \Delta \ell = \int d\ell = \int_{T_0}^{T_2} (aT - bT^2) \ell_0 dT$ 

$$=\,\ell_{\,0} \Bigg[ \frac{a}{2} \Big( T_{2}^{2} - T_{1}^{2} \Big) - \frac{b}{3} \Big( T_{2}^{3} - T_{1}^{3} \Big) \Bigg] = \Bigg[ \frac{3}{2} \, a T_{1}^{2} - \frac{7b}{3} \, T_{1}^{3} \, \Bigg] \ell_{\,0}$$

**20.** 
$$\gamma_r = \gamma_1 + 3\alpha_1 = \gamma_2 + 3\alpha_2 \Rightarrow \alpha_2 = \frac{\gamma_1 - \gamma_2 + 3\alpha_1}{3}$$



$$\ell_0 (1 + 20 \,\alpha_C) = \ell_1 (1 + 20\alpha_S) \Longrightarrow \ell_1 = \left(\frac{1 + 20\alpha_C}{1 + 20\alpha_S}\right) \ell_0$$

22. Newton's law of cooling

$$\frac{\Delta \theta}{\Delta t} = k[\theta - \theta_0]$$

 $\theta_0$  = surrounding's temperature

$$\Rightarrow \frac{80-60}{t} = k \left[ \frac{80+60}{2} - 30 \right]$$
 ...(i)

and 
$$\frac{60-50}{t} = k \left[ \frac{60+50}{2} - 30 \right]$$
 ...(ii

$$\Rightarrow$$
 t = 48 sec

23. Let  $\theta$  = junction temperature Net heat current at junction is zero

$$3k(100 - \theta) + k(0 - \theta) + 2k(50 - \theta) = 0 \implies \theta = \frac{200}{3}$$
 °C

24. From Stefan's law :  $\Delta \hat{Q} = \sigma A T^4$ 

$$\Rightarrow \frac{1cal}{s - m^2} \times \frac{4.2J}{cal} = 5.67 \times 10^{-8} \times 1 \times T^4 \Rightarrow T = 100 \text{ K}$$

25. : 
$$t \propto (x_2^2 - x_1^2)$$
  
For  $x_1 = 0, x_2 = 1 \text{ cm}$   
 $7 \propto (1^2 - 0^2)$   
For  $x_1 = 1 \text{ cm}, x_2 = 2 \text{ cm}$   
 $t \propto (2^2 - 1^2) \Rightarrow \frac{7}{t} = \frac{1}{3} \Rightarrow t = 21 \text{ hrs}$ 

26. 
$$\frac{Power}{Area}$$
 = Intensity

Power absorbed by the foil = Intensity at foil  $\times$  Area of foil

$$\Rightarrow P = \frac{P_0}{4\pi d^2} \times A = \left(\frac{\sigma A_0 T^4}{4\pi d^2}\right) A$$

Now 
$$P = \frac{\sigma A_0 (2T)^4 \times A}{4\pi (2d)^2} = 4P$$

27. 
$$dR_H = \frac{dx}{KA} = \frac{dx}{KA_0(1 + \alpha x)}$$



$$\begin{split} R_{H} &= \int dR_{H} = \int_{0}^{\ell} \frac{dx}{KA_{0}(1 + \alpha x)} = \frac{1}{KA_{0}} \left( \frac{\ell n(1 + \alpha x)}{\alpha} \right)_{0}^{\ell} \\ &= \frac{1}{KA_{0}} \ell n(1 + \alpha \ell_{0}) \quad \text{or} \quad \text{Check dimensionally} \end{split}$$

28 
$$\therefore \left(\frac{\Delta Q}{\Delta t}\right)_{A} = \left(\frac{\Delta Q}{\Delta t}\right)_{B}$$

$$\therefore \frac{K_{A}A(100 - 70)}{30} = \frac{K_{B}A(70 - 35)}{70}$$

$$\Rightarrow K_{A} = \frac{K_{B}}{2} \Rightarrow \frac{K_{A}}{K_{B}} = \frac{1}{2}$$

29. 
$$\frac{Q}{t} = \sigma A T^4 = \text{same but } T_{red} < T_{green}$$

$$as \lambda_{red} T_{red} = \lambda_{green} T_{green} (\text{see VIBGYOR})$$

$$\Rightarrow \text{Area of red star is greater}$$

**30.** According to Wien's law

$$\lambda_{\rm m} \propto 1/T \Longrightarrow \nu_{\rm m} \propto T$$
.

As the temperature of body increases, frequency corresponding to maximum energy in radiation ( $\nu_m$ ) increases. Also area under the curve

$$\int \; E_{\nu} d\nu \propto T^4$$

31. Entire KE gets converted into heat.  $\Delta KE = \text{ms } \Delta\theta \implies 10 \times 10 \times 10 = 2 \times 4200 \times \Delta\theta$   $\implies \Delta\theta = 0.12^{\circ}\text{C}$ 

32. Rate of cooling of water = Rate of cooling of alcohol

$$\Rightarrow \frac{(250+10)\times1\times(5)}{130} = \frac{(200s+10)\times5}{67}$$

 $\Rightarrow$  Specific heat of alcohol s = 0.62

33. Amount of energy utilised in climbing  $mgh = 0.28 \times 10 \times 4.2$ 

⇒ 
$$h = \frac{0.28 \times 10 \times 4.2}{60 \times 10} = 1.96 \times 10^{-2} \text{ m} = 1.96 \text{ cm}$$

34.  $H_C = ms\Delta\theta = ms(1)^{\circ}C$   $H_K = ms\Delta\theta = ms(1)K = ms(1)^{\circ}C$  $H_F = ms\Delta\theta = ms(1)^{\circ}F = ms(5/9)^{\circ}C$ 

$$H_C = H_K > H_F$$

35. M= mass of hallstone falling m = mass of hallstone melting As Mgh = mL.

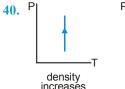
So 
$$\frac{m}{M} = \frac{gh}{L} = \frac{10 \times 10^3}{33 \times 10^3} = \frac{1}{33}$$

- **36.** Water has high specific heat and due to this it absorber more heat in rise of temperature.
- 37. Heat lost = Heat gained  $m_{\text{steam}} \times 540 = 1100 \times 1 \times (80 15) + 20 \times 1 \times (80 15)$   $\therefore \text{ mass of steam condensed} = 0.13 \text{ kg}$
- 38. If intermolecular forces vanish water behaves as gas.

Number of moles of water = 
$$\frac{4.5 \times 10^3}{18} = 250$$

Total volume of water at STP =  $22.4 \times 250 \times 10^{-3} \text{ m}^3 = 5.6 \text{ m}^3$ 

**39.** When water is cooled to form ice, the energy is released as heat so mass of water decreases.







For equation :  $\left( : P = \frac{\rho RT}{M_w} \right)$ 

At constant temperature  $\rho \propto p$ 

For  $1^{st}$  graph :  $\rho \propto P$  At constant temperature.

For 
$$2^{nd}$$
 graph:  $\left(\because P = \frac{\rho RT}{M_{uv}}\right)$ 

At constant P,  $\rho \propto \frac{1}{T}$ 

For 
$$3^{rd}$$
 graph L:  $\frac{dP}{dT}$  = constant  $\Rightarrow P \propto T$ 

 $\Rightarrow$  density  $\rho = constant$ 

41. Heat removed in cooling water from  $25^{0}$ C to  $0^{0}$ C =  $100 \times 1 \times 25 = 2500$  cal

Heat removed in converting water into ice at  $0^{0}$ C =  $100 \times 80 = 8000$  cal

Heat removed in cooling ice from

 $0^0$  to  $-15^0$ C =  $100 \times 0.5 \times 10 = 500$  cal

Total heat removed in 1hr 50min

=2500+8000+500=11000 cal

Heat removed per minute =  $\frac{11000}{110}$  = 100 cal/min

- 42. Volume can't be negative. At constant pressure  $V \propto T$  or  $V \alpha (t+273)$
- 43. If temperature is doubled, pressure will also be doubled as  $P = \frac{\rho RT}{M_w} \Rightarrow 100\%$  increase
- 44. Ideal gas equation: PV = nRTSo at  $V = V_0$ ;  $RT_1 = \left(\frac{P_0}{2}\right)$   $(V_0)$  and at  $V = 2V_0$ ,

$$RT_2 = \left(\frac{4P_0}{5}\right)(2V_0) \implies T_2 - T_1 = \frac{11P_0V_0}{10R}$$

45.  $\frac{3}{4}$  th volume of air at 0°C occupies entire volume at  $\theta$ ,

As 
$$\frac{V_1}{T_1} = \frac{V_2}{T_2} \Rightarrow \frac{3/4V}{273+60} = \frac{V}{273+\theta} \Rightarrow \theta = 171^{\circ}C$$

- **46.** Total translational KE =  $\frac{3}{2}$  nRT =  $\frac{3}{2}$  PV
- 47. Number of moles remain constant

$$n_1 + n_2 = n_1' + n_2' \implies \frac{P_1 V_1}{R T_1} + \frac{P_2 V_2}{R T_2} = \frac{P_1' V_1'}{R T_1'} + \frac{P_2' V_2'}{R T_2'}$$

$$\Rightarrow \frac{PV}{273} + \frac{PV}{273} = \frac{(1.5P)V}{R \times 273} + \frac{(1.5P)V}{R \times T}$$
$$\Rightarrow T = 273 \times 3 \text{ K} = (273 \times 3 - 273) \text{ °C} = 546 \text{ °C}$$

48. 
$$v_{rms} = \sqrt{\frac{3KT}{m}} \implies T = \frac{mv_{rms}^2}{3K} :: T \propto mv_{rms}^2$$

**49.** 
$$\gamma = \frac{n_1 C_{P_1} + n_2 C_{P_2}}{n_1 C v_1 + n_2 C v_2}$$

$$\gamma = 1.5 \therefore C_{p_1} = \frac{5R}{2}; C_{p_2} = \frac{7R}{2}$$

$$C_{V1} = \frac{3R}{2}$$
;  $C_{V2} = \frac{5R}{2}$ ; then  $n_1 = n_2$ 

**50.** Here V = aT + b where a, b > 0

So 
$$P = \frac{nRT}{aT + b} = \frac{nR}{a + b / T}$$
 but  $\frac{b}{T_2} < \frac{b}{T_1}$  so  $P_2 > P_1$ 

51. Change in momentum =  $2 \text{mv} \cos(45^\circ)$ 

= 
$$2 \times 3.32 \times 10^{-27} \times 10^{3} \times \frac{1}{\sqrt{2}}$$
  
=  $4.7 \times 10^{-24} \text{ kg ms}^{-1}$ .



52.  $\Delta U_1 = +ve_{,} \Delta U_2 = 0 \Rightarrow \Delta U_3 = -ve_{,}$ 

$$\Delta U_1 > \Delta U_2 > \Delta U_3$$

As volume increases,  $\Delta W = +ve$ .

53. 
$$PV = nRT \Rightarrow P = \frac{\rho}{M_w} RT$$

$$\Rightarrow \rho = \frac{PM_w}{RT} = \frac{(10^5)(28 \times 10^{-3})}{8.3 \times 273} \text{ kg m}^{-3} = 1.25 \text{ g/litre}$$

54.  $PT^{11} = constant & PV = nRT$ 

$$\Rightarrow$$
 V \preceq T<sup>12</sup>  $\Rightarrow \frac{\Delta V}{V} = 12 \frac{\Delta T}{T} \Rightarrow \gamma_v = \frac{\Delta V}{V \Delta T} = \frac{12}{T}$ 

- 55. Internal energy and volume depend upon states.
- **56.** When water is heated from 0°C to 4°C, its volume decreases.
- ..  $P \Delta V$  is negative Hence  $C_n - C_v < 0 \Rightarrow C_n < C_v$

57. 
$$\Delta U = 2P_0 \Delta V \& W = P_0 \Delta V$$
  
So  $Q = W + \Delta U = 3P_0 \Delta V = 3P_0 V_0$ 

**58.** 
$$f_{eq} = \frac{f_1 n_1 + f_2 n_2 + f_3 n_3}{n_1 + n_2 + n_3} = \frac{(5n)(3) + (n)(5) + (5n)(6)}{5n + n + 5n} = \frac{50}{11}$$

59.  $V \propto T^4 \Rightarrow V \propto (PV)^4$ 

$$\Rightarrow$$
 P<sup>4</sup>V<sup>3</sup> = constant  $\Rightarrow$  PV<sup>3/4</sup> = constant

$$\therefore C = C_v + \frac{R}{1 - x} = 3R + \frac{R}{1 - 3/4} = 3R + 4R = 7R$$

60. U = a + bPV = a + bnRT $\Rightarrow \Delta U = bnR\Delta T = nC_v\Delta T$   $\Rightarrow C_v = bR \Rightarrow C_p = bR + R$ 

$$\Rightarrow \gamma = \frac{C_p}{C_v} = \frac{bR + R}{bR} = \frac{b + 1}{b}$$

#### **EXERCISE - 2**

### Part # I: Multiple Choice

1.  $DC^2 = L_2^2 - \frac{L_1^2}{4} \implies 0 = 2L_2 \Delta L_2 - \frac{2L_1 \Delta L_1}{4}$ 

$$\Rightarrow 0 = 2L_2(\alpha_2L_2\theta) - \frac{2L_1(\alpha_1L_1\theta)}{4} \Rightarrow \alpha_1 = 4\alpha_2$$

- 2. All dimensions increase on heating.
- A part of liquid will evaporate immediately sucking latent heat from the bulk of liquid. Hence a part of liquid will freeze.
- 5.  $\Delta Q_{vap} = \Delta Q_{freezing}$  $m.(\eta L) = M(L) \Rightarrow M = \eta m$

L = latent heat of freezing

m = mass of vapour

M = mass of freezed

: Fraction of water which freezed

$$=\frac{M}{m+M}=\frac{\eta M}{m+\eta m}=\frac{\eta}{1+\eta}$$

6.  $Q_1 = \Delta U + W_1$ ;  $Q_2 = \Delta U + W_2$ Ratio of specific heats

$$\frac{C_1}{C_2} = \frac{\left(\frac{\Delta Q_1}{\Delta T}\right)}{\left(\frac{\Delta Q_2}{\Delta T}\right)} = \frac{\left(\frac{\Delta U}{\Delta T} + \frac{\Delta W_1}{\Delta T}\right)}{\left(\frac{\Delta U}{\Delta T} + \frac{\Delta W_2}{\Delta T}\right)} < 1 \quad (\because W_2 > W_1)$$

- 7. Water at 4°C has highest density
- **8.** Mixture may attain intermediate temperature or terminal temperatures of fusion or vapourisation.
- 9.  $O = \Delta U + W$

Q = +ve, as heat is absorbed from the atmosphere

W=-ve as the volume decrease

$$\Delta U = Q - W = +ve - (-ve) = +ve$$

- : Internal energy increases.
- 10. For insulated chambers  $n_1 + n_2 = n'_1 + n'_2$  (final pressures become equal)

$$\frac{PV}{RT} + \frac{2P.2V}{RT} = \frac{P}{RT}[3V] \implies P' = \frac{5P}{3}$$

For left chamber

$$PV = P'V' = \frac{5P}{3}V' \implies V' = \frac{3V}{5}$$

For right chamber

$$4PV = P'V' = \frac{5P}{3}V' \implies V' = \frac{12V}{5}$$

11. 
$$H_A = (6 \text{ cal/s}) \times (6-2) \text{ s}$$
  
 $H_B = (6 \text{ cal/s}) \times (6.5-4) \text{ s}$ 

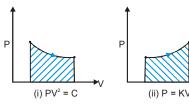
$$\therefore \frac{H_A}{H_B} = \frac{4}{2.5} = \frac{8}{5}$$

13. (i) 
$$PV^2 = C \Rightarrow TV = C$$

If volume expands temperature decreases.

(ii) 
$$P = KV^2 \Rightarrow \frac{V^3}{T} = constant$$

If volume expands, temperature increases



$$Q = \Delta U + W$$
  
 $Q_2 > Q_1$  as  $W_2 > W_1 & \Delta U_2 > \Delta U_1$ 

14. 
$$\frac{P^2}{\rho}$$
 = constant

$$P = p \frac{RT}{M}$$
(Ideal gas equation)

$$\Rightarrow \frac{P^2}{\rho} = \frac{P}{\rho} \left( \frac{\rho RT}{M} \right) = PT \left( \frac{R}{M} \right) = \text{constant}$$

.. The graph of the above process on the P–T diagram is hyperbola.

For the above process

$$\left(\frac{P^2}{\rho}\right)_1 = \left(\frac{P^2}{\rho}\right)_2 \Rightarrow \frac{P^2}{\rho} = \frac{P_2^2}{\rho/2} \Rightarrow P_2 = \frac{P}{\sqrt{2}} \qquad ...(i)$$

and 
$$P_1T_1 = P_2T_2 \Rightarrow PT = \frac{P}{\sqrt{2}} T_2 \Rightarrow T_2 = \sqrt{2} T$$
 ...(ii)

15. 
$$Q = \Delta U + W \implies +Q = \Delta U + P_0(V_2 - V_1)$$

$$\Rightarrow Q = \Delta U + P_0 \left( \frac{1}{\rho_2} - \frac{1}{\rho_1} \right) \Rightarrow \Delta U = Q + P_0 \left( \frac{1}{\rho_1} - \frac{1}{\rho_2} \right)$$

**16.** Ideal gas equation 
$$P = \frac{\rho}{M}.RT$$

For state A 
$$P_0 = \frac{\rho_0}{M} R T_0$$

For state B 
$$3P_0 = \frac{\rho}{M}R2T_0 \Rightarrow \rho = \frac{3}{2}\rho_0$$

17. 
$$v_A = \sqrt{\frac{3RT}{m}} = \frac{w}{\sqrt{3}}$$
;  $v_B = \sqrt{\frac{3RT}{2m}} = v \implies \frac{w^2}{v^2} = \frac{2}{3}$ 

18. Average KE per molecule in A & B = 
$$\frac{4KT}{\pi}$$

$$(v_{rms})_A = \sqrt{\frac{3RT}{M_A}} \; ; \; (v_{rms})_B = \sqrt{\frac{3RT}{M_B}}$$

$$\Rightarrow \frac{(v_{\rm rms})_A}{(v_{\rm rms})_B} = \sqrt{\frac{M_B}{M_A}} = \sqrt{\frac{M_B}{16M_B}} = \frac{1}{4}$$

No. of mole of 
$$A = \frac{m_A}{M_A}$$

No. of mole of B = 
$$\frac{m_B}{M_B} = \frac{m_{A/2}}{M_{A/16}} = 8n_A$$

Pressure exerted by a gas in the vessel depends on the number of molecules present inside.

19. 
$$(v_{rms})_L = (v_{avg})_R \sqrt{\frac{3RT}{M_1}} = \sqrt{\frac{8RT}{\pi M_2}} \implies \frac{M_1}{M_2} = \frac{3\pi}{8}$$

20. 
$$v_P = \sqrt{\frac{2RT}{M}}; \overline{v} = \sqrt{\frac{8RT}{\pi M}}; v_{rms} = \sqrt{\frac{3RT}{M}}$$

21. Average speed

$$v_{avg} = \frac{1+2+....+N}{N} = \frac{N(N+1)}{2.N} = \frac{N+1}{2}$$

rms speed

$$\begin{split} v_{rms} &= \sqrt{\frac{1^2 + 2^2 + 3^2 + \dots + N^2}{N}} \\ &= \sqrt{\frac{N(N+1)(2N+1)}{6N}} \ = \sqrt{\frac{(N+1)(2N+1)}{6}} \end{split}$$

$$\therefore \frac{v_{rms}}{v_{avg}} = \sqrt{\frac{(N+1)(2N+1)}{6}} \times \frac{2}{(N+1)} = \frac{2}{\sqrt{6}} \sqrt{\frac{2N+1}{N+1}}$$

- 22.  $Q = \Delta U + W$  and  $\Delta U = nC_V \Delta T$  $\Delta U$  can be zero if  $\Delta T$  is zero or Q - W is zero
- 23. Fig A:  $W_A = +ve$  Fig B:  $W_B = +ve$ Fig C:  $W_C = +ve$  Fig D:  $W_D = -ve$  $\therefore$  In process Fig-(D), heat is released.
- 24. For any process  $\Delta U = nC_V \Delta T$ In adiabatic process  $Q = \Delta U + W = 0 \implies \Delta U = -W$ For any process

$$C = \frac{\Delta U}{n\Delta T} + \frac{W}{n\Delta T} = \frac{Q}{n\Delta T} = \frac{\Delta U}{n\Delta T} + \frac{P}{n} \left(\frac{\Delta V}{\Delta T}\right)$$

For Q = 0, C = 0 (adiabatic process)

- 25. At constant volume, work done by gas is zero.
- **26.** Slope of isothermal process  $m_1 = \frac{\Delta P}{\Delta V} = -\frac{P}{V}$

Slope of adiabatic process

$$\mathbf{m}_2 = \frac{\Delta P}{\Delta V} = -\frac{\gamma P}{V} = -\gamma \mathbf{m}_1 = \frac{C_P}{C_V} \mathbf{m}_1$$

27. 
$$PV^{\gamma} = C$$
;  $\ell n P + \gamma \ell n V = \ell n C$ 

$$\Rightarrow \ell nP = -\gamma \ell nV + \ell nC \Rightarrow y = mx + c$$

$$\Rightarrow$$
 m =  $-\gamma = -\frac{-[2.10 - 2.38]}{(1.30 - 1.10)} = -1.4$ 

- : The gas is diatomic
- 28.  $W_{AB} = (2V_0 V_0)P_0 = P_0V_0$ [Isobaric process]

$$W_{BC} = \left| nR(2T_0) \ell n \frac{V_0}{2V_0} \right| = 2P_0 V_0 . \ell n2$$

[Isothermal process]

$$\therefore \frac{Q_{AB}}{W_{BC}} = \frac{\frac{3}{2}P_0V_0 + P_0V_0}{2P_0V_0.\ell n2} = \frac{5}{4\ell n2}$$

29. Final pressure =  $\frac{kx_0}{S}$ 

Work done by gas = P.E. stored in spring =  $1/2 kx_0^2$ Change in internal energy  $\Delta U = |-\Delta W| = 1/2 kx_0^2$ As gas expands,  $\Delta T$  is negative.

- 30. W<sub>OBC</sub> = W<sub>ODA</sub>
  ∴ Net work done = W<sub>OBC</sub> W<sub>ODC</sub> = 0
- 31. For constant pressure process Q =  $nC_p\Delta T = 30nC_p$

For constant volume process Q

= 
$$nC_V\Delta T = n\left(\frac{5}{7}C_P\right)\Delta T \Rightarrow \Delta T = 42^{\circ}C = 42K$$

32. Work done = Area of ABC with V-axis =  $P_0(2V_0 - V_0) + 0 = P_0V_0 = nRT_0 = RT_0$ Change in internal energy =  $nC_V\Delta T$ 

$$=1 \times \frac{3}{2} R \times (4T_0 - T_0) = \frac{9}{2} RT_0$$

:. Heat absorbed

$$=\frac{9}{2} RT_0 + RT_0 = \frac{11}{2} RT_0$$

33.  $C_P - C_V = R$ ; M (0.20 – 0.15) = 2 [M = molar mass]

$$\Rightarrow$$
 M =  $\frac{2}{0.05}$  = 40 g

$$\frac{C_P}{C_W} = \gamma = \frac{0.2}{0.15} = \frac{4}{3} = 1 + \frac{2}{f}$$

- $\Rightarrow$  f = degrees of freedom = 6
- 34. Ans. (C)

$$\Delta U_{CA} = nC_V(T_A - T_C)$$
  
=  $1 \times \frac{3}{2} R \times (300 - 450) = (-225 R)$ 

$$\Delta U_{AB} = nC_V(T_B - T_A)$$
  
= 1 ×  $\frac{3}{2}$  R × (600 – 300) = +450 R

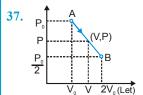
$$\Delta U_{BC} = nCv(T_C - T_B)$$
  
= 1 ×  $\frac{3}{2}$  R × (450 – 600) = -225R

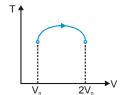
$$\Delta U_{ABCA} = \Delta U_{CA} + \Delta U_{AB} + \Delta U_{BC} = 0$$

35. 
$$W_{adiabatic} = \frac{nR(T_1 - T_2)}{\gamma - 1} = 6R$$

$$\Rightarrow \frac{1 \times R(T_1 - T_2)}{5/3 - 1} = 6R \Rightarrow T_2 = (T - 4)K$$

36. Work done in process 1-3 is greater than that in process 1-2. While change in internal energy is same for both processes
 ∴ Q<sub>2</sub> > Q<sub>1</sub>.





Let  $V_0$  = initial volume =  $2V_0$  = final volume V = volume of any state

then 
$$\frac{P_0 - P_0 / 2}{2V_0 - V} = \frac{P - P_0 / 2}{2V_0 - V}$$

$$\Rightarrow nRT = PV = V \left[ \frac{3P_0}{2} - \frac{P_0}{2V_0} V \right]$$

.. T-V curve is a parabola with vertex above. Hence temperature first increases then decreases.

**38.** For sphere 
$$kA\left(-\frac{dT}{dr}\right) = P$$

$$\Rightarrow k \int (-dT) = \int \frac{dr.P}{A} \Rightarrow -k \int_{0}^{T} dT = \int_{r_{0}}^{r_{2}} \frac{dr.P}{4\pi r^{2}}$$

$$\Rightarrow kT = \frac{P}{4\pi} \left( \frac{r_2 - r_1}{r_1 r_2} \right) \Rightarrow t = (r_2 - r_1) = \frac{kT}{P} 4\pi R^2$$

**39.** Intensity in first case

$$I_1 = \frac{P_1}{4\pi R_1^2} = \frac{\sigma A T_1^4}{4\pi d_1^2}$$

Intensity in second case

$$I_2 = \frac{P_2}{4\pi R_2^2} = \frac{\sigma A T_2^4}{4\pi d_2^2}$$

Given 
$$I_1 = I_2 \Rightarrow \frac{\sigma A T_1^4}{4\pi d_1^2} = \frac{\sigma A T_2^4}{4\pi d_2^2} \Rightarrow \frac{d_2}{d_1} = \left(\frac{T_2}{T_1}\right)^2$$

40. For body A P = 
$$\sigma$$
AT<sup>4</sup>  $\Rightarrow \frac{P}{A} = 100 = \sigma \times 300^4$ 

For body B 
$$\Rightarrow \frac{P}{A} = (\sigma T^4) \in = (1-0.5-0.3) \times [\sigma \times 300^4]$$
  
= 0.2 × 100 = 20 W/m<sup>2</sup>

41. For black body

$$\lambda_0 T = \frac{\lambda_0}{2} T' \Rightarrow T^1 = 2 T$$

$$\frac{P}{P'} = \frac{\sigma A T^4}{\sigma A T^{4}} = \frac{1}{16} \Rightarrow P'T' = (16P)(2T) = 32PT$$

**42.** For surface areas to be same

$$S_{\text{sphere}} = S_{\text{cube}} \implies 4\pi R^2 = 6a^2 \implies \frac{a}{R} = \sqrt{\frac{2\pi}{3}} (>1)$$

Volume ratio

$$\frac{V_{\text{sphere}}}{V_{\text{cube}}} = \frac{\frac{4}{3}\pi R^3}{a^3} = \frac{2R}{a} = \sqrt{\frac{6}{\pi}} (>1)$$

∴ (Mass of water in sphere) > (Mass of water in cube) Energy host by radiation depends on the surface area. Hence initial rate of energy loss by the two area equal. But mass of water inside the sphere is greater, hence it will cool slowly.

43. From Stefan's law of cooling:

eσA(T<sup>4</sup>-T<sub>0</sub><sup>4</sup>) = ms
$$\left(-\frac{dT}{dt}\right)$$
  
⇒ 1 × 5.8 × 10<sup>-8</sup> × π × (0.08)<sup>2</sup> × (500<sup>4</sup> – 300<sup>4</sup>)  
= 10 × 90 × 4.2 ×  $\left(-\frac{dT}{dt}\right)$  ⇒  $\left(-\frac{dT}{dt}\right)$  = 0.067° C/s

44. Newton's law of cooling implies that rate of cooling is proportional to temperature difference if the temperature difference between body and surrounding is small.

Then.

$$\left(-\frac{d\theta}{dt}\right)_{2} = \tan\phi_{2} \alpha (\theta_{2} - \theta_{0}) \text{ and}$$

$$\left(\frac{d\theta}{dt}\right)_{1} = \tan\phi_{1} \alpha (\theta_{1} - \theta_{0}) \implies \frac{\tan\phi_{2}}{\tan\phi_{1}} = \left(\frac{\theta_{2} - \theta_{0}}{\theta_{1} - \theta_{0}}\right)$$

**45.** For same rate of heat transfer the body having higher conductivity will have lower temperature difference. If cylinder with higher conductivity is connected with hot reservoir first then the function temperature T<sub>b</sub>, will be closer to hot reservoir temperature.

46. 
$$KA\left(-\frac{dT}{dx}\right) = \dot{Q} \implies \left(\frac{\alpha}{T}\right)A\left(-\frac{dT}{dx}\right) = \dot{Q}$$

$$\Rightarrow -\int_{T_1}^{T_2} \frac{dT}{T} = \frac{\dot{Q}}{\alpha A} \int_0^2 dx \qquad ....(i) & & \\ \Rightarrow -\int_{T_1}^{T} \frac{dT}{T} = \frac{\dot{Q}}{\alpha A} \int_0^x dx \qquad ...(ii)$$

$$\Rightarrow \ell n \left(\frac{T_1}{T_2}\right) = \left(\frac{\dot{Q}}{\alpha A}\right)L \quad \text{and} \quad \ell n \left(\frac{T_1}{T}\right) = \left(\frac{\dot{Q}}{\alpha A}\right)x$$

$$\Rightarrow T = T_1 \left(\frac{T_2}{T_1}\right)^{x/L}$$

47. From newton's law of cooling.

$$\sigma A(T^4 - T_0^4) = ms \left( -\frac{dT}{dt} \right)$$

$$\Rightarrow \sigma .4\rho r^2 [(T_0 + \Delta T)^4 - T_0^4] = \rho \frac{4}{3} \pi r^3 c \left( -\frac{dT}{dt} \right)$$

$$\Rightarrow \left( \frac{12\sigma T_0^3}{Prc} \right) (T - T_0) = -\frac{dT}{dt}$$

$$\Rightarrow K(T - T_0) dt = -dT \Rightarrow k \int_0^t dt = -\int_0^T \frac{dT}{(T - T_0)} dt$$

 $\Rightarrow$  T = T<sub>0</sub> + (T<sub>1</sub> - T<sub>0</sub>)e<sup>-kt</sup> where K =  $\frac{12\sigma T_0^3}{120}$ 

48. For the cube, net resistance =  $\frac{5R}{6}$  (Where R = thermal resistance of each side)

$$H = \frac{100 - 0}{5R/6}$$

For side A

$$\frac{H}{3} = \frac{100 - \theta_A}{R} \implies \theta_A = 60^{\circ} C$$

49. 
$$H = \frac{T_1 - T_2}{R}$$
 and  $2H = \frac{T_1 - T_2}{R'} \Rightarrow R' = \frac{R}{2}$  (where R & R' are thermal resistances).

$$R = \frac{1}{\frac{L}{kA} + \frac{3L}{kA}} \implies R' = \frac{1}{\frac{kA}{3L} + \frac{k'A}{3L}}$$

$$\Rightarrow$$
 k' =  $\frac{7k}{3}$  (k' = cond. of ADB wire).

50. Heat lost  

$$= \sigma A (T^4 - T_0^4) = -\sigma 4\pi r^2 (T_0^4 - T^4)$$

$$= \frac{d(mL)}{dt} = \rho L \frac{dv}{dt} = \rho L 4\pi r^2 \frac{dr}{dt}$$

$$\Rightarrow -\sigma 4\pi r^2 (T_0^4 - T^4) = \sigma L 4\pi r^2 \frac{dr}{dt}$$

- ⇒ radius decreases with time
- 51. Heat current flow rate is uniform everywhere.
- 52. For same power of radiation  $P_{A} = P_{B} = P_{C} \implies e_{A} \sigma A T_{A}^{4} = e_{B} \sigma A T_{B}^{4} = e_{C} \sigma A T_{C}^{4}$   $\& \lambda_{A} T_{A} = \lambda_{B} T_{B} = \lambda_{C} T_{C} (e_{A} : e_{B} : e_{C} = 1 : \frac{1}{2} : \frac{1}{4})$   $\implies \sqrt{T_{A} T_{C}} = T_{B} \qquad \text{or}$   $\sqrt{e_{A} T_{A}} \sqrt{e_{C} T_{C}} = e_{B} T_{B} \qquad \& \qquad \sqrt{\lambda_{A} \cdot \lambda_{C}} = \sqrt{\lambda_{B}}$

53. 
$$T_P = 50^{\circ}\text{C}$$
;  $T_Q = 45^{\circ}\text{C}$   
∴ Heat will flow from P to Q.

54. 
$$\dot{Q} = \frac{KA(4-0)}{10-x} = \frac{3KA(0+4)}{x} \implies x = 7.5 \text{ m}$$

$$\frac{-4 \text{ C}}{\text{ICE} \times 3K} = \frac{3KA(0+4)}{x} \implies 0 \text{ C}$$
WATER (10-30) K

55. 
$$R = \frac{1}{\frac{KA}{L/2} + \frac{KA}{L/2}} = \frac{KA}{4L};$$

$$R' = \frac{1}{\frac{KA}{3L/4} + \frac{KA}{L/4}} = \frac{3}{4}R$$

$$H_{II} = \frac{\Delta T}{3R/4} = \frac{4}{3} \frac{\Delta T}{R} = \frac{4}{3} \times 1.2 = 1.6W$$

56. Rate of cooling  $= ms \left( -\frac{d\theta}{dt} \right) = 4\sigma A T_0^3 \Delta T$   $\Rightarrow 4\sigma A \times T_0^3 (50 - 20) = 10$ and  $4\sigma A \times T_0^3 (35 - 20) = ms \left( -\frac{d\theta}{dt} \right) = ms \left( \frac{0.2}{60} \right)$   $\Rightarrow ms = \frac{60}{0.2} \times \left( \frac{15 \times 10}{30} \right) = 1500 \text{ J/°C}$ 

- 58. Wien's displacement law.  $\lambda_1 T_1 = \lambda_2 T_2 = b = 2.8 \times 10^{-3} \text{ km}$   $\Rightarrow 3000 \times \lambda_1 = T_2 \times (\lambda_2) \cong 3 \times 10^{-3} \text{ km}$   $\Rightarrow \lambda_1 = 1 \text{ } \mu\text{m} \text{ & } [\lambda_2 \lambda_1] = 9 \text{ } \mu\text{m}$   $\Rightarrow \lambda_2 = 10 \text{ } \mu\text{m}$   $\Rightarrow T_2 = 300 \text{ K}$
- 59. For a grey body  $\alpha + r + t = 1$  if  $\alpha = 0.4$ , r = 0.6then t = 1 - 0.4 - 0.6 = 0. The body is opaque

60. (i) 
$$Q = \frac{K_1A(\theta + 25)}{t_1} = \frac{K_2A(25 - \theta)}{t_2}$$

$$\Rightarrow \frac{KA(\theta + 25)}{2} = \frac{KA(25 - \theta)}{3} \Rightarrow \theta = -5^{\circ}C$$

$$-25 C Q + 25 C$$

$$t_1 = 2 t_2 = 3$$

$$K_1 K_2$$

(ii) 
$$\dot{Q} = \frac{K_1 A(\theta + 25)}{t_1} = \frac{K_2 A(25 - \theta)}{t_2}$$

$$\Rightarrow \frac{2A(\theta+25)}{2} = \frac{3A(25-\theta)}{3} \Rightarrow \theta = 0^{\circ}C$$

**61.** 
$$\dot{Q} = \frac{T_A - T_B}{\frac{L}{k_3 A}} = \frac{T_A - T_B}{\frac{L}{k_1 A} + \frac{L}{k_2 A}} \implies k_3 = \frac{k_1 k_2}{k_1 + k_2}$$

62. Fig A: 
$$20 = \left(\frac{100 - 0}{\frac{L}{kA} + \frac{L}{kA}}\right) \times 4$$
 ...(i)

Fig A: 
$$20 = Q = (100 - \theta) \left[ \frac{kA}{L} + \frac{kA}{L} \right] t$$
 ...(ii)

Equation (i) ÷ (ii) 
$$1 = \frac{4/2}{2/t} t = 1 \text{ min.}$$

**63.** For an elemental spherical shells,

$$\dot{\mathbf{Q}} = \mathbf{K} 4\pi \mathbf{r}^2 \left( -\frac{d\mathbf{T}}{d\mathbf{r}} \right) \Rightarrow \dot{\mathbf{Q}} \int_{r_1}^{r_2} \frac{d\mathbf{r}}{\mathbf{r}^2} = -4\pi \mathbf{K} \int_{T_1}^{T_2} d\mathbf{T}$$

$$\Rightarrow \dot{Q} \left( \frac{r_2 - r_1}{r_1 r_2} \right) = 4\pi K (T_1 - T_2) \Rightarrow \dot{Q} \propto \left( \frac{r_1 \cdot r_2}{r_2 - r_1} \right)$$

**64.** 
$$\dot{Q} = \frac{T_2 - T_1}{\frac{x}{KA} + \frac{4x}{2K.A}} = \frac{KA(T_2 - T_1)}{3x} = \left[\frac{KA(T_2 - T_1)}{x}\right] f$$

then 
$$f = 1/3$$

65. Let x= percentage of water solidified then heat lost = Heat gained  $\Rightarrow$  x × 3.36 × 10<sup>5</sup> = (100 – x) × 21 × 10<sup>5</sup>

$$\Rightarrow$$
 x =  $\frac{100}{1.16}$  = 86.2%

**66.**  $P = P_0 - aV^2$ 

From ideal gas equation PV=nRT

$$\Rightarrow$$
 RT =  $(P_0 - aV^2)V$  (n=1)

$$\Rightarrow T = \left(\frac{P_0 V - aV^3}{R}\right) \Rightarrow \frac{dT}{dV} = 0 = \left(\frac{P_0 - 3aV^2}{R}\right)$$

$$\Rightarrow$$
 V =  $\sqrt{\frac{P_0}{3a}}$  and  $\frac{d^2T}{dV^2} = -\frac{6aV}{R}$  (<0)

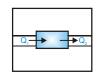
$$\therefore T_{\text{max}} = \frac{(P_0 - aV^2)V}{R} = \frac{2P_0}{3R} \sqrt{\frac{P_0}{3a}}$$

67. He and Ne are monatomic gas.

**68.** 
$$Q_1 + 36 = Q_2$$

$$\Rightarrow \frac{KA(100 - \theta)}{L} + 36 = \frac{KA(\theta - 4)}{L}$$

$$\Rightarrow \theta = 76^{\circ}$$



69. Area under the curve is equal to number of molecules of the gas sample.

Hence 
$$N = \frac{1}{2} a V_0 \implies aV_0 = 2N$$

$$V_{avg} = \frac{1}{N} \int_{0}^{\infty} vN(V)dV = \frac{1}{N} \int_{0}^{V_0} C. \left(\frac{a}{V_0}V\right) dV = \frac{2}{3}V_0$$

$$\Rightarrow \frac{V_{avg}}{V_0} = \frac{2}{3}$$

$$V_{\rm rms}^2 = \frac{1}{N} \int\limits_0^\infty V^2 N(V) dV = \frac{1}{N} \int\limits_0^{v_0} V^2 \left( \frac{a}{V_0} V \right) dV = \frac{V_0^2}{2}$$

$$\Rightarrow \frac{V_{rms}}{V_0} = \frac{1}{\sqrt{2}}$$

Area under the curve from 0.5  $V_0$  to  $V_0$  is 3/4 of total area

70. 
$$Q = W = nRT \ln \frac{V_f}{V_c}$$

$$T = \frac{Q}{nR\ell nV_{_f} / V_{_i}} = \frac{1500}{0.5 \times 25 / 3 \times \ell n3}$$

$$= \frac{1500}{0.5 \times 25 / 3 \times 1} = 360 \text{K}$$

71. At 30° true length is given by = SR  $(1 + \alpha_{zinc} \Delta T)$  $=100 (1+26 \times 10^{-6} \times 30) = 100.078 \text{ cm}$ 

At 0°, True length is given by

$$= \frac{\text{SR} \left( 1 + \alpha_{\text{zinc}} \Delta T \right)}{\left( 1 + \alpha_{\text{glass}} \Delta T \right)} = \frac{100.078}{\left( 1 + 8 \times 10^{-6} \times 30 \right)} = 100.054 \text{ cm}$$

**72.** Length 
$$\ell = \ell_0 (1 + \alpha \Delta T) = \ell_0 (1 + 20\alpha)$$

Area 
$$A=A_0(1+\beta\Delta T)=6\ell_0^2(1+40\alpha)$$

Area 
$$A=A_0 (1+\beta \Delta T) = 6\ell_0^2 (1+40\alpha)$$
  
Volume  $V=V_0 (1+\gamma \Delta T) = \ell_0^3 (1+3\alpha \Delta T) = \ell_0^3 (1+60\alpha)$ 

Density 
$$\rho = \frac{\rho_0}{1 + \gamma \Delta T} = \frac{\rho_0}{1 + 60\alpha}$$

73. 
$$\ell = \frac{\Delta V}{A_0} = \frac{V_0 (\gamma - 3\alpha)t}{A_0}$$

- 74. Tensile Stress =  $(Y_{steel})$   $\left(\frac{\Delta \ell}{\ell}\right) = Y_s \left(\alpha_b \alpha_s\right) \Delta T$ =  $200 \times 10^9 (0.8 \times 10^{-5}) (200) = 3.2 \times 10^8 \text{ Nm}^{-2}$ =  $0.32 \text{ GNm}^{-2}$
- **75.** At normal temperature  $C_v = \frac{f}{2} R = \frac{5}{2} R$

At any temperature  $C_p - C_v = \left(\frac{f}{2} + 1\right) - \frac{f}{2} R = R$ 

from process  $T = k_1 V^2$  and ideal gas equation PV = nRT we have  $PV^{-1} = constant \implies x = -1$ 

$$\Rightarrow$$
 C = C<sub>v</sub> +  $\frac{R}{1-x}$  = C<sub>v</sub> +  $\frac{R}{1+1}$  = C<sub>v</sub> +  $\frac{R}{2}$ 

At normal temperature  $C = \frac{5}{2}R + \frac{R}{2} = 3R$ 

76. Required heat Available heat  $10 \text{ gice } (0^{0}\text{C})$  5 g steam  $(100^{0}\text{C})$   $\downarrow 800 \text{ cal}$   $\downarrow 2700 \text{ cal}$  10 g water  $(0^{0}\text{C})$  5 g water  $(100^{0}\text{C})$   $\downarrow 1000 \text{ cal}$ 

 $10 \, \text{g water} \, (100^0)$ 

So available heat is more than required heat therefore final temperature will be  $100^{0}$ C.

Mass of vapour condensed  $=\frac{800+1000}{540} = \frac{10}{3} g$ 

Total mass of water =  $10 + \frac{10}{3} = \frac{40}{3} = 13\frac{1}{3} \text{ g}$ 

Total mass of steam

- 77.  $C_{Pmix} = \frac{n_1 C p_1 + n_2 C p_2 + n_3 C p_3}{n_1 + n_2 + n_3}$   $= \frac{(4) \left(\frac{7}{2}R\right) + 2\left(\frac{5}{2}R\right) + 1(4R)}{4 + 2 + 1} = \frac{16}{7}R$
- 78.  $PV^2 = constant \implies P \propto V^{-2} \implies \frac{\Delta P}{P} = -2\frac{\Delta V}{V}$ 
  - ⇒ Bulk modulus  $K = \frac{\Delta P}{-\frac{\Delta V}{V}} = 2P$
  - As PV = nRT So  $K \propto \frac{1}{V^2}$  and  $K \propto T^2$

79.  $C = C_V + \frac{R}{1 - x} = \frac{3}{2}R + \frac{R}{1 - x} < 0$  $\Rightarrow \frac{5 - 3x}{1 - x} < 0 \Rightarrow 1 < x < 1.67$ 

## Part # II: Assertion & Reason

 1.
 C
 2.
 B
 3.
 D
 4.
 A
 5.
 A
 6.
 A
 7.
 A

 8.
 C
 9.
 D
 10.
 A
 11.
 D
 12.
 A
 13.
 A
 14.
 A

 15.
 D
 16.
 D
 17.
 D
 18.
 A
 19.
 A
 20.
 A
 21.
 C

 22.
 A
 23.
 A
 24.
 A
 25.
 A
 26.
 A
 27.
 C
 28.
 A

 29.
 A
 30.
 A
 31.
 A
 32.
 B

### **EXERCISE - 3**

### Part # I: Matrix Match Type

1. Isobaric process  $\Rightarrow$  P = constant Isothermal process  $\Rightarrow$  T = constant  $\Rightarrow \Delta U = 0 \Rightarrow U = constant$ Isoentropy process

$$\Rightarrow \Delta S = \frac{\Delta Q}{T} = 0 \Rightarrow \Delta Q = 0$$

No heat exchange Isochoric process  $\Rightarrow$  V = constant  $\Rightarrow$  dW = PdV = 0

2. When A & B are mixed ms (T-20) = (2m) s (40-T)

⇒ 
$$T = \frac{100}{3} = 33.3$$
°C

When A & C are mixed  $ms(T-20) = (3m) s (60-T) \Rightarrow T = 50^{\circ}C$ When B & C are mixed  $(2m) s (T-40) = (3m) s (60-T) \Rightarrow T = 52^{\circ}C$ When A, B & C are mixed  $ms(T-20) + (2m)s(T-40) = (3m)s(60-T) \Rightarrow T = 46.67^{\circ}C$ 

- 3. Let  $R_{BC} = R$  then  $R_{AB} = R_{AC} = 2R$  as  $R = \frac{\ell}{kA}$   $\frac{100 T_B}{2R} = \frac{T_B 0}{R} \implies T_B = 67.7^{\circ}C$   $\left(\frac{\Delta Q}{\Delta t}\right)_{AB} = \left(\frac{\Delta Q}{\Delta t}\right)_{BC} \text{ and } \left(\frac{\Delta Q}{\Delta t}\right)_{AB} = \frac{2}{3} \left(\frac{\Delta Q}{\Delta t}\right)_{AC}$
- 4. From given V–T graph we cannot tell the nature of gas slope of V–T graph =  $\frac{nR}{P}$

From graph  $\left(\frac{nR}{P}\right)_A > \left(\frac{nR}{P}\right)_B \implies \left(\frac{n}{P}\right)_A > \left(\frac{n}{P}\right)_B$ 

 $\Rightarrow$  Cannot say anything about  $\frac{n_{_{A}}}{n_{_{B}}}\,\&\,\frac{P_{_{A}}}{P_{_{B}}}$ 

5. For(A) as 
$$PV = \frac{1}{3} \text{ mNv}^2_{\text{rms}} = \frac{2}{3} \text{ E so in } P = \frac{2}{3} \text{ E},$$

E is translational kinetic energy of unit volume.

### For (B):

In U = 3RT, U is not internal energy of one mole as for monoatomic gas U = 3/2 nRT

### For(C):

In W=  $P(V_f - V_i)$ ; w is work done in isobaric process.

For (D): 
$$\operatorname{In} \Delta U = \operatorname{nC}_{v} \Delta T$$

 $\Delta U$  is change in internal energy for every process.

6. As 
$$Q = nCdT$$
 and  $dT = \frac{Q}{nC}$ 

Therefore molar heat constant C is the determining factor for rate of change of temperature of a gas as heat is supplied to it. It is minimum for isochoric process of a

monoatomic gas  $\left(C_{V} = \frac{3}{2}R\right)$ , resulting in greatest slope

$$\left(\frac{dT}{Q}\right)$$
 i.e. curve 1.

For isobaric process of monoatomic gas and isochoric process of diatomic gas, their heat capacities are same

$$\left(\frac{5}{2}R\right)$$
, therefore both are represented by curve 2.

For isobaric process of diatomic gas  $C_p = \frac{7}{2}R$  that is represented by curve 3.Q axis represent isothermal process and  $\Delta T$  axis represent adiabatic process.

7. Initially rate of heat flow will be maximum at A and minimum at B as there is no temperature difference across section B.

In steady state  $\frac{dQ}{dt}$  will be same.

In steady state 
$$\frac{dQ}{dt} = -KA \frac{dT}{dx} = same$$

& 
$$\frac{dT}{dt} = 0 \Rightarrow \left(\frac{dT}{dx}\right) \propto \frac{1}{A} \Rightarrow \left(\frac{dT}{dx}\right)$$

will be maximum at B & minimum at A

8. Isothermal bulk modulus = 
$$P = \frac{RT}{V}$$

Adiabalic bulk modulus = 
$$\gamma P = \frac{5RT}{3V}$$

Slope of PV graph in isothermal process

$$\frac{P}{V} = -\frac{RT}{V^2}$$

Slope of P-V graph in adiabatic process

$$\frac{\gamma P}{V} = -\frac{5P}{3V}$$

9. 
$$W = \int PdV = \int_{V_0}^{4V_0} 2VdV = (V^2)_{V_0}^{4V_0} = 15V_0^2 = 15 \text{ units}$$

From PV = nRT,  $2V^2$  = nRT

$$\Rightarrow 2(V_2^2 - V_1^2) = nR(\Delta T) \Rightarrow nR\Delta T = 30V_0^2$$

$$\Delta U = nC_{V}\Delta T = \frac{nR}{\gamma - 1}\Delta T = \frac{30V_{0}^{2}}{\gamma - 1} = \frac{30(1)^{2}}{7/5 - 1} = \frac{30}{2}(5)$$
= 75 units

$$O = 75 + 15 = 90 \text{ units}$$

Molar heat capacity

$$C = C_V + \frac{R}{1 - x} = \frac{5}{2} R + \frac{R}{1 - (-1)} = \frac{5}{2} R + \frac{R}{2} = 3R$$

$$= 3 \times \frac{25}{3} = 25 \text{ units}$$

### 10. For (A)

$$R_y = \frac{\ell}{K_y A} = \frac{\ell}{2K_x A} = \frac{R}{2}$$
  $A = \frac{R}{R}$   $R = \frac{R/2}{R/2}$   $R/2 = \frac{R}{R}$ 

No heat current flows through rod CD

So B 
$$R/2$$
  $R/2$   $R/2$ 

#### For (R

$$\frac{R}{A} = \frac{2R/3}{R} = \frac{R/2}{F} = A = \frac{13R/6}{F}$$

#### For (C)

Total heat current form A to F,

$$I = \frac{100 - 0}{\frac{13}{6}R} = \frac{600}{13R}$$

Let temperature of B be T<sub>B</sub> then

$$I = \frac{100 - T_B}{R} = \frac{600}{13R} \implies T_B = \frac{700}{13} \text{°C}$$

#### For (D)

As heat current is inversely proportional to heat resistance.

So heat current in BD = 
$$\left(\frac{2R}{R+2R}\right)I = \frac{2}{3}I$$

$$\Rightarrow \frac{T_B - T_D}{R/2} = \frac{2}{3}I = \frac{2}{3} \left(\frac{600}{13R}\right)$$

$$\Rightarrow$$
  $T_D = \frac{700}{13} - \frac{200}{13} = \frac{500}{13}$   $^{\circ}$   $C$ 

11. 
$$P = \frac{\rho}{M_w} RT$$

### For (A):

For AB 
$$P \propto V \Rightarrow T \propto V^2 \Rightarrow T \propto \rho^{-2}$$

For BC 
$$V = constant \Rightarrow \rho = constant$$

For CA 
$$P = constant \Rightarrow \rho T = constant$$

### For (B)

For AB 
$$P \propto T \Rightarrow \rho = constant$$

For BC 
$$T = constant \Rightarrow P \propto \rho$$

For CA 
$$P = constant \Rightarrow \rho T = constant$$

### For (C)

For AB 
$$P = constant \Rightarrow \rho T = constant$$

For BC 
$$T = constant \Rightarrow P \propto \rho$$

For CA 
$$V = constant \Rightarrow \rho = constant$$

### For (D)

For AB 
$$\rho \propto T \Rightarrow P \propto T^2$$

For BC 
$$T = constant \Rightarrow P \propto \rho$$

For A 
$$\rho = \text{constant} \Rightarrow P \propto T$$

### Part # II: Comprehension

### Comprehension#1

1. 
$$P \propto V \Rightarrow PV^{-1} = constant \Rightarrow x = -1$$

$$\Rightarrow$$
 C = C<sub>v</sub> +  $\frac{R}{2}$  =  $\frac{5R}{2}$  +  $\frac{R}{2}$  = 3R

2. 
$$Q = nC\Delta T = n(3R)\Delta T = n(3R)(3T) = 9nRT = 9P_1V_1$$

#### Comprehension#2

1,2 Let heat is supplied at a rate of  $k_1$  cal/min then

$$k_1 \times 1 = m(0.5)\theta_1$$

$$k_1 \times 4 = m(80) k_1 \times 2 = m(1) (\theta_2)$$

$$\Rightarrow$$
  $k_1 = 20 \text{ m} \Rightarrow \theta_1 = 40^{\circ}\text{C}, \theta_2 = 40^{\circ}\text{C}$ 

Therefore initial temperature  $=-40^{\circ}$ C

Final temperature = +40°C

### Comprehension#3

- 1. Since P is constant = 1 atm, heat added will cause temperature rise. From the phase diagram, A will sublime while B will first melt and then boils.
- 2. From the phase diagram, at 2 atm & 220 K, A is gas & B is solid

#### Comprehension#4

- On increasing temperature (giving heat), U increases. Now r<sub>avg</sub> increases for A while decreases for B.
- 2. The equilibrium remain unchanged but average distance increases.

3. We have  $\Delta r_{avg} = \left(\frac{1.0003 - 0.9999}{2}\right) r_0$  (from equilibrium position)

$$\therefore \frac{\Delta r}{r} = \alpha \Delta T \implies \alpha = 2 \times 10^{-5} / K$$

### Comprehension#5

1. L et M be the mass of solid

$$\therefore \text{ Volume displaced} = \frac{1 \times M}{2 \times \rho_s}$$

Thrust force 
$$= \rho_L \times \frac{M}{2\rho_s} g = Mg$$
  $\therefore \rho_L = 2\rho_S$ 

2. If 
$$\gamma_{Liq} > \gamma_{solid}$$
 Also  $\rho_L Vg = Mg$ 

As T  $\uparrow$ ,  $\rho_{\rm I} \downarrow$ , so V displaced  $\uparrow$ 

Fraction of solid submerged should increased.

3. If fraction of solid submerged doesn't change, then

$$\frac{\rho_0 V_0 (1 + 3\alpha \Delta T)}{\left(1 + \gamma_{Liq} \Delta T\right)} = \text{constant} \Rightarrow \gamma_{liq} = 3\alpha_S$$

4. If h doesn't change

$$V = Ah : \gamma_L = 2\alpha_S$$

5. If volume change in solid is zero.

Let at T', solid sinks 
$$\rho_0 \frac{V}{2}g = V \rho_s g(Initially)$$

Finally 
$$\rho_T Vg = V \rho_S g = \frac{\rho_0}{2}$$

$$\rho_T = \frac{\rho_0}{(1 + \gamma_L \Delta T)} = \frac{\rho_0}{2} \implies 2 = 1 + \gamma_L \Delta T = \Delta T = \frac{1}{\rho_L}$$

$$\Rightarrow$$
 Temperature = T+ $\frac{1}{\gamma_L}$ 

## Comprehension#6

- 1. At temperature above 4°C, temperature of water above is less as compared to below as water is heated by radiation of longer wavelength.
- 2. At temperature below 4°C, temperature above is less as compared to below & thus water remain is it is due to higher volume at the upper surface.

3. 
$$\frac{Ldm}{dt} = \frac{\Delta T \cdot kA}{x}, dm = \rho A dx$$

$$\Rightarrow \frac{L\rho A dx}{dt} = \frac{\Delta T k A}{x} = L\rho \frac{x^2}{2} = \Delta T k \times t$$

Thickness,  $x \propto t^{1/2}$ 

**4.** Transition of ice starts from the top & decreases below to the bottom.

### Comprehension#7

- 1. As  $Q = n_A C_{vA} \Delta T = n_B C_{vB} \Delta T \Rightarrow n_A C_{vA} = n_B C_{vB}$ But volume is constant  $\Rightarrow \frac{n_A}{n_B} = \frac{\Delta P_A}{\Delta P_B} = \frac{2.5}{1.5} = \frac{5}{3}$ 
  - $\Rightarrow \frac{C_{vB}}{C_{vA}} = \frac{5}{3} = \frac{5/2R}{3/2R}$
  - ⇒ Gas B is diatomic & gas A is monoatomic
- 2. As  $n_A = \frac{5}{3} n_B$  so  $\frac{125}{M_A} = \frac{5}{3} \left( \frac{60}{M_B} \right)$  $\Rightarrow 5 M_B = 4M_A \Rightarrow Gas A = Ar, gas B = O_2$
- 3. Number of molecules in A =  $n_A N_A$ =  $\frac{125}{40} N_A = 3.125 N_A$
- 4.  $U = nC_VT = \frac{125}{40} \times \frac{3}{2} \times 2 \times 300 = 2812.5 \text{ cal}$

### Comprehension#8

2. Ans. (D)

$$\frac{\Delta Q}{t} = \frac{1 \times 4200 \times 2}{20} \text{J/sec} = 420 \text{W}$$

3.  $\frac{d\theta}{dt} = +K(T_S - T_L) \implies \frac{2}{20} = K(40) \implies K = \frac{1}{400}$   $\int_{60^\circ}^{40} \frac{d\theta}{(20 - \theta)} = +K \int_0^t dt \; ; \; \ln(20 - \theta)|_{60}^{40} = -\frac{1}{400}t$   $\implies \ln\left(\frac{20}{40}\right) = -\frac{1}{400}t \implies t = 277s$ 

#### Comprehension#9

- 1.  $M_{\text{mix}} = \frac{n_1 M_1 + n_2 M_2}{n_1 + n_2} = \frac{5 \times 4 + 2 \times 2}{7} = \frac{24}{7} \text{ g}$
- 2.  $C_{V_{mix}} = \frac{\frac{5}{2} \times 2R + \frac{3}{2} \times 5R}{7} = \frac{f_{mix}}{2}R = f_{mix} = 3.57$
- 3.  $C_{V_{\text{mix}}} = \frac{\frac{5}{2} \times 2R + \frac{3}{2} \times 5R}{7}, C_{P_{\text{mix}}} = \frac{\frac{7}{2} \times 2R + \frac{5}{2} \times 5R}{7}$   $\gamma_{\text{mix}} = \frac{C_{P_{\text{mix}}}}{C_{..}} = 1.56$

4. Internal energy He = 100 J Internal energy H = 200 J while mixing, they don't interact Internal energy of mix = (100 + 200) J = 300 J

### Comprehension#10

- Stress developed at junction are same
- As cross sectional area is same & equal and opposite force acting on both rods.
   So F/A= same.
- 3. Let shifting in junction be x towards right then

$$\left(\frac{\Delta\ell}{\ell}\right)_1 = \frac{\ell_1\alpha_1\Delta T - x}{\ell_1}, \left(\frac{\Delta\ell}{\ell}\right)_2 = \frac{\ell_2\alpha_2\Delta T + x}{\ell_2}$$

But 
$$Y_1 \left(\frac{\Delta \ell}{\ell}\right)_1 = Y_2 \left(\frac{\Delta \ell}{\ell}\right)_2$$

So x = 
$$\frac{\ell_1 \ell_2 (Y_1 \alpha_1 - Y_2 \alpha_2) \Delta T}{Y_1 \ell_2 + Y_2 \ell_1}$$

### Comprehension#11

- 1.  $\frac{Q_1}{Q_2} = \frac{T_1}{T_2} \implies Q_1 = \left(\frac{T_1}{T_2}\right)Q_2 = \left(\frac{300}{273}\right)(80) = 87.9kcal$
- 2.  $W = Q_1 Q_2 = 87.9 80 = 7.9 \text{ kcal} = 33.18 \text{ kJ}$
- 3.  $\beta = \frac{T_2}{T_1 T_2} = \frac{273}{27} = 10.1$

### Comprehension#12

- 1. Change is entropy =  $\frac{\Delta Q}{T}$  $\Rightarrow$  Unit of entropy =  $JK^{-1}$
- 2. When milk is heated, its entropy increases as it is irreversible process.
- 3. After a long time disorder is increased.

## Comprehension#13

- 1.  $450 = m(0.5)(150) \implies m = 6g$
- 2.  $L = \frac{Q}{m} = \frac{800 450}{6} = \frac{350}{6} = \frac{175}{3} \text{ cal/g}$
- 3.  $s = \frac{Q}{m\Delta T} = \frac{200}{6(240 150)} = \frac{10}{27} \text{ cal/g}^{\circ}\text{C}$

### Comprehension#14

1.  $Q_{BC} = 0 \Rightarrow \Delta U_{BC} = -W_{BC} = -400 \text{ J}$ 

2. For complete cycle Q = W

$$\Rightarrow Q_{AB} + Q_{BC} + Q_{CA} = W_{AB} + W_{BC} + W_{CA}$$
$$\Rightarrow 700 + 0 + (-100) = 700 + 400 + W_{CA}$$

$$\Rightarrow$$
 700 + 0 + (-100) = 700 + 400 + W<sub>CA</sub>

$$\Rightarrow$$
 W<sub>CA</sub> = -500 J

3. 
$$\eta = \frac{W_{net}}{Q_{input}} \times 100 = \frac{600}{700} \times 100 = \frac{600}{7} = 85.71\%$$

## Comprehension#15

1. 
$$\eta = \frac{T_1 - T_2}{T_1} = 0.5 \implies T_1 = 560 \text{K}$$

$$\eta' = 0.7 = \frac{T_1' - T_2}{T_1'} = \frac{T_1' - 280}{T_1'} \Rightarrow \frac{2800}{3}$$

$$\Rightarrow$$
  $T_1'-T_1=\frac{1120}{3}$ 

2. 
$$\eta_{max} = \frac{T_1 - T_2}{T_1} \times 100 = \frac{600 - 300}{600} \times 100 = 50\%$$

3. 
$$\eta = 1 - \frac{T_2}{T_1} = \frac{1}{6}; \eta' = 1 - \frac{T_2}{T_1 + 100} = \frac{1}{3} \implies T_2 = \frac{1000}{3} \text{K}$$

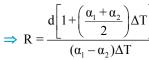
#### EXERCISE - 4

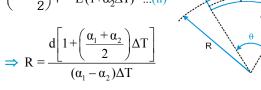
### Subjective Type

1. Here:

$$\left(R + \frac{d}{2}\right)\phi = L(1 + \alpha_1 \Delta T) \dots (i)$$

$$\left(R - \frac{d}{2}\right)\phi = L\left(1 + \alpha_2 \Delta T\right) \dots (ii)$$

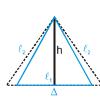




Since 
$$\left(\frac{\alpha_1 + \alpha_2}{2}\right) \Delta T \ll 1$$

$$=\frac{d}{(\alpha_1-\alpha)\Delta T}=\frac{d}{(\alpha_1-\alpha_2)(t_2-t_1)}$$

2.



$$h^2 = L_2^2 - \frac{\ell_1^2}{4} = constant$$

$$\Rightarrow 2L_2 \Delta L_2 - \frac{2L_1 \Delta L_1}{4} = 0$$

$$\Rightarrow$$
 4L<sub>2</sub> (L<sub>2</sub> $\alpha_2\Delta T$ ) =L<sub>1</sub>(L<sub>1</sub> $\alpha_1\Delta T$ )

$$\Rightarrow$$
  $4L_2^2\alpha_2 = L_1^2\alpha_2$ 

3. (i) Thermal current = 
$$\frac{Temperature difference}{R_H}$$

where 
$$\frac{1}{R_H} = \frac{K_1 A}{\ell} + \frac{K_2 A}{\ell} = \frac{(K_1 + K_2)a^2}{a}$$
  
=  $(60 + 40)(3 \times 10^{-2}) = 3 \text{ WK}^{-1}$ 

Thermal current

$$= 80 \times 3 = 240 \text{ W}$$

Ratio of thermal currents

$$\frac{H_{Cu}}{H_{Al}} = \frac{K_{Cu}}{K_{Al}} = \frac{60}{40} = 1.5$$

4. 
$$Q = KA \frac{(\theta_1 - \theta_2)t}{\ell} = mL \implies m \times 335 \times 10^3$$

= 
$$0.01 \times \frac{0.54 \times 45 \times 6 \times 60 \times 60}{5 \times 10^{-2}} \Rightarrow m = 0.261 \text{ kg}$$

Therefore mass of ice left in the box after 6 hours = (4-0.261) kg = 3.739 kg

5. In steady state rate of flow of heat in the whole system will be same.

$$\frac{{\rm KA}(200-\theta_1)}{\ell} = \frac{2{\rm KA}(\theta_1-\theta_2)}{\ell} = \frac{1.5{\rm KA}(\theta_2-18)}{\ell}$$

$$\Rightarrow$$
 200 -  $\theta_1$  = 2 $\theta_1$  - 2 $\theta_2$  & 2 $\theta_1$  - 2 $\theta_2$  = 1.5 $\theta_2$  - 27

$$\Rightarrow$$
  $\theta_1 = 116^{\circ}\text{C}, \theta_2 = 74^{\circ}\text{C}$ 

**6.** (i) Temperature gradient

$$= \frac{T_1 - T_2}{\ell} = \frac{100 - 0}{1} = 100$$
°C/m

(i) Steady state temperature of element dx : T = 100 (1-x)Heat absorbed by the element to reach steady state

$$dQ = (dm)s \Delta T = (\lambda dx)s(T - 0)$$

 $\Rightarrow$  dQ = 20 [100 (1-x)] dx

Total heat absorbed by the rod

$$Q = \int dQ = 2000 \int_{0}^{1} (1 - x) dx = 1000 J$$

$$\Rightarrow 2L_{2}\Delta L_{2} - \frac{2L_{1}\Delta L_{1}}{4} = 0$$

$$\Rightarrow 4L_{2}(L_{2}\alpha_{2}\Delta T) = L_{1}(L_{1}\alpha_{1}\Delta T)$$

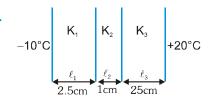
$$\Rightarrow 4L_{2}^{2}\alpha_{2} = L_{1}^{2}\alpha_{1}$$

$$\Rightarrow 2\theta = 10 \Rightarrow \theta = 5^{\circ}C$$
7. 
$$\frac{\Delta Q}{\Delta t} = \text{same So } \frac{KA(20 - 10)}{\ell} = \frac{2KA(10 - \theta)}{\ell}$$

$$\Rightarrow 2\theta = 10 \Rightarrow \theta = 5^{\circ}C$$

$$\Rightarrow$$
 2  $\theta$  = 10  $\Rightarrow$   $\theta$  = 5°C

8



Power required

$$= \frac{K_{eq}A(T_1 - T_2)}{\ell}$$

$$= \frac{\ell}{\left(\frac{\ell_1}{K_1} + \frac{\ell_2}{K_2} + \frac{\ell_3}{K_2}\right)} \left[\frac{A(T_1 - T_2)}{\ell}\right]$$

$$= \frac{A \left(T_1 - T_2\right)}{\frac{\ell_1}{k_1} + \frac{\ell_2}{k_2} + \frac{\ell_3}{k_3}}$$

$$= \frac{(137)(30)}{\left(\frac{2.5}{0.125} + \frac{1}{1.5} + \frac{25}{1}\right) \times 10^{-2}} = 9000 \text{ W}$$

9. By using Wien's displacement law

$$T = \frac{b}{\lambda_m} = \frac{2.89 \times 10^{-3}}{1.5 \times 10^{-6}} = 1927 \text{ K}$$

10. Let m = mass of steam required per hour

Heat needed

= 
$$(10 \times 1000 \text{ kg}) \times (1\text{cal/g}) \times (80-20)$$
  
=  $60 \times 10^4 \text{ cal/hour}$ 

Heat supplied

$$= m \times 1 \times (150 - 100) + m \times 540 + m \times 1 \times (100 - 90)$$

Heat needed = Heat supplied

$$\Rightarrow$$
 60 × 10<sup>4</sup> = 600 m = 1000 gm = 1 kg

11. (i) 
$$\therefore P_A = P_B$$
  
  $\therefore e_A \sigma A_A T_A^4 = e_B \sigma A_B T_B^4$ 

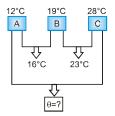
$$\Rightarrow T_{B} = \left(\frac{e_{A}}{e_{B}}\right)^{1/4} T_{A} = \left(\frac{0.01}{0.81}\right)^{\frac{1}{4}} 5802 = 1934K$$

(ii) According to Wein's displacement law

$$\lambda_{A}T_{A} = \lambda_{B}T_{B} \Rightarrow \lambda_{B} = \left(\frac{5802}{1934}\right)\lambda_{A} \Rightarrow \lambda_{B} = 3\lambda_{A}$$

Also 
$$\lambda_B - \lambda_A = 1 \mu m \Rightarrow \lambda_B - \frac{\lambda_B}{3} = 1 \mu m \Rightarrow \lambda_B = 1.5 \mu m$$

13. When A & B are mixed



$$mS_A 12 + mS_B 19 = m(S_A + S_B)16 \Rightarrow 3S_B = 4S_A$$
 ...(i)

When B & C are mixed

$$mS_B 19 + mS_C 28 = m(S_B + S_C)23 \Rightarrow 4S_B = 5S_C$$
 ...(ii)  
when A & C are mixed

$$mS_{\Delta}12 + mS_{C}28 = m(S_{\Delta} + S_{C})\theta \Rightarrow \theta = 20.3$$
°C

14. Heat needed to bring ice to freezing point

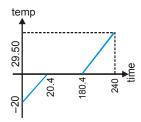
$$=10 \times 0.2 \times 20 + 200 \times 0.5 \times 20$$

$$=40+2000=2040$$
 cal

Time taken to reach 
$$0^{\circ}\text{C} = \frac{2040}{100} \text{ s} = 20.4 \text{ s}$$

Heat needed to melt ice

$$=2040 + 200 \times 80 = 18040$$
 cal



Time taken to melt ice = 
$$\frac{18040}{100}$$
 = 180.4 sec

Heat taken in 4 min =  $100 \times 4 \times 60 = 24,000$  cal

Let

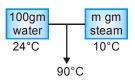
 $\theta$  = final temperature then

heat lost = heat gained

$$18040 + 10 \times 0.2 \times \theta + 200 \times 1 \times (\theta - 0) = 24,000$$

$$\Rightarrow \theta = \frac{24000 - 18040}{202} = 29.50^{\circ} \text{C}$$

15. Heat gained = Heat lost



$$100 \times 1 \times (90-24) = m \times 540 + m \times 1 \times (100-90) \implies m = 12 g$$

**16.** Heat lost = 
$$\frac{3}{4} \left( \frac{1}{2} \text{mv}^2 \right)$$

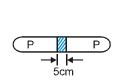
Heat gained = ms(327-27) + mL

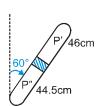
As heat lost = Heat gained

So 
$$\frac{3}{4}\left(\frac{1}{2}mv^2\right) = ms \times 300 + m \times L$$

$$\Rightarrow \frac{3}{8} v^2 = 0.03 \times 1000 \times 4.2 \times 300 + 6 \times 1000 \times 4.2$$

- $\Rightarrow$  v = 12.96 m/s
- 17. (i) At triple point (temperature = -56.6°C) & pressure = 5.11 atm), the solid, the liquid & the vapour phases of CO<sub>2</sub> co-exist.
  - (ii) Fusion point & boiling point both decrease on decreasing pressure.
  - (iii) Critical temperature is 31.1°C and critical pressure is 73.0 atm. On temperature higher than critical temperature it can't be liquified.
  - (iv) (A) Vapour (B) Solid (C) liquid
- 18.  $P'' = P' + 5 \cos 60^{\circ} = (P' + 2.5) \text{ cm of Hg}$





For constant temperature process:

$$P \times \left(\frac{46 + 44.5}{2}\right) = P' \times 46 = (P' + 2.5) (44.5)$$

$$\Rightarrow$$
 P' =  $\frac{44.5 \times 2.5}{1.5}$  & P = 75.4 cm of Hg

19. No. of moles (initially) = No. of moles (finally)

$$\frac{76 \times V_0}{273} + \frac{76 \times V_0}{273} = \frac{PV_0}{273} + \frac{PV_0}{335}$$

- $\Rightarrow$  P = 83.83 cm of Hg
- 20. No. of moles withdrawn =  $n_1 n_2 = \frac{\Delta m}{M}$

$$\Rightarrow \Delta m = M(n_1 - n_2) = M\left(\frac{P_1V_1}{RT_1} - \frac{P_2V_2}{RT_2}\right)$$

$$=32\left[\frac{15\times10^{5}\times30\times10^{-3}}{300\times8.314}-\frac{11\times10^{5}\times30\times10^{-3}}{290\times8.314}\right]$$
  
=0.139 kg

21. Let m = mass of neon gas then

$$n = \left(\frac{m}{20} + \frac{28 - m}{40}\right) \text{ from PV} = nRT$$

⇒ 
$$10^5 \times 0.2 = \left(\frac{m}{20} + \frac{28 - m}{40}\right) \times 8.314 \times 300$$
  
 $m_{\text{Ne}} = 4.074 \text{ g; } m_{\text{Argon}} = 23.926 \text{ g}$ 

22. 
$$\frac{R}{C_p} = 0.4 \Rightarrow C_p = \frac{R}{0.4} = \frac{5}{2}R \Rightarrow C_v = C_p - R = \frac{3}{2}R$$

(i) Atomicity = Monatomic, Degree of freedom = 3

(ii) 
$$C_v = \frac{3}{2}R \Rightarrow \gamma = \frac{C_P}{C_V} = \frac{5}{3}$$

(iii) Mean gram-molecular kinetic energy

$$=\frac{3}{2} R \times 300 = 450 R$$

- 23. (i) Dotted lines correspond to ideal gas
  - (ii)  $T_1 > T_2$ (On high temp. real gas behaves as ideal gas)

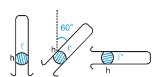
(iii) 
$$\frac{PV}{T} = \frac{m}{M}.R = \frac{10^{-3}}{32 \times 10^{-3}} \times 8.314 = 0.26 \text{ J/K}$$

24. For gas trapped in the tube

$$P_1V_1 = P_2V_2 = P_3V_3$$

$$P_1V_1 = P_2V_2 = P_3V_3$$
  
 $\Rightarrow (76-h) A\ell = (76-h\cos 60^\circ) A\ell = 76 \times A\ell$ 

⇒ 
$$66 \times 40 = 71 \times \ell' = 76 \times \ell''$$
  
 $\ell = 37.2 \text{ cm } \& \ell'' = 34.7 \text{ cm}$ 



- 25. (i) Let  $\dot{n}$  = number of collisions per second per unit area, change in momentum = 2mv
  - $\therefore$  Pressure exerted on wall =  $\stackrel{\bullet}{n}$  (2mv) =  $\stackrel{\bullet}{P_0}$

$$\Rightarrow \frac{\dot{n} \times 2 \times 32 \times 10^{-3}}{6.02 \times 10^{23}} \times \sqrt{\frac{3 \times 8.3 \times 300}{0.032}} = 10^{5}$$

- $\Rightarrow$   $\dot{n} = 1.95 \times 10^{27}$
- (ii) If vessel is suddenly stopped then KE will utilized in increase in temperature.

So 
$$\frac{1}{2}MV_0^2 = nC_v\Delta T$$

$$\Rightarrow$$
  $V_0 = \sqrt{\frac{2nC_v\Delta T}{M}} = \sqrt{\frac{2C_v\Delta T}{M_w}} = 36 \text{ ms}^{-1}$ 

**26.** 
$$V_A = V_0 = \frac{nRT_A}{P_A} = \frac{2R \times 300}{2} = 300R$$

$$V_{B} = \frac{nRT_{B}}{P_{B}} = \frac{2R \times 400}{2} = 400R = \frac{4}{3}V_{0}$$

$$V_C = \frac{nRT_C}{P_C} = \frac{2R \times 400}{1} = 800 R = \frac{8}{3} V_0$$

$$V_{D} = \frac{nRT_{D}}{P_{D}} = \frac{2R \times 300}{1} = 600 R = 2V_{0}$$

For cyclic process

$$\Delta U = 0$$
,  $Q = W$ 

$$W_{A\to B} = P_A (V_B - V_A) = 2 \left( \frac{4V_0}{3} - V_0 \right) \times 10^5 = \frac{2V_0}{3} \times 10^5$$

$$W_{B\to C} = P_B V_B \ell n 2 = 2 \times 10^5 \times \frac{4 V_0}{3} \ell n 2 = \frac{8 V_0}{3} \ell n 2 \times 10^5$$

$$W_{C\to D} = P_C(V_D - V_C)$$

$$=10^{5} \left(2V_{0} - \frac{8V_{0}}{3}\right) = -\frac{2V_{0}}{3} \times 10^{5}$$

$$W_{D\to A} = -P_D V_D$$
.  $\ell n2 = -10^5 \times 2 \times \ell n2$ 

∴ W = W<sub>A→B</sub> + W<sub>B→C</sub> + W<sub>C→D</sub> + W<sub>D→A</sub> = 1152 J  
(i) ∴ Q = 1152 J (ii) W = 1152 J (iii) 
$$\Delta U = 0$$

(i) : 
$$Q = 1152 J$$
 (ii)  $W = 1152 J$  (iii)  $\Delta U = 0$ 

27. (i) 
$$T_A = \frac{P_A V_A}{nR} = \frac{5 \times 10^4 \times 10}{\left(\frac{2000}{4}\right) \times 8.314} = 120.3$$
°K

$$T_B = \frac{P_B V_B}{nR} = 2T_A = 240.6^{\circ} \text{ K}$$

$$T_{\rm C} = \frac{P_{\rm c}V_{\rm C}}{nR} = 2T_{\rm B} = 481.3^{\circ} \,\rm K$$

$$T_{\rm D} = \frac{P_{\rm D}V_{\rm D}}{nR} = T_{\rm B} = 240.6$$
°K

- (ii) No. we can not predict the direction of reaction.
- (iii) Process ABC:

$$W = P\Delta V = 10 \times 10^4 \times (20 - 10) = 10^6 J$$

$$\Delta U = nC_V \Delta T = \left(\frac{2000}{4}\right) \left(\frac{3R}{2}\right) \times (T_C - T_A)$$

$$= 2.25 \times 10^6 \,\mathrm{J}$$
  $\therefore O = 3.25 \times 10^6 \,\mathrm{J}$ 

Process ADC →

$$W = 5 \times 10^4 \times (20 - 10) = 0.5 \times 10^6 J$$

$$\Delta U = nC_V (T_C - T_A) = 2.25 \times 10^6 J$$

$$Q = 2.75 \times 10^6 J$$

**28.** (i) 
$$P_1V_1 = nRT_1$$
 and  $P_2V_2 = nRT_2$ 

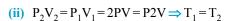
$$P_1V_2>P_1V_1$$

$$\Rightarrow$$
 nRT<sub>2</sub> > nRT<sub>1</sub>  $\Rightarrow$  T<sub>2</sub> > T<sub>1</sub>

For same volume,  $P_1V = nRT_1$ 

$$T_1 < T_2 & P_2 V = nRT_2$$

$$\Rightarrow$$
  $P_1 < P_2$ 



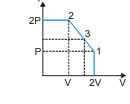
For state 3:

Let 
$$V_3 = 3V/2$$

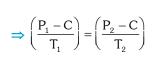
$$P_3 = 3P/2$$
 then

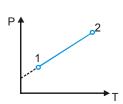
$$P_3V_3 = \frac{3P}{2}\frac{3V}{2} = \frac{9}{4}PV$$

$$T_3 > T_2 & T_3 > T_1$$



(iii) 
$$P = mT + C \Rightarrow \frac{P - C}{T} = m P = 0$$



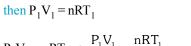


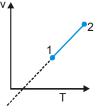
From ideal gas equation

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \implies \frac{P_1 V_1}{P_2 V_2} = \frac{T_1}{T_2} = \left(\frac{P_1 - C}{P_2 - C}\right)$$

$$\Rightarrow \frac{V_1}{V_2} = \frac{\left(1 - \frac{C}{P_1}\right)}{\left(1 - \frac{C}{P_2}\right)} < 1 \Rightarrow V_1 < V_2$$

(iv) 
$$V = mT - C$$
;  $\frac{V_1 + C}{T_1} = \frac{V_2 + C}{T_2}$ 





$$P_2V_2 = nRT_2 \Longrightarrow \frac{P_1V_1}{P_2V_2} = \frac{nRT_1}{nRT_2}$$

$$\implies \frac{P_1}{P_2} = \frac{T_1}{T_2} \times \frac{V_2}{V_1} = \left(\frac{V_1 + C}{V_1}\right) \left(\frac{V_2}{V_2 + C}\right)$$

$$\frac{P_1}{P_2} = \left(1 + \frac{C}{V_1}\right) \frac{1}{\left(1 + \frac{C}{V_2}\right)} > 1 :: P_1 > P_2$$

### PHYSICS FOR JEE MAINS & ADVANCED

29. (i) Work done by gas

$$= \frac{1}{2} (4+8) \times 10^{5} \times (0.5-0.2) \stackrel{\circ}{\times} \stackrel{\circ}{\times} \stackrel{\circ}{\times} \stackrel{\circ}{\times} =$$

$$= 1.8 \times 10^{5} \text{ J} \qquad \stackrel{\circ}{\times} \stackrel{\circ}{\times} \stackrel{\circ}{\times} \stackrel{\circ}{\times} =$$

(ii) Increase in internal energy

$$\Delta U = nC_V \Delta T = \frac{nR(T_2 - T_1)}{\gamma - 1} = \frac{P_2V_2 - P_1V_1}{\gamma - 1}$$

$$=\frac{(8\times0.5-4\times0.2)\times10^5}{\frac{5}{3}-1}=4.8\times10^5\,\mathrm{J}$$

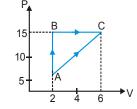
(iii) Amount of heat supplied  $Q = \Delta U + W = 6.6 \times 10^5 \text{ J}$ 

(iv) Molar specific heat of the gas

$$= \frac{Q}{n\Delta T} = \frac{6.6 \times 10^5 \times R}{(P_2 V_2 - P_1 V_1)} = 17.1 \text{ J/mole-K}$$

30. (i)  $W_{AC} < W_{ABC}$  (Area under PV-graph gives work)

(ii)  $U_A = 10J$ 



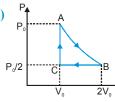
$$\Delta W_{AC} = \frac{1}{2} \times (6-2) \times (15+5)$$

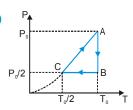
$$=\frac{4\times20}{2}=40\,\mathrm{J}$$

$$\Rightarrow$$
 Q =  $\Delta$ U+W  $\Rightarrow$  200 = (U<sub>C</sub>-10)+40

$$\rightarrow$$
 U<sub>C</sub> = 200 + 10 - 40 = 210 - 40 = 170 J

(iii) 
$$Q_{AB} = \Delta U_{AB} + W_{AB} = (U_B - U_A) + W_{A \to B}$$
  
=  $(20-10) + 0 = 10 J$ 





(iii) Work done by gas 
$$W_{AB} = nR(T_A) \ell n \frac{V_B}{V_A}$$

$$=3RT_A\ell n2$$

$$W_{BC} = \frac{P_0}{2} (V_0 - 2V_0)$$

$$=-\frac{P_{_{0}}V_{_{0}}}{2}=\frac{-nRT_{_{A}}}{2}=-\frac{3}{2}RT_{_{A}} \implies W_{_{CA}}=0$$

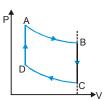
$$W_{ABCA} = RT_A (3 \times 0.693 - 1.5) = 0.58 RT_A$$

$$\Delta Q_{ABCA} = W_{ABCA} = 0.58 RT_A$$

32. Given that

$$T_A = 1000 \,\text{K} \, \text{n=1}$$

$$P_{\rm B} = \left(\frac{2}{3}\right) P_{\rm A}, \gamma = 5/3$$



$$P_C = \left(\frac{1}{3}\right) P_A, \left(\frac{2}{3}\right)^{2/5} = 0.85$$

For process  $A \rightarrow B$ 

$$P_{\scriptscriptstyle A}^{1-\gamma}\,T_{\scriptscriptstyle A}^{\gamma}\,=P_{\scriptscriptstyle R}^{1-\gamma}\,T_{\scriptscriptstyle R}^{\gamma}$$

$$T_B = T_A \left(\frac{P_A}{P_D}\right)^{\frac{1-\gamma}{\gamma}} = 1000 \times \left(\frac{3}{2}\right)^{-2/5}$$

$$= 1000 \times 0.85 = 850 \,\mathrm{k}$$

For Process  $B \rightarrow C$ 

$$\frac{P_B}{T_B} = \frac{P_C}{T_C} \Longrightarrow T_C = T_B \left(\frac{P_C}{P_B}\right) = 850 \times \frac{1}{2} = 425 \text{ K}$$

(i) 
$$W_{A \rightarrow B} = \frac{nR(T_A - T_B)}{\gamma - 1}$$

$$= \frac{1 \times 8.314 \times (1000 - 850)}{\left(\frac{5}{3} - 1\right)} = 1870.2 \,\mathrm{J}$$

(ii) 
$$\Delta Q_{B\rightarrow C} = \Delta U_{B\rightarrow C} + \Delta W_{B\rightarrow C} = nC_V \Delta T + 0$$

= n. 
$$\frac{3}{2}$$
 R(T<sub>C</sub>-T<sub>B</sub>) = 1 ×  $\frac{3}{2}$  × 8.314 (425 – 850)

$$=-5300.175 \,\mathrm{J}$$

(iii) For process  $A \rightarrow B$ 

$$P_A V_A^{\gamma} = P_B V_B^{\gamma} \Longrightarrow \left(\frac{V_B}{V_A}\right)^{\gamma} = \frac{P_A}{P_B} = \frac{3}{2}$$

For Process  $C \rightarrow D$ 

$$P_C V_C^{\gamma} = P_D V_D^{\gamma}$$

$$\Rightarrow \left(\frac{V_{\text{C}}}{V_{\text{D}}}\right)^{\gamma} = \left(\frac{V_{\text{B}}}{V_{\text{A}}}\right)^{\gamma} = \frac{3}{2} = \frac{P_{\text{D}}}{P_{\text{C}}} \Rightarrow P_{\text{D}} = \frac{3}{2}P_{\text{C}}$$

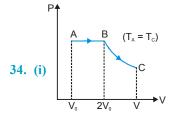
At end points A and D

$$\Rightarrow \frac{P_A}{T_A} = \frac{P_D}{T_D} \Rightarrow \frac{3P_C}{1000} = \frac{\left(\frac{3P_C}{2}\right)}{T_D} \Rightarrow T_D = 500 \text{ K}$$

- 33. (i) For adiabatic process  $T_1V_1^{\gamma-1} = T_2.V_2^{\gamma-1}$   $\Rightarrow 300 \text{ V}^{5/3-1} = T_2.(2\text{V})^{5/3-1} \Rightarrow T_2 = 189 \text{ K}$ 
  - (ii) Change in internal energy

$$\Delta U = nC_V \Delta T = n \frac{3}{2} R(T_2 - T_1)$$
$$= 2 \times \frac{3}{2} \times 8.314 \times (189 - 300) = -2767 J$$

(iii) Work done by gas =  $\frac{P_1V_1 - P_2V_2}{\gamma - 1} = \frac{nR(T_1 - T_2)}{\gamma - 1}$ = 2767 J



(ii) Process AB

$$\frac{V_A}{T_A} = \frac{V_B}{T_B} \implies T_B = \frac{V_B}{V_A} T_A = 2T_A = 600 \text{ K}$$

Process BC

$$T_{B}V_{B}^{\gamma-1} = T_{C}V_{C}^{\gamma-1}$$

$$\Rightarrow$$
 V<sub>C</sub> =  $80\sqrt{2}$  Litre = 113 L

For end states A & C  $\frac{P_A.V_A}{T_A} = \frac{P_CV_C}{T_C} = nR$ 

$$\Rightarrow$$
 P<sub>C</sub> = 0.44 × 10<sup>5</sup> N/m<sup>2</sup>

(iii) Work done

$$W_{AB} = P_A (2V_0 - V_0) = nRT_A = 600 R; W_{BC}$$
$$= \frac{nR(T_B - T_C)}{\gamma - 1} = \frac{3}{2} nR(600 - 300) = 900R$$

**35.** For polytropic process  $T_1V_1^{n-1} = T_2V_2^{n-1}$ 

$$\Rightarrow$$
 TV<sup>n-1</sup>= $\frac{T}{2}(5.66V)^{n-1}$  $\Rightarrow$  2 = 5.66<sup>n-1</sup>

Taking log both sides  $\ell n2 = (n-1) \ell n 5.66$ 

$$\Rightarrow$$
 n = 1.4 = 1 +  $\frac{2}{f}$   $\Rightarrow$  f = 5

- (i)  $\therefore$  Degrees of freedom = 5
- (ii) Work done by gas

$$= -\frac{P_1V_1 - P_2V_2}{\gamma - 1} = \frac{PV - P_2(5.66V)}{1.4 - 1} = 12.3PV$$

Where 
$$P_2V_2^{\gamma} = P_1V_1^{\gamma} \implies P_2 = P\left(\frac{1}{5.66}\right)^{1.4}$$

36. 
$$PV^{\gamma} = \text{constant} \Rightarrow (10^5) (6)^{5/3} = (P_2) (2)^{5/3}$$
  

$$\Rightarrow P_2 = (10^5)(3)^{5/3} \text{ Nm}^{-2}$$

$$W = \frac{P_1 V_1 - P_2 V_2}{\gamma - 1}$$

$$= (10^5)(6 \times 10^{-3}) - (10^5 \times 3^{5/3})(2 \times 10^{-3}) - ... 972 \text{ I}$$

$$= \frac{\left(10^{5}\right)\left(6\times10^{-3}\right) - \left(10^{5}\times3^{5/3}\right)\left(2\times10^{-3}\right)}{\frac{5}{3}-1} = -972J$$

37. Number of moles  $n = \frac{PV}{RT} = \frac{(1.6 \times 10^6)(0.0083)}{(8.3)(300)} = \frac{16}{3}$ 

Heat is supplied at cosntant volume

So  $Q = nC_V \Delta T$ 

$$\Rightarrow T_2 = T_1 + \frac{Q}{nC_V} = 300 + \frac{2.49 \times 10^4}{\left(\frac{16}{3}\right) \left(\frac{3R}{2}\right)}$$

$$=300+375=675 \text{ K}$$

As V = constant So 
$$\frac{P_2}{P_1} = \frac{T_2}{T_1}$$

$$\Rightarrow$$
 P<sub>2</sub>= $\left(\frac{675}{300}\right)(1.6 \times 10^6) = 3.6 \times 10^6 \text{ Nm}^{-2}$ 

**38.** (i) For a cyclic process

$$Q_1 + Q_2 + Q_3 + Q_4 = W_1 + W_2 + W_3 + W_4$$

$$\Rightarrow W_4 = Q_1 + Q_2 + Q_3 + Q_4 - W_1 - W_2 - W_3$$

$$= 5960 - 5585 - 2980 + 3645 - 2200 + 825 + 1100 = 765 \text{ J}$$

(ii) 
$$\eta = \frac{W_{net}}{Q_{given}} = \frac{W_1 + W_2 + W_3 + W_4}{Q_1 + Q_4}$$

$$= \frac{2200 - 825 - 1100 + 765}{5960 + 3645} = 0.1082$$

39. 
$$\gamma_{\text{mix}} = \frac{n_{\text{A}} C_{\text{P}_{\text{A}}} + n_{\text{B}} C_{\text{P}_{\text{B}}}}{n_{\text{A}} C_{\text{V}_{\text{A}}} + n_{\text{B}} C_{\text{V}_{\text{B}}}}$$

$$\Rightarrow \frac{19}{13} = \frac{\left(1\right)\left(\frac{5}{2}R\right) + n_{B}\left(\frac{7}{2}R\right)}{\left(1\right)\left(\frac{3}{2}R\right) + n_{B}\left(\frac{5}{2}R\right)} \Rightarrow n_{B} = 2 \text{ mole}$$

**40.** The maximum temperature of the gas will be during process BC.

Process BC can be represented by straight line,

$$y = mx + C$$

So 
$$P = mV + C$$

Putting point B & C gives

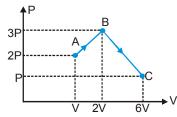
$$3P = 2mV + C$$

...(i)

$$\Rightarrow$$
 P = 6 mV + C

...(ii)

So subtracting 2P = -4mV So  $m = -\frac{P}{2V}$ 



From (ii) 
$$P = -\frac{P}{2V} .6V + C \implies C = 4P$$

Hence we get equation as

$$y = \left(-\frac{P}{2V}\right)x + 4P \qquad ...(iii)$$

where y is pressure and x is volume of gas. Putting y from above. Now we have

$$x y = nRT \Rightarrow \left(-\frac{P}{V}x^2 + 4Px\right) = nRT$$
 ....(iv)

For maximum temperature  $\frac{dT}{dx} = 0$ 

$$\Rightarrow \left(-\frac{2P}{2V}x + 4Px\right) = 0$$

Hence x = 4V Putting in (iii)

We get  $nRT_{max} = 2P(4V) = 8PV$ 

So 
$$T_{\text{max}} = \frac{8PV}{nR} \implies x = 8$$

41.  $PT = constant \Rightarrow P^2V = constant \Rightarrow PV^{1/2} = constant$ 

For this process  $C = C_V + \frac{R}{1 - 1/2} = C_V + 2R$ 

$$\Rightarrow$$
 C<sub>V</sub> = 37.35 -2 (8.314) = 20.722 =  $\frac{5}{2}$ R

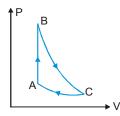
$$\Rightarrow \frac{f}{2} R = \frac{5}{2} R \Rightarrow f = 5$$

42. Slope

$$=-\frac{\gamma P}{V} = -\tan 37^{\circ} \Rightarrow \frac{mP}{V} = \tan 37^{\circ}$$

$$\Rightarrow m = \left(\frac{V}{P}\right) \left(\frac{3}{4}\right) = \left(\frac{4 \times 10^5}{2 \times 10^5}\right) \left(\frac{3}{4}\right) = \frac{3}{2} = 1.5$$

**43.** PV = nRT 
$$\Rightarrow$$
 n =  $\frac{PV}{RT} = \frac{(10^3)(10^{-3})}{(25/3)(3)} = \frac{1}{25}$ 



For process AB

$$W = 0$$
,  $Q = \Delta U = nC_V \Delta T$ 

$$= \left(\frac{1}{25}\right) \left(\frac{3}{2}R\right) (300 - 3) = \frac{297}{2} = 148.5 J$$

For process BC

Q=0, W = 
$$\frac{nR}{\gamma - 1} (T_1 - T_2) = \frac{\left(\frac{1}{25}\right)\left(\frac{25}{3}\right)}{\left(\frac{5}{3} - 1\right)} [300 - 3]$$

= 148.5 J and 
$$\Delta U = -W = -148.5 J$$

For process  $CA \Rightarrow \Delta U = 0$ 

W = nRT 
$$\ln \left( \frac{V_A}{V_C} \right) = -6.9 \text{ J}$$
 and Q = W = -6.9 J

Thermal efficiency = 
$$\frac{W_{net}}{Q_{supplied}} = \frac{148.5 - 6.9}{148.5} = 0.954$$

44. 
$$P_1A + Mg = P_2A$$
  
Extra force needed
$$= P_2'A - P_1'A - Mg$$

$$= P_2'A - P_1'A - P_2A + P_1A$$

$$= (\Delta P_2)A - (\Delta P_1)A$$

$$= \left[ \frac{nR\Delta T}{V} - \frac{nR\Delta T}{2V} \right] A = \frac{5000}{3} N$$

45. 
$$\Delta U = nC_V \Delta T$$
,  $Q = nC_P \Delta T$  and

W = nR
$$\Delta$$
T = (1)  $\left(\frac{25}{3}\right)$  (100) =  $\frac{2500}{3}$  J

$$\Delta U = n(C_{p} - R)\Delta T = nC_{p}\Delta T - nR\Delta T$$

$$=1000-(1)\left(\frac{25}{3}\right)(100)=\frac{500}{3}$$
 J

46. New length of gas column =  $\frac{h}{2} + \frac{h}{16} = \frac{9}{16}h$ New volume of gas

$$= \left(\frac{9}{16}h\right) A = \frac{9}{16}V_0 \Rightarrow P = P_0 + kx$$

As 
$$PV^{\gamma} = \text{constant so } P_0 V_0^{1.5} = P \left( \frac{9}{16} V_0 \right)^{1.5}$$

$$\Rightarrow P = \frac{64}{27} P_0 = P_0 + kx \Rightarrow kx = \frac{37}{27} P_0$$

But 
$$kx = (3700) \left(\frac{h}{16}\right)$$
 so  $(3700) \left(\frac{h}{16}\right) = \left(\frac{37}{27}\right) (10^5)$ 

Now 
$$T_1 V_1^{\gamma - 1} = T_2 V_2^{\gamma - 1}$$

$$\Rightarrow$$
 (273)  $(V_0)^{0.5} = (T_2) \left(\frac{9}{16}V_0\right)^{0.5}$ 

⇒ 
$$T_2 = \frac{4}{3} \times 273 = 364 \text{ K}$$

**48.** Final volume of chamber =  $V_0 + Ax = 3.2 \times 10^{-3} \text{ m}^3$ 

Final pressure in chamber =  $P_0 + \frac{kx}{\Delta} = 2 \times 10^5 \text{N/m}^2$ 

From ideal gas equation  $\frac{P_1 V_1}{T_2} = \frac{P_2 V_2}{T_2}$ 

$$T_2 = (P_2 V_2) \left( \frac{T_1}{P_1 V_1} \right) = 800 \text{ K}$$

Work done by gas =  $\int_{0.1}^{0.1} \left( P_0 + \frac{Kx}{\Delta} \right) A dx = 120 J$ 

Change in internal energy  $\Delta U = nC_v \Delta T$ 

$$\Rightarrow$$
  $\Delta U = \left(\frac{P_1 V_1}{RT_1}\right) \left(\frac{3}{2}R\right) \Delta T = 600 J$ 

:. Heat Supplied = 120 + 600 = 720 J

**49.** (i) For the right chamber

$$P_0^{\ 1-\gamma}T_0^{\ \gamma}\!=\!\left(\frac{243P_0}{32}\right)^{\!1-\gamma}.T_2^{\gamma}$$



$$\Rightarrow T_2 = \frac{9}{4} T_0 \text{ and } \frac{P_0 \cdot V_0}{T_0} = \frac{\left(\frac{243 P_0}{32}\right) \cdot V_2}{\left(\frac{9}{4} T_0\right)}$$

$$\Rightarrow$$
  $V_2 = \frac{9}{4} \times \frac{32}{243} V_0 = \frac{8}{27} V_0$ 

For the left chamber

$$\frac{P_0 V_0}{T_0} = \frac{P_1 \cdot V_1}{T_1}$$
 where  $P_1 = \frac{243}{32} P_0$ 

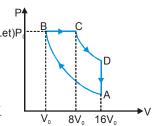
$$V_1 = 2V_0 - \frac{8}{27}V_0 = \frac{46}{27}V_0$$

$$\Rightarrow T_1 = \frac{T_0}{P_0 V_0} \times \left(\frac{243}{32} P_0\right) \left(\frac{46}{27} V_0\right) = \frac{9 \times 23}{16} T_0$$
$$= 12.94 T_0$$

(ii) Work done by the gas in the right chamber:

$$\frac{P_1 V_1 - P_2 V_2}{\gamma - 1} = \frac{nR(T_1 - T_2)}{\gamma - 1} = \frac{1 \times R\left(T_0 - \frac{9}{4}T_0\right)}{\left(\frac{5}{3} - 1\right)}$$
$$= -\frac{3}{2} \times R \times \frac{5}{4}T_0 = -1.875 RT_0$$

50. Let  $V_B = V_0$ Process  $A \rightarrow B$   $T_A V_A^{\gamma - 1} = T_B V^{\gamma - 1}$   $\Rightarrow T_B = 909 \text{ K}$ Process  $B \rightarrow C$ 



 $\frac{V_B}{T_R} = \frac{V_C}{T_C} \Rightarrow T_C = 7272K$ 

Process 
$$C \rightarrow D$$
:  
 $T_C V_C^{\gamma - 1} = T_D V_D^{\gamma - 1} \Rightarrow T_D = 5511.15 \text{ K}$ 

Process 
$$A \rightarrow B$$
  $Q_{AB} = 0$ 

Process B 
$$\rightarrow$$
 C  $Q_{BC} = nC_p\Delta T$ 

$$=1 \times \frac{7}{2} R (T_C - T_B) = 185156.937 J$$

Process  $C \rightarrow D$   $Q_{CD} = 0$ 

Process D  $\rightarrow$  A  $Q_{DA} = nCv\Delta T$ 

$$=1\left(\frac{5}{2}R\right)(T_A-T_D) = -108313.753 J$$

: Efficiency

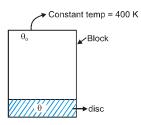
$$\eta = \frac{work \ output}{Heat \ input} = \frac{Q_{in} - Q_{out}}{Q_{in}}$$

$$= \left(1 - \frac{108313.753}{185156.937}\right) \times 100\%$$

$$\eta = 41.50\%$$

**Note**: please read  $V_C/V_D = \frac{1}{2}$  instead of  $V_C/V_D = 2$  in the question.

51.



 $\theta$  = temperature of disc

 $\theta_0$  = constant temperature

Heat input to disc  $\frac{KA(\theta_0 - \theta)}{L}$ 

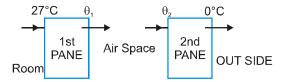
Heat utilised by disc = ms  $\frac{d\theta}{dt}$ 

(where s = specific heat of disc)

$$\Rightarrow \ ms\frac{d\theta}{dt} = \frac{KA(\theta_0 - \theta)}{L} \ \Rightarrow \ \int\limits_{300}^{350} \frac{d\theta}{\theta_0 - \theta} = \frac{KA}{msL} \int\limits_0^t dt$$

$$\Rightarrow t = \frac{\text{msL}}{\text{KA}} \ln \left( \frac{\theta_0 - 300}{\theta_0 - 350} \right) \Rightarrow t = 166.32 \text{ sec}$$

**52.** Heat flow for three sections will be same.



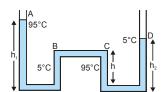
$$\frac{27 - \theta_1}{\left(\frac{L}{KA}\right)_{1 \text{st Pane}}} = \frac{\theta_1 - \theta_2}{\left(\frac{L}{KA}\right)_{A.S.}} = \frac{\theta_2 - 0}{\left(\frac{L}{KA}\right)_{2 \text{nd Pane}}}$$

$$\Rightarrow$$
 Q<sub>1</sub> = 26.48°C; Q<sub>2</sub> = 0.52°C

Heat flow rate

$$\frac{d\theta}{dt} = \frac{27 - \theta_1}{\left(\frac{L}{KA}\right)_{1st Pane}} = \frac{27 - 26.48}{\left(\frac{0.01}{0.8 \times 1}\right)} = 41.6 \text{ watt}$$

53.



Pressure at the bottom of A – B limb:

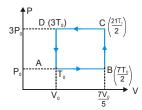
$$P_0 + \rho_{95}gh_1 = P_B + \rho_5gh$$
 ...(

Pressure at the bottom of C–D limb:

$$P_B + \rho_{95} gh = P_0 + \rho_5 \times g \times h_2 (P_B = P_C)$$
 ...(ii)

Solving we get, 
$$\gamma = 2 \times 10^{-4} \, ^{\circ}\text{C}^{-1}$$
 ::  $\alpha = \frac{2}{3} \times 10^{-4} \, ^{\circ}\text{C}^{-1}$ 

54. For each state



$$n = \frac{P_0 V_0}{T_0} = \frac{P_0.(7 V_0 \ / \ 2)}{T_B} = \frac{3 P_0 (7 V_0 \ / \ 2)}{T_C} = \frac{3 P_0 V_0}{T_D}$$

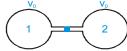
$$\Rightarrow$$
 T<sub>B</sub> =  $\frac{7}{2}$  T<sub>0</sub>; T<sub>C</sub> =  $\frac{21}{2}$  T<sub>0</sub>  $\Rightarrow$  T<sub>D</sub> = 3T<sub>0</sub>.

 $\therefore$  Heat absorbed =  $(nC_p. \Delta T)_{A \to B} + (nC_v\Delta T)_{B \to C}$ 

= 
$$n4R\left(\frac{5}{2}T_0\right) + n3R(7T_0) = 31.nRT_0 = 31P_0V_0$$

Work done =  $(3P_0 - P_0)(V_0 - \frac{7}{2}V_0) = -5P_0V_0$ 

55.  $n_1 = \text{no. of moles in vessel-1}$  $n_2 = \text{no. of moles in vessel-2}$ 



 $P_1^2$  = initial pressure in both vessels

 $P_2$  = final pressure in both vessels.

Initially

volume of vessel-1 = volume of vessel-2

$$\frac{n_1RT_0}{P_2} = \frac{n_2RT_0}{P_2} \implies n_1 = n_2$$

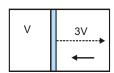
Finally, 
$$V_1 = \frac{n_1 R T_1}{P_2}$$
 &  $V_2 = \frac{n_2 . R T_2}{P_2} = \left(\frac{n_1 R}{P_2}\right) T_2$ 

$$\frac{V_1}{V_2} = \frac{T_1}{T_2} = \frac{275}{271} \& V_1 + V_2 = V_0 + \lambda A$$

Displacement of mercury droplets

$$\Delta L = \frac{V_1 - V_2}{A} = \frac{4}{546} \left( \frac{V_0 + \lambda A}{A} \right) = 0.26 \text{m}$$

56. In free expansion, temperature remains constant



Initial temperature  $T_0 = \frac{P_0 V_0}{nR}$ 

After compression  $T_0(4V)^{\gamma-1} = T(V)^{\gamma-1} \Rightarrow T = 2T_0$ 

Change in internal energy  $\Delta U = nC_V \cdot \Delta T = n\left(\frac{R}{\gamma - 1}\right)$ 

$$\Delta T = \frac{nR(2T_0 - T_0)}{\gamma - 1}$$

$$= \frac{nRT_0}{\gamma - 1} = \frac{P_0V_0}{\gamma - 1} = \frac{(2 \times 10^5) \times (10^{-3})}{(1.5 - 1)} = 400 \text{ J}$$

57. Work done by gas

$$=\int\limits_0^x P_0 A dx + \int\limits_0^x kx. dx$$

$$\Rightarrow$$
 50 J=P<sub>0</sub>Ax +  $\frac{kx^2}{2}$ 

$$\Rightarrow$$
 50 = 10<sup>5</sup> × 4 × 10<sup>-3</sup> × 0.1 +  $\frac{k}{2}$  (0.01)

Spring constant  $\Rightarrow$  k = 2000 N/m

Heat supplied

$$Q = \Delta U + W = nC_V \Delta T + W$$

$$= \frac{nR\Delta T}{\gamma - 1} + W = \frac{2 \times 8.314 \times 50}{\left(\frac{5}{3} - 1\right)} + 50 = 1295 \text{ J}$$

58. Let  $h_i$  = empty space over Hg-column For constant temperature process

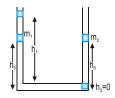
$$P_1V_1 = P_2V_2 \Rightarrow 4 \times h_1 = 5h_2$$
  
where  $h_1 - h_2 = 1 \Rightarrow h_2 = 4 \& h_1 = 5$ 

True Reading	Faulty Reading
73 75 74	69 70 ×

- (i) Total length of tube =69+5=74 cm or 70+4=74 cm
- (i)i When faulty barometer reads 69.5 cm.  $P_1V_1 = P_2V_2$ ;  $4h_1 = 4.5 h$ ; h = 4.44 $\therefore$  True reading = 69.5 + 4.44 = 73.94
- (iii) When the barometer reads 74 cm  $P_1V_1 = P_2V_2 \implies 4 \times 5 = (74 - x)^2 \implies x = 69.528 \text{ cm}$
- 59. For equilibrium

$$\frac{m_1 g}{A_1} + \rho g h_0 = \frac{m_2 g}{A_2} + \rho g h_0$$

$$m_1 = 2kg, m_2 = 1kg$$



$$\Rightarrow \frac{2}{A_1} = \frac{1}{A_2}$$

For final equilibrium  $\frac{m_1g}{A_2} > \frac{m_2g}{A_1}$ 

.. m<sub>1</sub> block will fall down

For constant temperature forces and pressure being  $constant V_{initial} = V_{final}$ 

$$h_0A_1 + h_0A_2 = h_1A_1 + h_2A_2 \implies h_1 = 30 \text{ cm } \& h_2 = 0$$

**60.** 
$$\theta_1 = 372$$
°C;  $\theta_2 = -15$ °C;  $\theta_3 = 157$ °C  $\gamma_{CO_2} = \frac{7}{5}$ 

$H_2$	He	CO <sub>2</sub>				
$\leftarrow \ell \rightarrow \leftarrow \ell \rightarrow \leftarrow \ell \rightarrow$						

For the H<sub>2</sub> gas

$$\frac{P_1 V_1}{RT_1} = \frac{P_2 V_2}{RT_2} \implies \frac{P_0 A \ell}{645 R} = \frac{P \times A \ell_1}{TR} \qquad ...(i)$$

For the He gas 
$$\frac{P_0 A \ell}{258R} = \frac{P \times A \ell_2}{TR}$$
 ...(ii)

For the 
$$CO_2$$
gas  $\frac{P_0A\ell}{430R} = \frac{P \times A\ell_3}{TR}$  ...(iii)

$$\Rightarrow \frac{\ell_1}{\ell_2} = \frac{258}{645} = \frac{1}{2.5} \& \frac{\ell_1}{\ell_2} = \frac{430}{645} = \frac{1}{1.5}$$

$$\Rightarrow \ell_1 + \ell_2 + \ell_3 = 3\ell \Rightarrow \ell_1(1 + 2.5 + 1.5) = 3\ell$$

$$\Rightarrow \ell_1 = 0.6 \ \ell \text{ and } \ell_2 = 2.5 \ \ell_1 = 1.5 \ell$$

$$\ell_3 = 1.5 \times 0.6\ell = 0.9\ell$$

For the entire system  $\Delta U_1 + \Delta U_2 + \Delta U_3 = 0$ 

$$\Rightarrow \frac{n_1 R(T - T_1)}{\gamma_1 - 1} + \frac{n_1 R(T - T_2)}{(\gamma_2 - 1)} + \frac{n_3 R(T - T_3)}{(\gamma_3 - 1)} = 0$$

$$\Rightarrow \frac{P \times 0.6\ell - P_0\ell}{\left(\frac{7}{5} - 1\right)} + \frac{(P \times 1.5\ell - P_0\ell)}{\left(\frac{5}{3} - 1\right)} + \frac{(P \times 0.9\ell - P_0\ell)}{\left(\frac{7}{5} - 1\right)} = 0$$

$$\Rightarrow P = \frac{13}{12}P_0$$

**61.** For the process

$$U = a\sqrt{V} \Rightarrow nC_vT = n\frac{5}{2}RT = a\sqrt{V}$$

$$\Rightarrow$$
 nRT = PV =  $\frac{2}{5}$  a $\sqrt{V}$   $\Rightarrow$  P =  $\frac{2}{5}\frac{a}{\sqrt{V}}$ 

$$\Rightarrow$$
 W =  $\int PdV = \frac{4}{5}a(\sqrt{V})_{V_i}^{V_f}$ 

$$\therefore \Delta U = a \left( \sqrt{V} \right)_{V_i}^{V_f} = 100$$

$$\therefore$$
 W =  $\frac{4}{5}\Delta U = 80 J$ 

(i) W = 80J $Q = \Delta U + W = 100 J + 80J = 180 J$ 

(ii) 
$$C = \frac{\Delta Q}{n\Delta T} = \frac{\Delta U + W}{n\Delta T} = \frac{\Delta U + \frac{4}{5}\Delta U}{n\Delta T}$$
  
=  $\frac{9}{5} \left(\frac{\Delta U}{n\Delta T}\right) = \frac{9}{5} \times \frac{5}{2} R = \frac{9}{2} R$ 

**62.** For compartment C

$$P_0 V_0^{\gamma} = P \left( \frac{4 V_0}{9} \right)^{\gamma} \implies P = \frac{27}{8} P_0 \implies P_0 \cdot T_0^{\gamma/1 - \gamma} = P \cdot T^{\gamma/1 - \gamma}$$

$$P_0 T_0^{-3} = \left(\frac{27}{8}P_0\right) \times T^{-3} \Rightarrow T = \frac{3}{2}T_0$$

For compartment A

$$P_{A} = \frac{27}{8} P_{0} \Rightarrow \frac{P_{0} V_{0}}{RT_{0}} = \frac{P_{1} V_{1}}{RT_{1}}$$

$$\Rightarrow T_1 = \frac{\frac{27}{8} P_0 \left( 2V_0 - \frac{4V_0}{9} \right)}{R} \times \frac{RT_0}{P_0 V_0} = T_1 = \frac{21}{4} T_0$$

For compartment B

$$\frac{P_{0}V_{0}}{T_{0}} = \frac{P_{1}V_{1}}{T_{1}} \implies \frac{P_{0}V_{0}}{T_{0}} = \frac{P_{1}V_{0}}{\left(\frac{21}{4}T_{0}\right)} \implies P_{1} = \frac{21}{4}P_{0}$$

- (i) Final pressure in A  $\frac{27}{8}$  P<sub>0</sub>
  - Final pressure in B  $\frac{21}{4}$  P<sub>0</sub>
  - Final pressure in C  $\frac{3}{2}$  P<sub>0</sub>
- (ii) Final temperature in A =  $\frac{21}{4}$  T<sub>0</sub>

Final temperature in B =  $\frac{21}{4}$ T<sub>0</sub>

Final temperature in  $C = \frac{3}{2}T_0$ 

(iii) Heat supplied by heater =  $(\Delta U + W)$  all chambers

$$Q = (\Delta U_1 + W_1) + (\Delta U_2 + W_2) + 0$$

$$= (\Delta U_1 - W_3) + (\Delta U_2 + 0)$$

$$= \Delta U_1 + \Delta U_2 - W_3$$

$$= \frac{n_1 R \Delta T}{\gamma_1 - 1} + \frac{n_2 R \Delta T}{\gamma_2 - 1} - \left(\frac{n_3 R \Delta T}{\gamma_3 - 1}\right)$$

$$= \frac{17}{2} P_0 V_0 + \frac{17}{2} P_0 V_0 + P_0 V_0 = 18 P_0 V_0$$

(iv) Work done by gas in chamber B = 0 Work done by gas in chamber C

$$= -\Delta U = \frac{-nR\Delta T}{\gamma - 1} = -P_0 V_0$$

Work done by gas in chamber A

$$= (-) W_{chamber} = -(P_0 V_0) = P_0 V_0$$

(v) Heat flowing across piston –I

#### **EXERCISE - 5**

## Part # I : AIEEE/JEE-MAIN

- The temperature of gas molecules depends on the average kinetic energy associated with the disorderly motion (i.e., random motion) of the gas molecules. The orderly kinetic energy of the molecules of the gas container will increase in the lorry, whereas disorderly kinetic energy will still remain the same; hence the temperature of the gas molecules will remain unchanged.
- $v_{\rm rms} = \sqrt{\frac{3RT}{M}}$

Where T is the temperature of the gas molecules in kelvin and M is the molecular mass of the gas

$$v_{H_2} = v_{O_2} \Rightarrow \sqrt{\frac{T_{H_2}}{M_{H_2}}} = \sqrt{\frac{T_{O_2}}{M_{O_2}}} \Rightarrow \frac{T_{H_2}}{2} = \frac{320}{32}$$

$$\Rightarrow T_{H_2} = 20K$$

3. 
$$\frac{n_1 + n_2}{\gamma - 1} = \frac{n_1}{\gamma_1 - 1} + \frac{n_2}{\gamma_2 - 1}$$

$$\Rightarrow \frac{1+1}{\gamma-1} = \frac{1}{(5/3)-1} + \frac{1}{(7/5-1)}$$

$$\Rightarrow \frac{2}{\gamma - 1} = \frac{3}{2} + \frac{5}{2} = 4 \Rightarrow \gamma = \frac{3}{2} = \frac{24}{16}$$

- 4. Given  $P \propto T^3$ 
  - $\therefore$  PV =  $\mu$ RT
  - $\therefore P \propto (PV)^3 \implies P^3V^3 \propto P \implies P^2V^3 = \text{constant}$

$$\Rightarrow$$
 PV<sup>3/2</sup> = constant  $\Rightarrow \gamma = \frac{C_P}{C_V} = \frac{3}{2}$ 

5. Monoatomic  $n_1 = 1$   $\gamma_1 = \frac{5}{3}$ 

Diatomic 
$$n_2 = 1$$
  $\gamma_2 = \frac{7}{5}$ 

$$\frac{n_1 + n_2}{\gamma_{mix} - 1} = \frac{n_1}{\gamma_1 - 1} + \frac{n_2}{\gamma_2 - 1} \implies \gamma_{mix} = \frac{3}{2}$$

6. 
$$\frac{n_1 + n_2}{\gamma_{mix} - 1} = \frac{n_1}{\gamma_1 - 1} + \frac{n_2}{\gamma_2 - 1}$$

Number of moles in 16 g He = 4

Number of moles in 16 g  $O_2 = 0.5$ 

$$\gamma_{\text{He}} = \frac{5}{3} \qquad \qquad \gamma_{\text{O}_2} = \frac{7}{5}$$

On replacing  $n_{He}n_{O_2}$ ;  $\gamma_{He}$ ,  $\gamma_{O_2}$ ,  $\gamma_{mix} = 1.62$ 

7. We have, molar heat capacity = molar mass × specific heat capacity per unit mass

$$\therefore C_p = 28 C_p \text{ (for nitrogen) and } C_V = 28 C_V$$
Now  $C_p - C_V = R \text{ or } 28C_p - 28 C_v = R$ 

$$\Rightarrow$$
  $C_p - C_v = \frac{R}{28}$ 

8. 
$$U = U_1 + U_2 \Rightarrow (n_1 + n_2) C_v T = n_1 C_v T_1 + n_2 C_v T_2$$

$$\Rightarrow T = \frac{(P_1V_1 + P_2V_2)T_1T_2}{(P_1V_1T_2 + P_2V_2T_2)}$$

9. 
$$v = \sqrt{\frac{\gamma RT}{M}} \Rightarrow \frac{v_1}{v_2} = \sqrt{\frac{\gamma_1 M_2}{\gamma_2 M_1}} = \sqrt{\frac{\frac{7}{5} \times 4}{\frac{5}{3} \times 32}}$$

$$\Rightarrow \frac{460}{v_2} = \sqrt{\frac{21}{25 \times 8}} \Rightarrow v_2 = 460\sqrt{\frac{200}{21}} \text{ m/s}$$

10. Energy of the diatomic gas

$$\frac{5}{2}nRT = \frac{5}{2}PV = \frac{5}{2} \times 8 \times 10^{4} \times \frac{1}{4} = 5 \times 10^{4} J$$

- 11.  $Q = ms\Delta\theta = 0.1 \times 4184 \times 20 = 8.4 \text{ kJ}$
- 12.  $\left(n_1 C_{v_1} T_1 + n_2 C_{v_2} T_2 + n_3 C_{v_3} T_3\right)$ =  $\left(n_1 + n_2 + n_3\right) C_{V_{only}} T$

$$\text{As } C_{V_1} = C_{V_2} \text{ so } T = \frac{n_1 T_1 + n_2 T_2 + n_3 T_3}{n_1 + n_2 + n_3}$$

13. Specific heat at low temperature is

$$C_{p} = 32 \left(\frac{T}{400}\right)^{3} \implies Q = \int \text{m.c.dT}$$
$$= \int_{20}^{4} \frac{100}{1000} \times 32 \left(\frac{T}{400}\right)^{3} dT$$

$$= \frac{32}{10} \times \frac{1}{(400)^3} \left(\frac{T^4}{4}\right)$$

$$= \frac{32}{10 \times (400)^3} \times \frac{1}{4} (20^4 - 4^4)$$

$$= \frac{32}{10 \times (400)^3} \times \frac{1}{4} \times (160000 - 256)$$

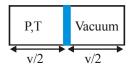
$$= 0.002 \text{ kJ}$$

$$\beta = \frac{T_2}{T_1 - T_2} = \frac{Q_2}{W} \implies \frac{20}{300 - 20} = \frac{0.02}{W}$$

$$\Rightarrow$$
 W = 0.028 kJ

$$\Rightarrow \frac{4}{300-4} = \frac{0.002}{W} \Rightarrow W = 0.0148 \text{ kJ}$$

**14.** This is free expansion of the gas in which temperature will remain constant i.e. on the other side temperature will T.



Number of moles 
$$n_1 = \frac{PV/2}{KT}$$

Finally number of moles  $n_2 = \frac{P'V}{KT}$ 

$$n_1 = n_2$$

$$\frac{PV}{2} = \frac{P^1V}{KT} \implies P' = \frac{P}{2}$$

- 15. All reversible engines work for different values of temperature of source and sink hence the efficiencies of all such engines are different. The incorrect statement is all reversible cycles have same efficiency.
- **16.** When water is cooled to form ice, the energy is released as heat so mass of water decreases.

17. 
$$\eta = 1 - \frac{T_2}{T_1} = 1 \implies \frac{T_2}{T_1} = 0 \implies T_2 = 0 \text{ or } T = \infty$$

Which is not possible

- 18. Heat can't flow from the body at lower temperature to body at higher temperature is a consequences of second law of thermodynamics.
- **19.** The instantaneous thermodynamic state of matter is denoted by pressure, volume and temperature.

**20.** 
$$T_{\text{source}} = 627^{\circ}\text{C} = 627 + 273 = 900\text{K}$$

$$T_{cink} = 27^{\circ}C = 27 + 273 = 300K$$

Efficiency (दक्षता)

$$(\eta) = 1 - \frac{T_{\text{sink}}}{T_{\text{source}}} = 1 - \frac{300}{900} = 1 - \frac{1}{3}$$

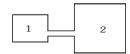
$$(\eta) = \frac{2}{3} = \frac{\text{Output}}{\text{Input}} = \frac{\text{Work}}{\text{Heat Input}}$$

$$\Rightarrow \frac{2}{3} \times \text{Heat Input} = \text{Work}$$

$$\Rightarrow \frac{2}{3} \times 3 \times 10^6 \times 4.2 = \text{Work}$$

$$\Rightarrow$$
 Work =  $8.4 \times 10^6$  J

- **21.** Internal energy and entropy are state functions and not path functions.
- **22.** Assume  $T_1 > T_2$

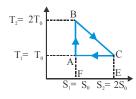


Heat given = Heat taken

$$\mu_1 C_{v_1} (T_1 - T) = \mu_2 C_{v_2} (T - T_2)$$

Here 
$$C_{v_1} = C_{v_2} \& \mu_1 = \frac{P_1 V_1}{T_1}, \mu_2 = \frac{P_2 V_2}{T_2}$$

- 23. The first law of thermodynamics does not introduce the concept of entropy.
- 24. Heat supplied Q = Area FBCEF



= 
$$T (S_2 - S_1) + \frac{1}{2} (T_2 - T_1) (S_2 - S_1)$$

Work done W = Area ABC

$$=\frac{1}{2}(T_2-T_1)(S_2-S_1)$$

$$\eta = \frac{W}{Q} = \frac{\frac{1}{2}(T_2 - T_1)(S_2 - S_1)}{T_1(S_2 - S_1) + \frac{1}{2}(T_2 - T_1)(S_2 - S_1)}$$
$$= \frac{T_2 - T_1}{T_2 + T_1} = \frac{2T_0 - T_0}{2T_0 + T_0} = \frac{1}{3}$$

**25.** The internal energy of a system is a state function, i.e., change in internal energy only depends on the initial and the final position and not on the path chosen.

Hence 
$$\Delta U_1 = \Delta U_2$$

**26.** : 
$$n_1 C_{v_1} T_1 + n_2 C_{v_2} T_2 = (n_1 C_{v_1} + n_2 C_{v_2}) T_f$$

$$T_{f} = \frac{n_{1}C_{v_{1}}T_{1} + n_{2}C_{v_{2}}T_{2}}{n_{1}C_{v_{1}} + n_{2}C_{v_{2}}}$$

$$= \frac{1 \times \frac{5}{2}RT_0 + 1 \times \frac{3}{2}R\left(\frac{7}{3}T_0\right)}{1 \times \frac{5}{2}R + 1 \times \frac{3}{2}R} = \frac{6RT_0}{4R} = \frac{3}{2}T_0$$

27. Work done in adiabatic process

$$W = \frac{\mu R (T_1 - T_2)}{\gamma - 1} \implies \gamma = 1 + \frac{R (T_2 - T_1)}{W}$$

$$=1+\frac{10^3\times 8.3(7)}{146\times 10^3}=1+0.40=1.40$$

- .. The gas must be diatomic
- 28. Let  $\eta$  is the efficiency of heat engine and  $\beta$  is the corresponding coefficient of performance of a refrigerator working between the same temperature.

The relation between  $\eta$  and  $\beta$  is

$$\beta = \frac{1}{\eta} - 1 = 10 - 1 = 9$$
 Also  $\beta = \frac{\text{Output}}{\text{Input}}$ 

Energy absorbed from the reservoir at lower temperature

Work done on the system

$$\beta = 9 = \frac{\text{Energy absorbed}}{10 \text{ J}}$$

So, energy absorbed = 90 J

**29.** As a thermodynamic system is taken from state *i* to state *f*; then the internal energy of the system remains the same irrespective of the path followed

$$(Q-W)_{iaf} = (Q-W)_{ibf} \Rightarrow 50-20 = 36-W$$
  
 $\Rightarrow W = 6 \text{ cal}$ 

30.  $W_{AB}$  = Work done in isobaric process =  $\mu R\Delta T = 2R \times (500 - 300) = 400R$ 

Work done on the gas = -400R

31.  $W_{DA}$  = Work done in isothermal process

= 2.303 
$$\mu$$
RT  $\log \frac{P_1}{P_2}$   
= 2.303 × 2R × 300  $\log \frac{1 \times 10^5}{2 \times 10^5}$ 

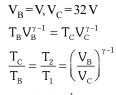
$$=2.303 \times 2R \times 300 \times (-0.3010) = -414R$$

Word done on the gas = -(-414 R) = 414 R

32.  $W_{ABCDA} = W_{AB} + W_{BC} + W_{CD} + W_{DA}$ =  $\mu R(500-300) + 2.303 \mu R(500) \log \frac{2}{2} + \mu R(300-500) + 2.303$  $\mu R(300) \log \frac{1}{2} = 276R$ 

Work done on the gas = -276 R

33.  $T_B = T_1, T_C = T_2, \gamma = 1.4$ 



$$=\left(\frac{1}{32}\right)^{\gamma-1}=\frac{1}{4}$$

$$\eta = 1 - \frac{T_2}{T_1} = 1 - \frac{1}{4} = \frac{3}{4} = 0.75$$

34. 
$$\frac{1}{2}Mv^2 = \frac{f}{2}R\Delta T$$
 and

$$\gamma = 1 + \frac{2}{f} \implies \Delta T = \frac{(\gamma - 1)}{2R} M v^2$$

**35.** 
$$1 - \frac{T_2}{T_1} = \frac{1}{6} \Rightarrow \frac{T_2}{T_1} = \frac{5}{6}$$
 ... (1)

and 
$$1 - \frac{T_2 - 62}{T_1} = \frac{1}{3} \implies \frac{T_2 - 62}{T_1} = \frac{2}{3}$$
 ... (2)

By solving equation (1) and (2)

 $T_1 = 372 \text{ K} \text{ and } T_2 = 310 \text{ K}$ 

**36.** 
$$\Delta V = V_0(3\alpha)\Delta\theta$$

$$= \frac{4}{3} (3.14)(10)^3 [3 \times 23 \times 10^{-6}] [100-0]$$
  
= 28.9 cc

37. Strain = 
$$\frac{\ell_2 - \ell_1}{\ell_1}$$
 =  $\alpha t$  and  $Y = \frac{Stress}{Strain}$ 

$$\Rightarrow$$
 Stress = Y \alpha t

**38.** W = Area bounded by curve =  $P_0V_0$ 

$$Q_{AB} = nC_V \Delta T = n \times \frac{3}{2} R \times \Delta T = \frac{3}{2} P_0 V_0$$

$$Q_{BC} = nC_P \Delta T = n \times \frac{5}{2} R \times \Delta T = 5 P_0 V_0$$

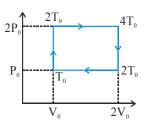
Total heat supplied

$$= \frac{3}{2} P_0 V_0 + 5 P_0 V_0 = \frac{13}{2} P_0 V_0$$

$$\eta = \frac{W}{Q} \times 100 = \frac{P_0 V_0}{13P_0 V_0} \times 100 = 15.4\%$$

**40.** 
$$\eta = \left(1 - \frac{T_2}{T_1}\right) \times 100 \Rightarrow \frac{40}{100} = 1 - \frac{T_2}{500} \Rightarrow T_2 = 300 \text{ K}$$

Again 
$$\frac{60}{100} = 1 - \frac{300}{T_1} \implies T_1 = 750 \text{ K}$$



heat supplied =  $nC_v(2T_0 - T_0) + nC_p(4T_0 - 2T_0)$ 

$$=\frac{n.3RT_{_{0}}}{2}+\frac{D5R}{2}(2T_{_{0}})=\frac{13}{2}nRT_{_{0}}=\frac{13}{2}P_{_{0}}V_{_{0}}$$

- **41**. Amount of heat required by a body of any mass of undergo a unity change in temperature is known as heat capacity or thermal capacity of the substance.
- 42. Black board paint is more close to a black body.
- **43.** Infrared radiations are detected by pyrometer.
- **44**. The power radiated by a sphere of radius R at temperature T is

$$P = \varepsilon \sigma T^4 (4\pi R^2)$$

Where

 $\varepsilon$  = emissivity of the material of sphere.

 $\sigma$  = Stefan's constant

T = Absolute temperature

R = Radius of the sphere

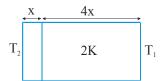
$$\Rightarrow \frac{P_1}{P_2} = \frac{T_1^4 R_1^2}{T_1^4 R_2^2} = \left(\frac{4000}{2000}\right)^4 \left(\frac{1}{4}\right)^2 = \left(2^4\right) \times \frac{1}{4^2} = \frac{16}{16} = 1$$

**45**. According to Stefan's law, power radiated by a perfectly black body is

$$P = \sigma A T^4$$
;  $P = \sigma 4 \pi R^2 T^4$ 

$$\frac{P_2}{P_1} = \left(\frac{R_2}{R_1}\right)^2 \left(\frac{T_2}{T_1}\right)^4 \implies P_2 = 64P_1$$





$$R_1$$
=Resistance of left part =  $\frac{x}{KA}$ 

$$R_2$$
=Resistance of right part =  $\frac{4x}{2KA} = \frac{2x}{KA}$ 

Total Resistance 
$$R_1 + R_2 = \frac{x}{KA} + \frac{2x}{KA} = \frac{3x}{KA}$$

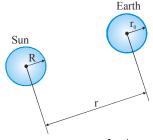
Thermal current = 
$$\frac{T_2 - T_1}{R} = \frac{K(T_2 - T_1)A}{3x}$$

Comparing with the given result  $f = \frac{1}{3}$ 

47. Rate of flow of heat

$$= KA \left(\frac{\Delta T}{\Delta x}\right) = K \left(4\pi r_1 r_2\right) \left(\frac{T_1 - T_2}{r_2 - r_1}\right)$$

48. According to Stefan's law



Power radiated by Sun =  $\sigma(4\pi R^2)T^4$ Intensity of the sun received by the earth

$$= \frac{\text{Power of the sun}}{4\pi r^2}$$

$$I = \frac{\sigma 4\pi R^{2} T^{4}}{4\pi r^{2}} = \frac{\sigma R^{2} T^{4}}{r^{2}}$$

Radiant power incident on the earth =  $I(\pi r_0^2)$ 

where  $\left(\pi r_0^2\right)$  is the projection of the earth's area receiving

the energy from the sun. 
$$P = \frac{\sigma R^2 T^4}{r^2} \left( \pi r_0^2 \right)$$

49. Let the temperature of the interface be  $T_0$ .

$T_1$	$l_1$	$T_{o}$	$l_2$	$T_2$
	K <sub>1</sub>		$K_2$	

Thermal current (I) = 
$$\frac{Temperature \ difference}{Thermal \ resitance}$$

Thermal resistance = 
$$\frac{1}{K} \frac{\ell}{A}$$

$$\Rightarrow \frac{T_1 - T_0}{\ell_1 / K_1 A} = \frac{T_0 - T_2}{\ell_2 / K_2 A}$$

$$\Rightarrow T_0 = \frac{K_1 \ell_2 T_1 + K_2 \ell_1 T_2}{K_1 \ell_2 + K_2 \ell_1}$$

50. In steady state, temperature decreases linearly along the

bar. i.e. 
$$\frac{dQ}{dt} = -KA\left(\frac{d\theta}{dx}\right)$$

51. Rate of cooling  $= -\frac{d\theta}{dt} = k(\theta - \theta_0)$ 

$$\frac{d\theta}{\theta - \theta_0} = -kdt \implies \int \frac{d\theta}{\theta - \theta_0} = -\int kdt$$

$$\Rightarrow ln(\theta - \theta_0) = -k t + C \Rightarrow$$
 correct answer is (2)

52. 
$$Y = \frac{\text{stress}}{\text{strain}} \Rightarrow \text{stress} = Y \times \text{strain}$$

$$\frac{F}{S} = Y(\alpha \Delta T) \implies F = YS\alpha \Delta T$$

Therefore force by one part on other part  $= 2F = 2SY\alpha\Delta T$ 

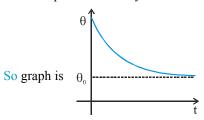
53. By Newton's Law of cooling  $T = T_S + (T_H - T_S)e^{-kt}$ 

 $T_S \rightarrow$  Temperature of surrounding

 $T_H \rightarrow$  Temperature of body at t = 0

 $K \rightarrow constant$ 

 $T \rightarrow$  Temperature of body at time t



54. (i) 
$$\Delta s_1 = \int \frac{dQ}{T} = ms \int_{100}^{150} \frac{dT}{T} + ms \int_{150}^{200} \frac{dT}{T}$$
  

$$= \ln\left(\frac{150}{100}\right) + \ln\left(\frac{200}{150}\right) = \ln\left(\frac{3}{2}\right) + \ln\frac{4}{3}$$

$$\Delta s_1 = \ln 2$$

(ii) 
$$\Delta s_2 = \int \frac{dQ}{T} = \int_{100}^{112.5} \frac{dQ}{T} + \int_{112.5}^{125} \frac{dQ}{T} + \dots$$
  

$$= \ln\left(\frac{112.5}{100}\right) + \ln\left(\frac{125}{112.5}\right) + \dots$$

$$= \ln\left(\frac{9}{8}\right) + \ln\left(\frac{10}{9}\right) + \ln\left(\frac{16}{15}\right) = \ln\left(\frac{16}{8}\right) = \ln 2$$

55. 
$$u = \frac{U}{V} \propto T^4 \Rightarrow P = \frac{1}{3} \left(\frac{U}{V}\right)$$

Adiabatic expansion

$$TV^{\gamma-1} = K \implies TV^{\frac{\gamma}{4}} = C$$

$$\gamma - 1 = \frac{\gamma}{4} \implies \frac{3\gamma}{4} = 1 \implies \gamma = \frac{4}{3}$$

$$TV^{\frac{\gamma}{4}} = C \implies TV^{\frac{1}{3}} = C \implies T\left(\frac{4}{3}\pi R^3\right)^{\frac{1}{3}} = C$$

$$T \propto \frac{1}{R}$$

56. mean free path

$$\begin{split} \lambda &= \frac{1}{\sqrt{2}\pi d^2 n} \\ n &= \frac{\text{no. of molecules}}{\text{volume}} \\ v_{\text{avg.}} &\propto \sqrt{T} & \text{T.V}^{\gamma-1=C} \\ t &= \frac{\lambda}{v_{\text{avg.}}} \propto \frac{V}{\sqrt{T}} \quad v \to \text{is volume} \\ &\frac{V}{\sqrt{\frac{C}{v^{r-1}}}} \propto V^{\frac{\gamma+1}{2}} \implies v^q \propto v^{\frac{\gamma+1}{2}} \implies q = \frac{\gamma+1}{2} \end{split}$$

57. T<sub>max.</sub> at mid point

$$T = \frac{pv}{nR} = \frac{\left(\frac{3}{2}P_0\right)\left(\frac{3V_0}{2}\right)}{nR} = \frac{9}{4}\left(\frac{P_0V_0}{nR}\right)$$

58. 
$$\frac{\Delta T}{T} \propto \Delta \theta$$
  
 $\frac{12}{4} = \frac{40 - \theta}{\theta - 20}$   
 $3\theta - 60 = 40 - \theta$   
 $4\theta = 100$   
 $\theta = 25^{\circ} C$   
 $\Delta T = \frac{1}{2} \alpha \Delta \theta \times T \; ; \quad 4 = \frac{1}{2} \alpha 5 \times 86400$   
 $\frac{8 \times 10^{5}}{5 \times 86400} = \alpha \; ; \quad \frac{8000}{4320} = \alpha$   
 $\alpha = 1.85 \times 10^{-5}/^{\circ}C$ 

59. 
$$Pv^{n} = k$$

$$C = C_{v} + \frac{R}{1 - n} \quad ; \quad C - C_{v} = \frac{R}{1 - n}$$

$$1 - n = \frac{R}{C - C_{v}} \quad ; \quad n = 1 - \frac{R}{C - C_{v}}$$

$$n = \frac{C - C_{v} - R}{C - C_{v}} \quad ; \quad n = \frac{C - C_{v} - (C_{p} - C_{v})}{C - C_{v}}$$

$$n = \frac{C - C_{v} - C_{p} + C_{v}}{C - C_{v}} \quad ; \quad n = \frac{C - C_{p}}{C - C_{v}}$$

### Part # II : IIT-JEE ADVANCED

- 1. Average rotational KE =  $2 \times \frac{1}{2}$  kT (for diatomic gas)
- 2. Initial conditions  $P_1V = n_1RT$ ,  $P_2V = n_2RT$ Final condition  $(P_1-\Delta P)2V = n_1RT$

$$(P_2-1.5\Delta P) 2V = n_2RT \implies \frac{n_1RT}{2V} = \Delta P$$

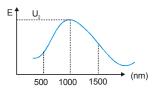
$$\frac{n_2RT}{2V} = 1.5\Delta P \implies \frac{n_1}{n_2} = \frac{1}{1.5} = \frac{2}{3} \implies \frac{m_A}{m_B} = \frac{2}{3}$$

3. For A: 
$$Q = nC_p\Delta T = (nC_p)(30)$$
  
For B:  $Q = nC_v\Delta T = nC_v\Delta T = nC_p(30)$   

$$\Rightarrow \Delta T = (30) \left(\frac{C_p}{C_v}\right) = 30 \times \frac{7}{5} = 42 \text{ K}$$

4. At 2880 K:

$$\lambda_{_{m}} = \frac{b}{T} = \frac{2.88 \times 10^{6} \, \text{nm} - \text{K}}{2880 \, \text{K}} = 1000 \, \text{nm}$$



Therefore  $U_2 > U_1 \& U_2 > U_3$ 

5. 
$$v_{\text{sound}} = \sqrt{\frac{\gamma RT}{M_w}}$$

$$\mathbf{6.} \quad C_{V_{mix}} = \frac{n_1 C_{V_1} + n_2 C_{V_2}}{n_1 + n_2} = \frac{(2) \bigg(\frac{5}{2} \, R\bigg) + 4 \bigg(\frac{3}{2} \, R\bigg)}{2 + 4} = \frac{11 R}{6}$$

$$U = (n_1 + n_2) C_{V \text{ mix}} T = (6) \left(\frac{11R}{6}\right) T = 11RT$$

7. 
$$T_1 V_1^{\gamma - 1} = T_2 V_2^{\gamma - 1}$$
 but  $V = AL$ 

So 
$$\frac{T_1}{T_2} = \left(\frac{V_2}{V_1}\right)^{5/3-1} = \left(\frac{L_2}{L_1}\right)^{2/3}$$

$$\label{eq:def_sol} \pmb{8}. \quad \ \lambda_1 T_1 = \lambda_2 T_2 = \lambda_3 T_3 = b \ \ \text{so} \ \ T_1 > T_3 > T_2$$

9. The temperature of ice will first increase from  $-10^{\circ}$ C to  $0^{\circ}$ C. Heat supplied in this process will be:  $Q_1 = mS_i(10)$  m=mass of ice

 $S_i$  = specific heat of ice

Then, ice starts melting

Temperature during melting will remain constant (0°C)

Heat supplied in the process will be  $Q_2 = mL$ 

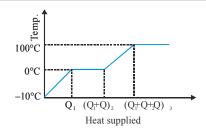
L = latent heat of melting

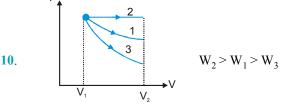
Now the temperature of water will increase from 0°C to 100°C.

Heat supplied will be  $Q_3 = mS_w(100)$ 

where  $S_w = Specific heat of water$ 

Finally water at 100°C will be converted into steam at 100°C and during this process temperature again remains constant. Temperature versus heat supplied graph will be as follows

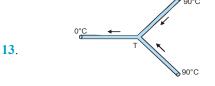




11. As P = constant

So 
$$P\Delta V = nR\Delta T \implies \delta = \frac{\Delta V}{V\Delta T} = \frac{nR}{PV} = \frac{1}{T}$$

12. 
$$v_{\text{sound}} = \sqrt{\frac{\gamma RT}{M_w}}$$
 So  $\frac{v_1}{v_2} = \sqrt{\frac{m_2}{m_1}}$ 



$$\frac{kA(90-T)}{\ell} + \frac{kA(90-T)}{\ell} = \frac{kA(T-0)}{\ell}$$

$$\Rightarrow 90-T+90-T = T \Rightarrow 3T = 180 \Rightarrow T = 60^{\circ}C$$

- 14. If dW = 0, dQ < 0 then dU < 0 ⇒ The temperature will decrease
- 15. As  $\gamma_{\text{mono}} > \gamma_{\text{dia}}$  so  $2 \rightarrow$  monoatomic &  $1 \rightarrow$  diatomic
- **16**. For complete cycle

$$\Delta U = 0$$
 so  $W = Q = 5$ 

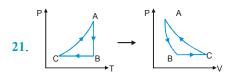
$$\Rightarrow$$
 W<sub>AB</sub> + W<sub>BC</sub> + W<sub>CA</sub> = 5 But W<sub>BC</sub> = 0 &  
W<sub>AB</sub> = 10 (2-1) = 10  $\Rightarrow$  W<sub>CA</sub> = 5 - 10 = -5J

17. At constant temperature PV = constant

So PdV + VdP = 
$$0 \Rightarrow \frac{dV}{dP} = -\frac{V}{P}$$

$$\Rightarrow \beta = -\frac{dV/dP}{V} = \frac{1}{P}$$

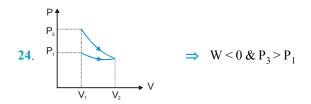
- 18. Black body radiates maximum number of wavelength and maximum energy if all other conditions (e.g., temperature surface area etc.) are same. So, when the temperature of black body becomes equal to the temperature of the furnace, the black body will ,radiate maximum energy and it will be brighted of all. Initially it will absorb all the radiant energy incident on it, so it is the darkest one.
- 19. For same temperature difference less time is taken for x, this means  $e_x > e_y$ . According to Kirchoff's law
- **20.**  $\Delta \ell_1 = \Delta \ell_2 \implies \ell_1 \alpha_2 \Delta T = \ell_2 \alpha_5 \Delta T$ 
  - $\Rightarrow \frac{\ell_1}{\ell_2} = \frac{\alpha_s}{\alpha_s} \Rightarrow \frac{\ell_1}{\ell_1 + \ell_2} = \frac{\alpha_s}{\alpha_s + \alpha_s}$



- 2kg ice (-20 C) ↓ 20 kcal
- 5kg water (20 C)
- 2kg ice (0 C)

2 kg water (0 C)

- ↓ 100 kcal
- **22**. ↓ 160 kcal
- 5kg water (0 C)
- ⇒ Final temperature 0°C
  - Amount of ice melted =  $\frac{100-20}{80}$  = 1 kg
- Final mass of water = 5 + 1 = 6 kg
- 23. Temperature of liquid oxygen will first increase in the same phase. Then, phase change (liquid to gas) will take place. During which temperature will remain constant. After that temperature of oxygen in gaseous state will further increase.



25. 
$$q_1 L = \frac{k(2A)(T_1 - T_2)}{\ell}$$
  $\Rightarrow$   $q_2 L = \frac{kA(T_1 - T_2)}{2\ell}$   $\Rightarrow \frac{q_2}{q_1} = \frac{1}{4}$ 

26. Power radiated

$$Q = e\sigma AT^4$$
 and  $\lambda_m T = b$ 

So (300) 
$$T_1 = (400) T_2 = (500) T_3$$

$$\Rightarrow 3T_1 = 4T_2 = 5T_3$$

and 
$$A_1: A_2: A_3 = 4: 16: 36 = 1: 4: 9$$

$$Q_A: Q_B: Q_C = \frac{1}{81}: \frac{4}{256}: \frac{9}{625} \Rightarrow Q_B \text{ is maximum.}$$

27. Net heat absorbed by water

$$= 1000 - 160 = 840 \,\mathrm{J/s}$$

$$\frac{Q}{t} = \frac{ms\Delta T}{t}$$



$$840 = \frac{2 \times 4200 \times (77 - 27)}{t}$$

$$\Rightarrow$$
 t = 500 s = 8 min 20 s

- 28. Heat transfer in warming of glass of bulb due to filament is through radiation.
- 29. The temperature of sun is a higher than that of welding arc which in turn greater than tungsten filament.
- 30. 1 calorie is the heat required to raise the temp. of 1g of water from 14.5 to 15.5°C at 760 mm of Hg.

32. 
$$\gamma_{V} = \frac{\Delta V}{V \Delta T}$$

$$PT^2 = constant & PV = nRT$$

$$\Rightarrow$$
 V  $\propto$  T<sup>3</sup>  $\Rightarrow$   $\frac{\Delta V}{V} = 3$   $\frac{\Delta T}{T}$   $\Rightarrow$   $\frac{\Delta V}{V \wedge T} = \frac{3}{T} = \gamma_V$ 

33. 
$$P = \frac{\rho}{M}RT \implies \frac{P_1}{P_2} = \frac{\rho_1 M_2}{\rho_2 M_1} = \frac{4}{3} \implies \frac{\rho_1}{\rho_2} = \frac{4}{3} \times \frac{2}{3} = \frac{8}{9}$$

**34.** For two rectangular blocks

$$R_1 = \frac{\ell}{kA} = 2R \; ; \; R_2 = \frac{\ell}{2kA} = R$$

In configuration 1

Equivalent thermal resistance = 3R

In configuration 2

Equivalent thermal resistance =  $\frac{2}{2}$ R

Rate of heat flow

$$\Delta Q_1 = \frac{\Delta T}{3R} t_1$$
 and  $\Delta Q_2 = \frac{\Delta T}{\frac{2R}{3}} t_2$ 

$$\Rightarrow \frac{\Delta T}{3R} t_1 = \frac{3\Delta T}{2R} t_2 \Rightarrow t_2 = \frac{2}{9} t_1 = 2 \text{sec.}$$

35. Process FG is isothermal

so work done = nRT ln 
$$\left(\frac{P_i}{P_f}\right)$$

$$= 32 P_0 V_0 \ln \left( \frac{32 P_0}{P_0} \right) = 160 P_0 V_0 \ln 2.$$

Process GE is isobaric

So work done

$$= P|\Delta V| = P_0|(V_G - V_E)| = P_0|(32V_0 - V_0)| = 31 P_0V_0$$

Process FH is adiabatic

so 
$$(32P_0)V_0^{5/3} = (P_0)V_H^{5/3} \implies V_H = 8V_0$$

Since process FH is adiabatic so

$$\left| \frac{\left| \left( P_{H} V_{H} - P_{F} V_{F} \right) \right|}{(8-1)} \right| = \frac{\left| \left( P_{0} 8 V_{0} \right) - 32 P_{0} V_{0} \right|}{\left( \frac{5}{3} - 1 \right)} = 36 P_{0} V_{0}$$

Process G $\rightarrow$ H is isobaric so work done =  $P_0|(32V_0 - 8V_0)|= 24 P_0V_0$ 

**36.** A **37.** B

### MCO's

1. 
$$v_p = \sqrt{\frac{2kT}{m}}$$
;  $\overline{v} = \sqrt{\frac{8kT}{\pi m}}$ ,  $v_{rms} = \sqrt{\frac{3kT}{m}} \Longrightarrow v_p < \overline{v} < v_{rms}$ 

Average KE of a molecule  $=\frac{3}{2} kT = \frac{3}{4} mv_P^2$ 

2. There is a decrease in volume during melting of an ice slab. Therefore negative work is done by the ice—water system on to the surrounding ⇒ W = -ve Heat is absorbed during melting

$$\Rightarrow$$
 Q = +ve  $\Rightarrow$   $\Delta U = Q - W = +ve$ 

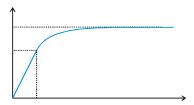
- 3. Radius of curvature  $R = \frac{d}{(\alpha_1 \alpha_2)\Delta T}$
- 4.  $C_p C_v = R$  Always constant

$$\frac{C_p}{C_v} = \gamma$$
 decreases with atomicity

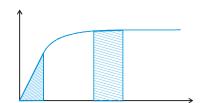
 $(C_p + C_v)$  and  $C_p.C_v$  depends on degree of freedom therefore it will be more for diatomic gas

- 5. (i) For isothermal process curve should be hyperbola.
  - (ii) Work done & change in internal energy are both negative.
  - (iii) For higher pressure volume is increasing and lower pressure volume is decreasing.

6. (A) From 0 to 100 k the major part of graph lies in linear region and very small part in non-linear region, therefore to a reasonable approximation between 0 K - 100 K, graph of C vs T is linear.



(B) by comparing area under curve



- (C) from 400 K to 500 K, Graph of C vs T become asymptotic hence rate of heat absorption become constant
- (D) The rate of heat absorption increases as C is increasing.
- **7.** B,D

8. 
$$E_{\text{mix.}} = \frac{1 \times \frac{3RT}{2} + 1 \times \frac{5RT}{2}}{1 + 1} = 2RT$$

$$C_{\text{Pmix}} = 3R$$

$$\gamma_{\text{mix}} = \frac{3}{2}$$

$$M_{\text{mix}} = \frac{1 \times 4 + 1 \times 2}{1 + 1} = 3 \implies V_s = \sqrt{\frac{\gamma RT}{M_w}}$$

$$\frac{V_{\text{mix}}}{V_{\text{He}}} = \sqrt{\frac{\gamma_{\text{mix}}}{\gamma_{\text{He}}}} \frac{M_{\text{He}}}{M_{\text{mv}}} = \sqrt{\frac{3}{2} \times \frac{3}{5} \times \frac{4}{3}} = \sqrt{\frac{6}{5}}$$

$$V_{rms} \propto \frac{1}{\sqrt{M_{_{Y}}}} \Rightarrow \frac{V_{_{He}}}{V_{_{H_{_{1}}}}} = \sqrt{\frac{M_{_{H_{_{2}}}}}{M_{_{H}}}} = \sqrt{\frac{2}{4}} = \frac{1}{\sqrt{2}}$$

Change in internal energy

$$P_1V_1 = nRT_1$$

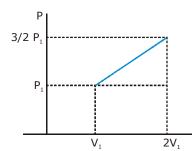
$$\Delta U = nC_V dT = n \left(\frac{3}{2}R\right) (3T_1 - T_1)$$

$$=\frac{3}{2}$$
 nR  $(T_1)$  = 3nRT<sub>1</sub> So option B

$$\Delta U = 3P_1V_1$$

$$\frac{P_1 V_1}{P_2 V_2} = \frac{nRT_1}{nRT_2}$$

$$\frac{P_1 V_1}{P_2 (2V_1)} = \frac{nRT_1}{nR (3T_1)}$$



$$P_2 = \frac{3}{2} P_1$$

$$\mathbf{w} = \frac{1}{2} \times 2\mathbf{V}_{_{\! 1}} \times \frac{P_{_{\! 1}}}{2} + P_{_{\! 1}} \left( 2\mathbf{V}_{_{\! 1}} \right)$$

$$=\frac{P_1V_1}{2} + 2V_1P_1 = \frac{5}{2}P_1V_1 \implies V_1 = A$$

$$dV = V_2 - V_1 = Ax = V_1$$

$$x = \frac{V_1}{A}$$

$$F = kx = (P_2 - P_1)A \implies kx = (\frac{3}{2}P_1 - P_1)A$$

### 10. C 11. A

#### **Match the Column**

- 1. Process J  $\rightarrow$  K (isochoric): W = 0,  $\Delta$ U < 0  $\Rightarrow$  Q < 0 Process K  $\rightarrow$  L (isobaric): W > 0,  $\Delta$ U > 0  $\Rightarrow$  Q > 0 Process L  $\rightarrow$  M (isochoric): W = 0,  $\Delta$ U > 0  $\Rightarrow$  Q > 0 Process M  $\rightarrow$  J, W < 0,  $\Delta$ U < 0  $\Rightarrow$  Q < 0
- (A) Bimetallic strip: Works on the thermal expansion of solids (different solids expands by different length for the same rise of temperature). The energy is converted to kinetic energy.

## (B) Steam engine

Energy is converted (heat-mechanical)

#### (C) Incandescent lamp

Heat  $\rightarrow$  Light; radiation from hot body.

#### (D) Electric fuse

Works on melting of fuse wire on heating. Heat  $\rightarrow$  P.E. of molecules.

3. For (A)  

$$Q = 0$$
,  $W = PdV = 0$  so  $\Delta U = 0 \Rightarrow T = constant$   
For (B):

$$P \propto V^{-2} \& PV = \mu RT \Longrightarrow V \propto \frac{1}{T}$$

Since volume increases so temperature decreases. For polytropic process  $PV^2 = constant$ 

$$C = C_v + \frac{R}{1 - x} = C_v + \frac{R}{1 - 2} = \frac{3}{2}R - R = \frac{R}{2}$$

$$Q = \mu C \Delta T = \mu \left(\frac{R}{2}\right) \Delta T = \text{Negative}$$

For (C):

$$C = C_v + \frac{R}{1 - \frac{4}{3}} = -\frac{3}{2}R \implies Q = \mu C \Delta T$$

$$=-\mu \left(\frac{3}{2}R\right)\Delta T \equiv Positive$$

For (D):

$$P \uparrow, V \uparrow, T \uparrow$$

Work = Area under PV curve  $\rightarrow$  positive

 $\Delta U \rightarrow positive$ 

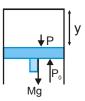
 $Q \rightarrow positive (given to system)$ 

#### Comprehension #1

 When the piston is pulled out slowly, the pressure drop produced inside the cylinder is almost instantaneously neutralised by the air entering from outside into the cylinder. Therefore the pressure inside is P<sub>0</sub>.

2. 
$$Mg = (P_0 - P) \pi R^2 \implies P = P_0 - \frac{Mg}{\pi R^2}$$

Since the cylinder is thermally conducting, the temperature remains the same.



$$P_0 (2L \times \pi R^2) = P(y \times \pi R^2) \implies y = \left(\frac{P_0 \times \pi R^2}{P_0 \pi R^2 - Mg}\right) (2L)$$

**3.** Equating pressures

$$P_0 + \rho g(L_0 - H) = P = \frac{P_0 L_0}{(L_0 - H)}$$

### Comprehension #2

- Force due to the pressure of liquid = The buoyancy force.
- 2.  $T^{\gamma}P^{1-\gamma}=\text{constant} \Rightarrow T_2 = T_1 \left(\frac{P_2}{P_1}\right)^{\frac{\gamma-1}{\gamma}}$

$$=T_0 \left( \frac{P_0 + \rho_{\ell} g(H - y)}{P_0 + \rho_{\ell} gH} \right)^{1 - \frac{3}{5}} = T_0 \left( \frac{P_0 + \rho_{\ell} g(H - y)}{P_0 + \rho_{\ell} gH} \right)^{\frac{2}{5}}$$

3. Buoyancy force =  $V\rho_{\ell}g = \left(\frac{nRT_2}{P_2}\right)\rho_{\ell}g$ 

$$=\frac{nR\rho_{\ell}gT_{0}}{P_{0}+\rho_{\ell}g(H-y)}\Bigg[\frac{P_{0}+\rho_{\ell}g(H-y)}{P_{0}+\rho_{\ell}gH}\Bigg]^{2}$$

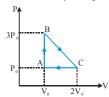
$$= \frac{\rho_{\ell} n R g T_0}{(P_0 + \rho_{\ell} g H)^{\frac{2}{5}} (P_0 + \rho_{\ell} g (H - y)^{\frac{3}{5}}}$$

### Comprehension #3

1. D 2. D

### **Subjective Questions**

1. (a) ABCA is a clockwise cyclic process.



∴ Work done by the gas W = + Area of triangle ABC

$$W = \frac{1}{2} \text{ (base) (height)} = \frac{1}{2} (2V_0 - V_0) (3P_0 - P_0) = P_0 V_0$$

(b) No. of moles n=1 and gas is monoatomic, therefore

$$C_V = \frac{3}{2} R$$
 and  $C_P = \frac{5}{2} R \Rightarrow \frac{C_V}{R} = \frac{3}{2}$  and  $\frac{C_P}{R} = \frac{5}{2}$ 

(i) Heat rejected in path CA (Process is isobaric)

$$\therefore Q_{CA} = C_p \Delta T = C_p (T_f - T_i) = C_p \left( \frac{P_f V_f}{R} - \frac{P_i V_i}{R} \right)$$
$$= \frac{C_p}{R} (P_f V_f - P_i V_i)$$

Substituting the values

$$Q_{CA} = \frac{5}{2} (P_0 V_0 - 2P_0 V_0) = -\frac{5}{2} P_0 V_0$$

Therefore, heat rejected in the process CA is  $\frac{5}{2} P_0 V_0$ .

(ii) Heat absorbed in path AB:

(process is isochoric)

$$\therefore Q_{AB} = C_{V}\Delta T = C_{V}(T_{f} - T_{i})$$

$$= C_{V}\left(\frac{P_{f}V_{f}}{R} - \frac{P_{i}V_{i}}{R}\right) = \frac{C_{V}}{R}(P_{f}V_{f} - P_{i}V_{i})$$

$$= \frac{3}{2}(P_{f}V_{f} - P_{i}V_{i}) = \frac{3}{2}(3P_{0}V_{0} - P_{0}V_{0}) = 3P_{0}V_{0}$$

- $\therefore$  Heat absorbed in the process AB is  $3P_0V_0$ .
- (c) Let Q<sub>BC</sub> be the heat absorbed in the process BC Total heat absorbed

$$Q = Q_{CA} + Q_{AB} + Q_{BC}$$

$$Q = \left(-\frac{5}{2}P_0V_0\right) + (3P_0V_0) + Q_{BC}$$

$$Q = Q_{BC} + \frac{P_0 V_0}{2}$$

Change in internal energy  $\Delta U = 0$ 

$$\therefore Q = W \qquad \therefore Q_{BC} + \frac{P_0 V_0}{2} = P_0 V_0$$

$$\Rightarrow$$
  $\therefore$   $Q_{BC} = \frac{P_0 V_0}{2}$ 

- $\therefore$  Heat absorbed in the process BC is  $\frac{P_0V_0}{2}$
- (d) Maximum temperature of the gas will some where between B and C. Line BC is a straight line. Therefore, P-V equation for the process BC can be written as

$$P = -mV + c; (y = mx + c)$$

Here, 
$$m = \frac{2P_0}{V_0}$$
 and  $c = 5P_0$  :  $P = -\left(\frac{2P_0}{V_0}\right)V + 5P_0$ 

Multiplying the equation by V

$$PV = -\left(\frac{2P_0}{V_0}\right)V^2 + 5P_0V \text{ (PV = RT for n=1)}$$

$$RT = -\left(\frac{2P_0}{V_0}\right)V^2 + 5P_0V$$

$$\Rightarrow T = \frac{1}{R} \left[ 5P_0V - \frac{2P_0}{V_0}V^2 \right] \qquad ...(i)$$

For T to be maximum

$$\frac{dT}{dV} = 0 \implies 5P_0 - \frac{4P_0}{V_0}, V = 0 \implies V = \frac{5V_0}{4}$$

i.e., at  $V = \frac{5V_0}{4}$  (on line BC), temperature of the gas is

maximum

From Equation (i) this maximum temperature will be

$$T_{max} = \frac{1}{R} \left[ 5P_0 \left( \frac{5V_0}{4} \right) - \frac{2P_0}{V_0} \left( \frac{5V_0}{4} \right)^2 \right] = \frac{25}{8} \frac{P_0 V_0}{R}$$

2. In the first part of the question  $(t \le t_1)$ At t = 0,  $T_X = T_0 = 400$ K and at  $t = t_1$   $T_X = T_1 = 350$ K Temperature of atmosphere,  $T_A = 300$ K (constant) This cools down according to Newton's law of cooling. Therefore, rate of cooling  $\infty$  temperature difference.

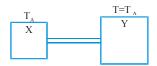


$$\therefore \left( -\frac{dT}{dt} \right) = k(T - T_A) \Rightarrow \frac{dT}{T - T_A} = -k.dt$$

$$\Rightarrow \int_{T_0}^{T_1} \frac{dT}{T - T_A} = -k \int_0^{t_1} dt \Rightarrow \ell n \left( \frac{T_1 - T_A}{T_0 - T_A} \right) = -kt_1$$

$$\Rightarrow kt_1 = -\ell n \left( \frac{350 - 300}{400 - 300} \right) \Rightarrow kt_1 = \ell n(2)$$

In the II<sup>nd</sup> part, body X cools by radiation (according to Newton's law) as well as by conduction  $(t > t_1)$ .



Therefore, rate of cooling

= (cooling by radiation) + (cooling by conduction)

In conduction 
$$\frac{dQ}{dt} = \frac{KA(T - T_A)}{L} = C\left(-\frac{dT}{dt}\right)$$

$$\therefore \left(-\frac{dT}{dt}\right) = \frac{KA}{LC}(T - T_A)$$

where C = heat capacity of body X

$$\therefore \left(-\frac{dT}{dt}\right) = k(T - T_A) + \frac{KA}{CL}(T - T_A) \qquad ...(ii)$$

$$\left(-\frac{dT}{dt}\right) = \left(k + \frac{KA}{CL}\right)(T - T_A) \qquad ...(iii)$$

Let at  $t = 3t_1$ , temperature of X becomes  $T_2$ Therefore, from Equation (iii)

$$\int\limits_{T_{1}}^{T_{2}} \frac{dT}{T-T_{A}} = -\bigg(k + \frac{KA}{LC}\bigg) \int\limits_{t_{1}}^{3t_{1}} dt$$

$$\implies \ell n \left( \frac{T_2 - T_A}{T_1 - T_A} \right) = - \left( k + \frac{KA}{LC} \right) (2t_1)$$

$$= -\left(2kt_1 + \frac{2KA}{LC}t_1\right)$$

$$\Rightarrow \ln \left( \frac{T_2 - 300}{350 - 300} \right) = -2\ln(2) - \frac{2KAt_1}{LC}$$

 $\Rightarrow$  kt<sub>1</sub>= $\ell$ n2 from Equation (i)

This equations gives  $T_2 = \left(300 + 12.5e^{\frac{-2KAt_1}{CL}}\right)$  kelvin

3. The P–V diagram for the complete process will be

P C P<sub>2</sub> B P A V V V V V

as follows

Process  $A \rightarrow B$  is adiabatic compression and Process  $B \rightarrow C$  is isochoric.

(b) (i) Total work done by the gas process A - B:

$$W_{_{AB}} = \frac{P_{_{A}}V_{_{A}} - P_{_{B}}V_{_{B}}}{\gamma - 1} = \frac{P_{_{i}}V_{_{i}} - P_{_{f}}V_{_{f}}}{\gamma - 1} = \frac{P_{_{1}}V_{_{1}} - P_{_{2}}V_{_{2}}}{\frac{5}{3} - 1}$$

$$= \frac{P_1 V_1 - P_1 \left(\frac{V_1}{V_2}\right)^{\gamma} V_2}{2/3} \left[ \therefore P_1 V_1^{\gamma} = P_2 V_2^{\gamma} \right]$$

$$= \frac{3}{2} P_1 V_1 \left\lceil 1 - \left( \frac{V_1}{V_2} \right)^{\gamma - 1} \right\rceil = -\frac{3}{2} P_1 V_1 \left\lceil \left( \frac{V_1}{V_2} \right)^{5/3 - 1} - 1 \right\rceil$$

$$= -\frac{3}{2} P_1 V_1 \left[ \left( \frac{V_1}{V_2} \right)^{2/3} - 1 \right]$$

Process B-C:  $W_{BC} = 0$  (V= constant)

$$\therefore W_{Total} = W_{AB} + W_{BC} = -\frac{3}{2} P_1 V_1 \left[ \left( \frac{V_1}{V_2} \right)^{2/3} - 1 \right]$$

## (ii) Total change in internal energy

#### Process A-B

 $Q_{AB} = 0$  (Process is adiabatic)

$$\Delta U_{AB} = -W_{AB} = \frac{3}{2} P_1 V_1 \left[ \left( \frac{V_1}{V_2} \right)^{2/3} - 1 \right]$$

### Process B-C

 $W_{RC} = 0$ 

$$\Delta U_{RC} = Q_{RC} = Q \text{ (Given)}$$

$$\Delta U_{Total} = \Delta U_{AB} + \Delta U_{BC} = \frac{3}{2} P_1 V_1 \left[ \left( \frac{V_1}{V_2} \right)^{2/3} - 1 \right] + Q$$

### (iii) Final temperature of the gas

$$\Delta U_{Total} = nC_{V}\Delta T = 2\left(\frac{R}{\gamma - 1}\right)(T_{C} - T_{A})$$

$$\therefore \frac{3}{2} P_1 V_1 \left[ \left( \frac{V_1}{V_2} \right)^{2/3} - 1 \right] + Q = \frac{2R}{5/3 - 1} \left( T_C - \frac{P_A V_A}{2R} \right)$$

$$\Rightarrow \frac{3}{2}P_1V_1\left[\left(\frac{V_1}{V_2}\right)^{2/3} - 1\right] + Q = 3R\left(T_C - \frac{P_1V_1}{2R}\right)$$

$$T_{C} = \frac{Q}{3R} + \frac{P_{1}V_{1}}{2R} \left(\frac{V_{1}}{V_{2}}\right)^{2/3} = T_{final}$$

4. (i) Number of moles

 $n=2, T_1=300K$ 

During the process  $A \rightarrow B$ 

 $PT = constant \text{ or } P^2V = constant = K(say)$ 

$$\therefore P = \frac{\sqrt{K}}{\sqrt{V}}$$

$$W_{A\to B} = \int_{V_A}^{V_B} P.dV = \int_{V_A}^{V_B} \frac{\sqrt{K}}{\sqrt{V}} dV$$

$$= 2\sqrt{K} [\sqrt{V_B} - \sqrt{V_A}] = 2[\sqrt{KV_B} - \sqrt{KV_A}]$$

$$= 2\left[\sqrt{(P_B^2 V_B)V_B} - \sqrt{(P_A^2 V_A)V_A}\right] (K = P^2 V)$$

$$= 2[P_B V_B - P_A V_A] = 2[nRT_B - nRT_A]$$

$$= 2nR[T_1 - 2T_1] = (2)(2)(R)[300 - 600] = -1200R$$

... Work done on the gas in the process AB is 1200R.

(ii) Heat absorbed/released in different processes. Since, the gas is monoatomic.

Therefore, 
$$C_V = \frac{3}{2} R$$
 and  $C_P = \frac{5}{2} R$  and  $\gamma = \frac{5}{3}$ 

#### Process A-B:

$$\Delta U = nC_V \Delta T = (2) \left(\frac{3}{2}R\right) (T_B - T_A) = (2) \left(\frac{3}{2}R\right)$$

(300-600) = -900R

 $\begin{array}{ll} \therefore & Q_{A\rightarrow B} = W_{A\rightarrow B} + \Delta U = (-1200R) - (900 R) \\ Q_{A\rightarrow B} = -2100R(Released) \end{array}$ 

#### Process B-C:

Process is isobaric

 $Q_{B\to C} = nC_p \Delta T$   $= (2) \left(\frac{5}{2}R\right) (T_C - T_B) = 2\left(\frac{5}{2}R\right) (2T_1 - T_1)$  = (5R) (600-300)  $Q_{B\to C} = 1500 \text{ R(absorbed)}$ 

#### **Process C-A:**

Process is isothermal

$$\Delta U = 0 \text{ and } Q_{C \to A} = W_{C \to A} = nRT_C \ell n \left(\frac{P_C}{P_A}\right)$$
$$= nR(2T_1)\ell n \left(\frac{2P_1}{P_1}\right) = (2)(R)(600)\ell n(2)$$
$$Q_{C \to A} = 831.6 \text{ R (absorbed)}$$

5. Let m be the mass of the container. Initial temperature of container,  $T_i = (227 + 273) = 500$  K and final temperature of container,

$$T_f = (27 + 273) = 300 \text{ K}$$

Now, heat gained by the ice cube = heat lost by the container i.e., (mass of ice) (latent heat of fusion of ice) + (mass of ice) (specific heat of water)

$$T_i = (227 + 273) = 500 \text{ K}$$

$$(300 \text{ K} - 273 \text{ K}) = -m \int_{T}^{T_i} S.dT$$

Substituting the values, we have

 $(0.1)(8 \times 10^4) + (0.1)(10^3)(27)$ 

$$= -m \int\limits_{500}^{300} (A + BT) dT \text{ of } 10700 = -m \left[AT + \frac{BT^2}{2}\right]_{500}^{300}$$

After substituting the values of A and B and the proper limits

we get m = 0.495 kg.

### **6.** Given:

No. of moles, n=2

$$C_V = \frac{3}{2} R \& C_P = \frac{5}{2} R$$

(Monoatomic)

$$T_A = 27^{\circ}C = 300 \text{ K}$$

Let 
$$V_A = V_0$$

then 
$$V_B = 2V_0$$

and 
$$V_D = V_C = 4V_0$$

### (i) Process $A \rightarrow B$ :

$$V \propto T \Rightarrow \frac{T_B}{T_\Delta} = \frac{V_B}{V_\Delta}$$

$$T_{\rm B} = T_{\rm A} \left( \frac{V_{\rm B}}{V_{\rm A}} \right) = (300)(2) = 600 {\rm K}$$

$$T_{\rm B} = 600 \, \rm K$$

### (ii) Process $A \rightarrow B$ :

$$V \propto T \Rightarrow P = constant$$

$$\therefore Q_{AB} = nC_p dT = nC_p (T_B - T_A)$$
$$= (2) \left(\frac{5}{2}R\right) (600 - 300)$$

$$\therefore$$
 Q<sub>AB</sub> = 1500R (absorbed)

#### Process $B \rightarrow C$ :

T = constant : dU = 0

$$∴Q_{BC} = W_{BC} = nRT_B \ell n \left(\frac{V_C}{V_B}\right) = (2) (R) (600) \ell n \left(\frac{4V_0}{2V_0}\right)$$
= (1200 R) \ell n(2) = (1200 R) (0.693)
$$⇒Q_{BC} \approx 831.6 \text{ R (absorbed)}$$

### Process $C \rightarrow D$

V = constant

$$\therefore Q_{CD} = nC_V dT = nC_V (T_D - T_C)$$

$$= n \left( \frac{3}{2} R \right) (T_A - T_B) (T_D = T_A \text{ and } T_C = T_B)$$

$$=(2)\left(\frac{3}{2}R\right)(300-600)$$

$$\Rightarrow$$
 Q<sub>CD</sub> = -900 R (released)

#### Process $D \rightarrow A$ :

 $T = constant \Rightarrow dU = 0$ 

$$\therefore$$
  $Q_{DA} = W_{DA} = nRT_D \ln \left( \frac{V_A}{V_D} \right)$ 

=(2)(R)(300)
$$ln\left(\frac{V_0}{4V_0}\right)$$
=600R $ln\left(\frac{1}{4}\right)$ 

$$Q_{DA} \approx -831.6 R$$
 (Released)

## (iii) In the complete cycle: dU = 0

Therefore, from conservation of energy

$$W_{net} = Q_{AB} + Q_{BC} + Q_{CD} + Q_{DA}$$

$$W_{net} = 1500R + 831.6R - 900R - 831.6R$$

$$\Rightarrow$$
 W<sub>net</sub> = W<sub>total</sub> = 600 R

#### 7. Given

Length of the wire  $\ell$ =5m

Radius of the wire  $r=2 \times 10^{-3}$ m

Density of wire  $\rho = 7860 \text{ kg/m}^3$ 

Young's, modulus

 $Y = 2.1 \times 10^{11} \text{ N/m}^2$  and specific heat

$$S = 420 \text{ J/kg-K}$$

Mass of wire, m = (density) (volume)

$$= (\rho) (\pi r^2 \ell) = (7860)(\pi)(2 \times 10^{-3})^2 (5) \text{ kg} = 0.494 \text{ kg}$$

Elastic potential energy stored in the wire,

$$U = \frac{1}{2} \text{ (stress) (strain)} \times \text{ (volume)}$$

$$\Rightarrow U = \frac{1}{2} \left( \frac{Mg}{\pi r^2} \right) \left( \frac{\Delta \ell}{\ell} \right) (\pi r^2 \ell) = \frac{1}{2} (Mg) \cdot \Delta \ell$$

$$\therefore \quad \left(\Delta \ell = \frac{F\ell}{AY}\right) = \frac{1}{2} (Mg) \frac{(Mg\ell)}{(\pi r^2)Y} = \frac{1}{2} \frac{M^2 g^2 \ell}{\pi r^2 Y}$$

Substituting the values, we have

$$U = \frac{1}{2} \frac{(100)^2 (10)^2 (5)}{(3.14)(2 \times 10^{-3})^2 (2.1 \times 10^{11})} J = 0.9478 J$$

When the bob gets snapped, this energy is utilised in raising the temperature of the wire.

So, 
$$U = ms\Delta\theta$$

$$\Delta \theta = \frac{U}{ms} = \frac{0.9478}{0.494(420)}$$
°C or K

$$\Rightarrow \Delta\theta = 4.568 \times 10^{-3}$$
°C

### 8. Volume of the box = $1 \text{m}^3$

Pressure of the gas =  $100 \text{N/m}^2$ 

Let T be the temperature of the gas.

#### Then

(i) Time between two consecutive collisions with one

wall = 
$$\frac{1}{500}$$
 s.

This time should be equal to  $\frac{2\ell}{v_{rms}}$ 



M=100kg

where  $\ell$  is the side of the cube.

$$\Rightarrow \frac{2\ell}{v_{rms}} = \frac{1}{500} \Rightarrow v_{rms} = 1000 \text{m/s (as } \ell=1 \text{m)}$$

$$\Rightarrow \sqrt{\frac{3RT}{M}} = 1000$$

$$T = \frac{(1000)^2 M}{3R} = \frac{(10)^6 (4 \times 10^{-3})}{3(25 / 3)} = 160 K$$

(ii) Average kinetic energy per atom =  $\frac{3}{2}$ kT

= 
$$\frac{3}{2}$$
 (1.38 × 10<sup>-23</sup>)(160) J = 3.312 × 10<sup>-21</sup> J

(iii) From PV = nRT = 
$$\frac{m}{M}$$
 RT

We get mass of helium gas in the box,  $m = \frac{PVM}{RT}$ 

Substituting the values we get

$$m = \frac{(100)(1)(4)}{(25/3)(160)} = 0.3g$$

9. Decrease in kinetic energy = increase in internal energy of the gas

$$\therefore \frac{1}{2} m v_0^2 = n C_v \Delta T = \left(\frac{m}{M}\right) \left(\frac{3}{2} R\right) \Delta T \therefore \Delta T = \frac{M v_0^2}{3 R}$$

10. (i) Rate of heat loss per unit area due to radiation  $I = e\sigma(T^4 - T_0^4)$ 

Here. 
$$T = 127 + 273 = 400 \text{ K}$$
  
and  $T_0 = 27 + 273 = 300 \text{ K}$ 

$$I = 0.6 \times \frac{17}{3} \times 10^{-8} [(400)^4 - (300)^4] = 595 \text{ W/m}^2$$

(ii) Let  $\theta$  be the temperature of the oil.

Then, rate of heat flow through conduction = rate of heat loss due to radiation

$$\frac{\text{temperature difference}}{\text{thermal resistance}} = (595)A$$

$$\Rightarrow \frac{(\theta - 127)}{\left(\frac{\ell}{KA}\right)} = (595)A$$

Here, A = area of disc; K = thermal conductivity and  $\ell$  = thickness (or length) of disc

$$\therefore \quad (\theta - 127) \frac{K}{\ell} = 595$$

$$\theta = 595 \left(\frac{\ell}{K}\right) + 127 = \frac{595 \times 10^{-2}}{0.167} + 127 = 162.6^{\circ}C$$

11. At constant pressure

$$V \propto T \Rightarrow \frac{V_2}{V_1} = \frac{T_2}{T_1} \Rightarrow \frac{Ah_2}{Ah_1} = \frac{T_2}{T_1}$$

$$\therefore h_2 = h_1 \left( \frac{T_2}{T_1} \right) = (1.0) \left( \frac{400}{300} \right) m = \frac{4}{3} m$$

As there is no heat loss, process is adiabatic.

For adiabatic process  $T_f V_f^{\gamma-1} = T_i V_i^{\gamma-1}$ 

$$\therefore T_{_f} = T_{_i} \left(\frac{V_{_i}}{V_{_f}}\right)^{\gamma-1} = (400) \left(\frac{h_{_i}}{h_{_f}}\right)^{1.4-1} = 400 \left(\frac{4}{3}\right)^{0.4}$$

12. When the temperature is increased, volume of the cube will increase while density of liquid will decrease. The depth upto which the cube is submerged in the liquid remains the same, hence the upthrust will not change.

$$F = F'$$
  $\therefore V_i \rho_L g = V_i' \rho'_L g$   
( $V_i = \text{volume immersed}$ )

$$\therefore (Ah_i)(\rho_L)(g) = A(1 + 2\alpha_s \Delta T) (h_i) \left(\frac{\rho_L}{1 + \gamma_c \Delta T}\right) g$$

Solving this equation, we get  $\gamma_1 = 2\alpha_s$ 

Rate of heat conduction through rod= rate of the heat lost from right end of the rod.

$$\therefore \frac{KA(T_1 - T_2)}{L} = eA\sigma(T_2^4 - T_s^4) \qquad ...(i)$$

Given that  $T_2 = T_s + \Delta T$ 

$$\therefore T_2^4 = (T_s + \Delta T)^4 = T_s^4 \left(1 + \frac{\Delta T}{T_s}\right)^4$$

Using binomial expansion, we have

$$T_2^4 = T_s^4 \left( 1 + 4 \frac{\Delta T}{T_s} \right) (as \Delta T << T_s)$$

$$T_2^4 - T_s^4 = 4(\Delta T)(T_s^3)$$

Substituting in Eq.(i), we have

$$\frac{K(T_1 - T_s - \Delta T)}{L} = 4e\sigma T_s^3.\Delta T$$

$$\Rightarrow \frac{K(T_1 - T_s)}{I_s} = \left(4e\sigma T_s^3 + \frac{K}{I_s}\right)\Delta T$$

$$\Delta T = \frac{K(T_1 - T_s)}{(4e\sigma LT^3 + K)}$$

Comparing with the given relation, proportionality

$$constant = \frac{K}{4e\sigma LT_s^3 + K}$$

14. (a) From  $\Delta Q = ms\Delta T$ 

$$\Delta T = \frac{\Delta Q}{ms} = \frac{20000}{1 \times 400} = 50^{\circ}C$$

(b) 
$$\Delta V = V \gamma \Delta T = \left(\frac{1}{9000}\right) (8 \times 10^{-5}) (50)$$
  
=  $5 \times 10^{-7} \,\text{m}^3$ 

: 
$$W = P.\Delta V = (10^5) (5 \times 10^{-7}) = 0.05 J$$

(c) 
$$\Delta U = \Delta Q - W = (20000 - 0.05) J = 19999.95 J$$

15. 0.05 kg steam at 373 K  $\xrightarrow{Q_1}$  0.05 kg water at 373 K

0.05 kg water at 373 K  $\longrightarrow$  0.05 kg water at 273 K

0.45 kg ice at 253 K  $\xrightarrow{Q_3}$  0.45 kg ice at 273 K

0.45 kg ice at 273 K  $_{-Q_4}$  0.45 kg water at 273 K

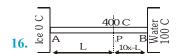
 $Q_1 = (50)(540) = 27,000 \text{ cal} = 27 \text{ kcal}$ 

 $Q_2 = (50)(1)(100) = 5000 \text{ cal} = 5 \text{ kcal}$ 

 $Q_3 = (450)(0.5)(20) = 4500 \text{ cal} = 4.5 \text{ kcal}$ 

 $Q_4 = (450)(80) = 36000 \text{ cal} = 36 \text{ kcal}$ 

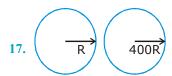
Now since  $Q_1 + Q_2 > Q_3$  but  $Q_1 + Q_2 < Q_3 + Q_4$  ice will come to 273K from 253 K, but whole ice will not melt. Therefore, temperature of the mixture is 273K.



$$\frac{k(400-0)A}{I} = m(80)$$
 ...(i)

$$\frac{kA(400-100)}{(10x-L)} = m(540) \qquad ...(ii)$$

Divide (i) by (ii) 1080 x = 120 L :  $L = \lambda x$  :  $\lambda = 9$ 



$$\frac{\lambda_A}{\lambda_B} = \frac{T_B}{T_A}$$

$$P = \sigma e A T_4$$

$$P_A = \sigma e. 4\pi (400 R)^2 \times T_A^4$$

$$P_B = \sigma e. 4pR^2 \times T_B^4$$

$$(400R)^2 \times T_A^4 = 10^4 \times T_B$$

$$\begin{aligned} &P_{B} = \sigma e. \ 4pR^{2} \times T_{B}^{4} \\ &(400R)^{2} \times T_{A}^{4} = 10^{4} \times T_{B}^{4} \\ &16 \times 10^{4} \times T_{A}^{4} = 10^{4} \times T_{B}^{4} \end{aligned}$$

$$\frac{T_B}{T_A} = 2$$

**18.** 2 **19.** 9 **20.** 3

#### **MOCK TEST: BASIC MATHS**

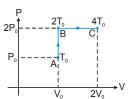
Let initial pressure, volume, temperature be  $P_0$ ,  $V_0$ ,  $T_0$ indicated by state A in P-V diagram. The gas is then isochorically taken to state B (2P<sub>0</sub>, V<sub>0</sub>, 2T<sub>0</sub>) and then taken from state B to state C  $(2P_0, 2V_0, 4T_0)$  isobarically. Total heat absorbed by 1 mole of gas

$$\Delta Q = C_v (2T_0 - T_0) + C_p (4T_0 - 2T_0)$$

$$\sum_{v} (2\mathbf{I}_{0} - \mathbf{I}_{0}) + C_{p} (4\mathbf{I}_{0} - 2\mathbf{I}_{0})$$

$$= \frac{5}{2} R T_0 + \frac{7}{2} R \times 2T_0 = \frac{19}{2} RT_0$$

Total change in temperature from state A to C is  $\Delta T = 3T_0$ 



.. Molar heat capacity

$$= \frac{\Delta Q}{\Delta T} = \frac{\frac{19}{2}RT_0}{3T_0} = \frac{19}{6}R.$$

2. In an ideal gas internal energy =  $\frac{1}{2}$  nRT

$$U = \frac{5}{2} \times 2 \times RT + 4 \times \frac{3}{2} RT = 11 RT.$$

3. Heat absorbed by gas in three processes is given by

$$Q_{ACB} = \Delta U + W_{ACB}$$

$$Q_{ADB} = \Delta U$$

$$Q_{AEB} = \Delta U + W_{AEB}$$

The change in internal energy in all the three cases is same. And  $W_{ACB}$  is +ve,  $W_{AEB}$  is -ve.

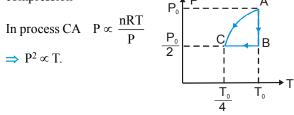
Hence 
$$Q_{ACB} > Q_{ADB} > Q_{AEB}$$

4. In an adiabatic expansion, internal energy decreases and hence temperature decreases.

: from equation of state of ideal gas

PV = nRT  $\Rightarrow$  The product of P and V decreases.

5. Process AB is isothermal expansion, BC is isobaric compression



## PHYSICS FOR JEE MAINS & ADVANCED

- Higher is the temperature greater is the most probable speed.
- The rate of heat loss by a thin hollow sphere of thickness ' $\Delta x$ ', mean radius 'r' and made of density ' $\rho$ ' is given by

mS 
$$\frac{dT}{dt} = -\varepsilon \sigma A (T^4 - T_0^4)$$

$$(\rho\, 4\pi r^2 \Delta x) \,\, S \, \frac{dT}{dt} = -\, \epsilon \sigma \, 4\pi r^2 \, (T^4 - {T_0}^4) \, \label{eq:phi}$$

$$\Rightarrow \frac{dT}{dt} = -\frac{\varepsilon\sigma(T^4 - T_0^4)}{S\Delta x}$$
 is independent of radius

Hence rate of cooling is same for both spheres.

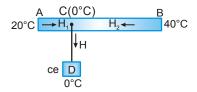
8. Thermal resistance of AC  $\left(=\frac{L}{K\Delta}\right)$ 

$$= \frac{0.1}{336 \times 1 \times 10^{-4}} = \frac{10^3}{336} = R \text{ (suppose)}$$

thermal resistance of BC = 
$$\frac{0.2}{336 \times 10^{-4}} = 2R$$

temperature of point C

$$\therefore H_1 = \frac{20}{R}$$
 ;  $H_2 = \frac{40}{2R} = \frac{20}{R}$ 



$$\therefore H = H_1 + H_2 = \frac{40}{R} = \frac{40 \times 336}{10^3} = \frac{13440}{10^3}$$
$$= 13.44 \text{ watt}$$

Rate of melting of ice =  $\frac{H}{I} = \frac{13.44 / 4.2}{80}$  g/s = 40 mg/s

- 9. Since tension is the two rods will be same, hence  $A_1Y_1\alpha_1 \Delta\theta = A_2Y_2\alpha_2 \Delta\theta$   $\Rightarrow$   $A_1Y_1\alpha_1 = A_2Y_2\alpha_2$
- **10.**  $V_{r.m.s.} = \sqrt{\frac{1^2 + 0^2 + 2^2 + 3^2}{4}} = \sqrt{3.5}$ .
- 11. We have  $\rho = \frac{PM}{PT}$

$$\frac{P_1M}{RT_1} = \frac{P_2M}{RT_2}$$
  $\frac{P_1}{T_1} = \frac{P_2}{2T_1}$ 

 $P_2 = 2P_1$  i.e., change in pressure is 100%.

12. Strain developed:

$$\varepsilon = \alpha \Delta T = (12 \times 10^{-6}) (50) = 6 \times 10^{-4}$$

Strain will be negative, as the rod is in a compressed

13. Heat current :  $i = -kA \frac{dT}{dx}$ 

$$idx = -kA dT$$

$$i\int_{0}^{\ell} dx = -A\alpha \int_{T_{L}}^{T_{2}} T dT \implies i \ell = -A\alpha \frac{(T_{2}^{2} - T_{1}^{2})}{2}$$

$$\Rightarrow i = \frac{A \alpha (T_1^2 - T_2^2)}{2 \ell}$$

- 14. BC is isochoric.  $V_B > V_A$ ,  $V_B = V_C$ ,  $V_D > V_C$

$$\Delta U_{AB} = \frac{f}{2} nR \Delta T$$



$$\Rightarrow \frac{f}{2}(\Delta PV) \Delta U_{AB} = \frac{5}{2}(\Delta PV) \qquad Q_{AB} = 2.5 P_0 V_0$$

$$Q_{AB} = 2.5 P_0 V_0$$

Process BC 
$$Q_{BC} = \Delta U_{BC} + W_{BC}$$
  
 $Q_{BC} = 0 + 2P_0V_0\log 2 = 1.4 P_0V_0$   
 $Q_{net} = Q_{AB} + Q_{BC} = 3.9 P_0V_0$ 

16. 
$$\frac{X - (-125)}{500} = \frac{Y - (-70)}{40}$$

For 
$$Y = 50$$

$$X = 1375.0^{\circ}X$$

17. Rate of radiation per unit area is proportional to  $(T^4)$ 

$$\therefore$$
 P \propto AT<sup>4</sup> \Rightarrow P \propto r<sup>2</sup>.

Also ms 
$$\frac{dT}{dt} \propto AT^4$$
  $\therefore \frac{dT}{dt} = R \propto \frac{1}{r}$ 

$$\therefore \frac{dT}{dt} = R \propto \frac{1}{r}$$

(because  $m = (V\rho) \propto r^3$  and  $A \propto r^2$ )

18. For a block body, wavelength for maximum intensity:

$$\lambda \propto \frac{1}{T}$$
 &  $P \propto T^4 \implies P \propto \frac{1}{\lambda^4} \implies P' = 16 P$ .

$$\therefore$$
 P'T' = 32PT

19. Since, e = a = 0.2 (Since, a = (1 - r - t) = 0.2 for the body B)

$$E = (100)(0.2) = 20 \text{ W/m}^2$$

20. Thermal equilibrium means same temperature.

21. 
$$\frac{C}{5} = \frac{F - 32}{9} \implies \frac{\Delta C}{5} = \frac{\Delta F}{9}$$
  
 $\Delta C = \frac{5}{9} \Delta F \implies \Delta C = \Delta K$ 

22. PV = RT for 1 mole

$$W = \int P dV = \int \frac{RT}{V} dV \implies V = CT^{2/3}$$

$$\therefore dV = \frac{2}{3} CT^{-1/3} dT \text{ or } \frac{dV}{V} = \frac{2}{3} \frac{dT}{T}$$

: 
$$W = \int_{T_1}^{T_2} RT\left(\frac{2}{3}\right) \frac{dT}{T} = \frac{2}{3} R(T_2 - T_1) = 166.2 J$$

23. 
$$\Delta s \Delta U = \frac{nfR}{2} \Delta T$$

 $\Delta U \propto \Delta T$ ;

Since volume is same in all three process therefore temperature will be least having least pressure.

24.  $\log P = m \log V$  where m is slope

$$m = \frac{2.38 - 2.10}{1.1 - 1.3} = -1.4$$

$$\log P = -1.4 \log V$$

$$\log PV^{1.4} = 0$$

$$PV^{1.4} = k$$

25. Rate of heat loss =  $\sigma$  eA (T<sup>4</sup> – T<sub>s</sub><sup>4</sup>)

$$-\operatorname{ms} \frac{dT}{dt} = \sigma \operatorname{eA} (T^4 - T_s^4)$$

$$-\frac{dT}{dt} = \frac{5.8 \times 10^{-4} \times i \times T(0.08)^{2} ((500)^{4} (300)^{4})}{10 \times 4.2 \times 90}$$

$$\Rightarrow \frac{-dT}{dt} = 0.066 \text{ °C/sec.}$$

**26.** In the equilibrium position the net force on the partition will be zero.

Hence pressure on both sides are same.

Hence, (A) is correct.

Initially, PV = nRT

$$n_1 = \frac{P_1 V_1}{RT_1} = \frac{PV}{RT}$$
 &  $n_2 = \frac{(2P)(2V)}{RT} = 4\frac{PV}{RT}$ 

$$\Rightarrow$$
  $n_2 = 4n_1$ 

Moles remains conserved.

Finally, pressure becomes equal in both parts.

Using, 
$$P_1V_1 = n_1RT_1 \Rightarrow P_2V_2 = n_2RT_2$$

$$P_1 = P_2 \& T_1 = T_2$$

$$\therefore \frac{V_1}{V_2} = \frac{n_1}{n_2} = \frac{1}{4} \implies V_2 = 4V_1$$

Also 
$$V_1 + V_2 = 3V \implies V_1 + 4V_1 = 3V$$

$$\Rightarrow$$
  $V_1 = \frac{3}{5}V$  And  $V_2 = \frac{12}{5}V$ 

Hence (B) and (C) are correct.

In compartment (I):

$$P_1' V_1 = n_1 R T_1$$

$$P_1'\left(\frac{3V}{5}\right) = \left(\frac{PV}{RT}\right)R(T)$$

$$P_1' = \frac{5PV}{3V} = \frac{5}{3}P$$

Hence (D) is also correct.

27. 
$$\frac{P^2}{Q} = k \implies \frac{P^2RT}{PM} = k$$

$$\Rightarrow$$
 PT =  $\left(\frac{kM}{R}\right)$  .....(i)

$$\frac{P^2}{\rho} = \frac{P'^2}{\rho/2} \Rightarrow P' = \frac{P}{\sqrt{2}}$$

Hence from (i) T' =  $T\sqrt{2}$ . PT = constant hence P – T curve is a hyperabola.

**28.** 
$$V_{r.m.s.} = \sqrt{\frac{3kT}{m}}$$

Since PV = nRT therefore P and V both can change simultaneously keeping temperature constant.

29. Slope of graph is smaller in the solid state i.e., temperature is rising slower, hence higher heat capacity.

The transition from solid to liquid state takes lesser time, hence latent heat is smaller.

30. Initial state is same for all three processes (say initial internal energy =  $E_0$ )

In the final state,  $V_A = V_B = V_C$ 

and 
$$P_A > P_B > P_C$$

$$\Rightarrow P_{A}V_{A} > P_{B}V_{B} > P_{C}V_{C} \Rightarrow E_{A} > E_{B} > E_{C}$$

$$f T_1 > T_2$$

then  $E_0 > E_f$  for all three processes

and hence 
$$(E_0 - E_1) < (E_0 - E_0) < (E_0 - E_0)$$

$$\Rightarrow |\Delta E_{A}| < |\Delta E_{B}| < |\Delta E_{C}|$$

If  $T_1 < T_2$ , then  $E_0 < E_f$  for all three processes

and hence 
$$(E_A - E_0) > (E_B - E_0) > (E_C - E_0)$$

$$\Rightarrow |\Delta E_{A}| > |\Delta E_{B}| > |\Delta E_{C}|$$

31. 
$$\frac{\Delta A}{A} \times 100 = 2 \left( \frac{\Delta \ell}{\ell} \right) \times 100$$

 $\Rightarrow$  % increase in Area =  $2 \times 0.2 = 0.4$ 

$$\frac{\Delta V}{V} \times 100 = 3 \times 0.2 = 0.6 \%$$

Since 
$$\Delta I = I \alpha \Delta T$$

$$\frac{\Delta \ell}{\ell} \times 100 = \alpha \Delta T \times 100 = 0.2 \implies \alpha = 0.25 \times 10^{-4} / ^{\circ}C$$

32. 
$$\Delta V_L = \Delta V_V \implies Y_L V_L = Y_V V_V \text{ or } \frac{Y_L}{Y_V} = \frac{V_V}{V_L}$$
  
but  $V_V > V_L \implies Y_L > Y_V$ 

- **33.** Every object emit and absorb the radiations simultaneously, if energy emitted is more than energy absorbed temperature falls and vice versa.
- **34.** Equivalent thermal conductivity of two identical rods in series is given by

$$\frac{2}{K} = \frac{1}{K_1} + \frac{1}{K_2}$$

If  $K_1 \le K_2$ , then  $K_1 \le K \le K_2$ . Hence statement 1 is false.

- 35. From Wein's law  $\lambda_m T = \text{constant i.e.}$ , peak emission wavelength  $\lambda_m \propto \frac{1}{T}$ . Hence as T increase  $\lambda_m$  decreases.
- 36. If the rate at which molecules of same mass having same rms velocity striking a wall decreases, then the rate at which momentum is imparted to the wall decreases. This results in lowering of pressure. Hence statement-2 is correct

In statement-1 the rms velocity of gas remains same on increasing the volume of container by piston, since the given process is isothermal. Now the piston is at a greater distance from opposite wall and hence time taken by gas molecules from near the opposite wall to reach the piston will be more. Thus rate of molecules striking the piston decreases. Hence statement-1 is correct and statement-2 is correct explanation.

37. Heat given:  $\Delta Q = n_1 C_{V_1} \Delta T \rightarrow \text{For gas A}$  & for Gas  $B \rightarrow \Delta Q = n_2 C_{V_2} \Delta T$ 

( $\cdot$ : For same heat given, temperature rises by same value for both the gases.)

$$\Rightarrow n_1 C_{V_1} = n_2 C_{V_2} \qquad ......(1$$
Also,  $(\Delta P_B)V = n_2 R\Delta T$  and  $(\Delta P_A)V = n_1 R\Delta T$ 

$$\Rightarrow \frac{n_1}{n_2} = \frac{\Delta P_A}{\Delta P_B} = \frac{2.5}{1.5} = \frac{5}{3} \Rightarrow n_1 = \frac{5}{3} n_2$$

Substituting in (1)

$$\frac{5}{3}$$
  $n_2$   $C_{v_1} = n_2 C_{v_2} \implies \frac{C_{v_2}}{C_{v_1}} = \frac{5}{3} = \frac{(\frac{5}{2}R)}{(\frac{3}{2}R)}$ 

Hence, Gas B is diatomic and Gas A is monoatomic.

**38.** Since 
$$n_1 = \frac{5}{3} n_2$$

Therefore 
$$\frac{125}{M_A} = \frac{5}{3} \left( \frac{60}{M_B} \right)$$

(From experiment 1 :  $W_A = 25 \text{ gm & } W_B = 60 \text{ gm}$ )

$$\Rightarrow$$
 5M<sub>B</sub> = 4M<sub>A</sub>

The above relation holds for the pair–Gas A: Ar and Gas B:  $O_2$ .

**39.** 
$$n_A C_{V_A} \times 300 + n_B C_{V_B} \times 300 = n_A C_{V_A} T + n_B C_{V_B} T$$

(number of moles remains same)

$$\Rightarrow$$
 T = 300 K

(It could also be seen directly that temperature finally will be 300 K, since no heat exchange takes place between those gases as their initial temperatures are same)

Since, volume remains same but number of moles increases.

Therefore, pressure increases.

**40.** We have  $\theta - \theta_s = (\theta_0 - \theta_s) e^{-kt}$ 

where  $\theta_0 = \text{Initial temperature of body} = 40^{\circ}\text{C}$ 

 $\theta$  = temperature of body after time t.

Since body cools from 40 to 38 in 10min, we have

$$38-30=(40-30) e^{-k10}$$
 .... (1

Let after 10 min, The body temp. be  $\theta$ 

$$\theta - 30 = (38 - 30) e^{-k \cdot 10}$$
 .... (2)

$$\frac{(1)}{(2)}$$
 gives  $\frac{8}{\theta - 30} = \frac{10}{8}$ ,  $\theta - 30 = 6.4$ 

$$\Rightarrow \theta = 36.4 \,^{\circ}\text{C}$$

- 41. Temperature will decrease exponentially
- 42. During heating process from 38 to 40 in 10 min. The body will lose heat in the surrounding which will be exactly equal to the heat lost when it cooled from 40 to 38 in 10 min, which is equal to ms  $\Delta\theta = 2 \times 2 = 4$  J. During heating process heat required by the body = m s  $\Delta\theta = 4$  J.
  - ∴ Total heat required = 8 J.

43. (A) If  $P = 2V^2$ , from ideal gas equation we get  $2V^3 = nRT$ 

- : with increase in volume
- (A) Temperature increases implies dU = +ve

$$\therefore dW = +ve$$
Hence  $dO = dU + W = +ve$ 

(B) If  $PV^2$  = constant, from ideal gas equation we get VT = K (constant)

On decreasing temperature, as volume of an ideal gas increases

$$dW = +ve$$

Now 
$$dQ = dU + PdV = nC_v dT - \frac{PK}{T^2} dT$$
 [:  $dV = -\frac{K}{T^2} dT$ ]

$$= nC_v dT - \frac{PV}{T} dT = n(C_v - R) dT$$

 $\therefore$  with increase in temperature dT = +ve

and since  $C_v > R$  for monoatomic gas. Hence dQ =+ve as temperature is increased

(C) 
$$dQ = nC dT = nC_{...} dT + PdV$$

$$\Rightarrow$$
 n (C, +2R) dT = nC, dT + PdV

$$\therefore 2nRdT = PdV \quad \therefore \frac{dV}{dT} = +ve$$

Hence with increase in temperature volume increases and vice versa.

$$dO = dU + W = +ve$$

(D) 
$$dQ = nC dT = nC_u dT + PdV$$

or 
$$n(C_v - 2R)dT = nC_r dT + PdV$$

or 
$$-2nRdT = PdV$$
  $\therefore \frac{dV}{dT} = -ve$ 

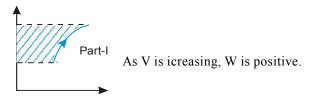
On decreasing temperature, as volume of an ideal gas increases

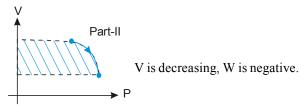
$$dW = +ve$$

Also 
$$dQ = n(C_y - 2R)dT$$

with increase in temperature dT = +ve but  $C_v < 2R$  for monoatomic gas. Therefore dQ = -ve with increase in temperature.

44. in (A), V is on vertical axis.





As negative work in part-II is greater than positive work in part-I, net work during the process is negative.

Using PV = nRT and as  $V_{remains}$  same for initial and final points of the process, it is obvious that final temp. is greater than initial temperature as pressure has increased. Therefore dU is positive. Hence option (S) is connected with (A).

As 
$$T = \frac{PV}{nR}$$

:. From graph we can say

Similar arguments can be applied to other graphs.

45. Due to the heating pressure inside is not changed. Let inside pressure be  $\rho$ . Then for equilibrium of the system:

$$P(A_1 - A_2) = P_0(A_1 - A_2) + (m_1 + m_2)g$$

$$\Rightarrow$$
 P $\Delta$ V = (P<sub>0</sub> $\Delta$ A + mg) $\ell$ 

$$\ell \text{ is displacement of the piston.}$$

$$P \cdot \Delta V = nR\Delta T.$$

$$\Delta T = \frac{P\Delta V}{nR}$$

$$= \frac{(P_0\Delta A + mg)\ell}{nR}$$

$$= \frac{(10^5 P_a \times 10^{-3} m^2 + 5 \times 10)(50 \times 10^{-2})}{1 \times R}$$

$$\Delta T = \frac{75}{R} K.$$

## PHYSICS FOR JEE MAINS & ADVANCED

**46.** Change in internal energy for cyclic process  $(\Delta U) = 0$ 

for process a 
$$\rightarrow$$
 b, (P - constant)  
 $W_{a \rightarrow b} = P.\Delta V = nR\Delta T = -400 R$ 

for process 
$$b \rightarrow c (T - constant)$$

$$W_{b\to c} = -2R((300)\ell n2$$

for process 
$$c \rightarrow d (P - constant)$$

$$W_{c \to d} = +400 R$$

for process 
$$d \rightarrow a (T - constant)$$

$$W_{d\to a} = +2R (500) \ell n2$$

Net work 
$$(\Delta W) = W_{a \rightarrow b} + W_{b \rightarrow c} + W_{c \rightarrow d} + W_{d \rightarrow a}$$
  
 $\Delta W = 400 \text{ R} \ell \text{n} 2$ 

- $\therefore$  dQ = dU + W, first law of thermady names.
- $dQ = 400 R \ell n2.$
- **47.** Energy supply by resistance

$$=i^2.R$$

By first law of thermodynamics

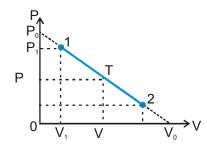
$$\Delta Q = \Delta U + \Delta W$$

$$\Delta U = 0$$

$$\therefore i^{2}R = mg\left(\frac{dx}{dt}\right) \implies v = \frac{F^{2}R}{mg} = \frac{2 \times 2 \times 10}{1 \times 10}$$

$$v = 4 \text{ m/s}.$$

48. 
$$Q = \Delta U + W$$



where  $\Delta U$  is the change in the internal energy of the gas; and W is work, done by the gas. For one mole of the monatomic ideal gas  $\Delta U = 3/2R \Delta T$ . Work equals the area under the graph

P vs. V

Therefore, for the process from the initial state with  $P_1V_1 = 3/2$  RT<sub>1</sub> to the state with P,V,T the heat given to system is

$$Q = (3/2) R (T - T_1) + (1/2) (P + P_1 (V - V_1)$$

$$= \frac{3}{2} (PV - P_1V_1) + \frac{1}{2} (PV + P_1V + PV_1 - P_1V_1) \dots (3)$$

$$= 2PV + \frac{1}{2}P_1V - \frac{1}{2}PV_1 - 2P_1V_1$$

from equation 1 and 3 we get

$$Q = 2\frac{P_0}{V_0}V^2 + \frac{5}{2}P_0V - 2P_0V_1\left(\frac{5}{4} - \frac{V_1}{V_0}\right)$$

The process switches from endothermic to exothermic

as 
$$\frac{dQ}{dV}$$
 changes from positive to negative, that is at

$$\frac{dQ}{dV} = 0$$
. Solving we get

$$V = \frac{5}{8} V_0$$