

# • CHEMICAL EQUILIBRIUM •

## **INTRODUCTION**

Chemical Reaction: Symbolic representation of any chemical change in terms of reactants and products is called chemical reaction.

Ex. 
$$N_2 + 3H_2 \rightarrow 2NH_3$$

# **Types of Chemical Reaction**

# On The Basis of Physical State

Homogeneous Reaction	Heterogeneous Reaction
All reactants and products are in same	Reactants and products are in more than one
phase	phase
$N_2(g) + 3H_2(g) \rightarrow 2NH_3(g)$	$Zn(s) + CO_2(g) \rightarrow ZnO(s) + CO(g)$

## On The Basis of Direction

	Reversible Reaction	Irreversible Reaction
(i)	Chemical reaction in which products can be converted back into reactants	(i) Chemical reaction in which products cannot be converted back into reactants.
	$N_2 + 3H_2 \longrightarrow 2NH_3$	$AgNO_3 + NaCl \longrightarrow AgCl + NaNO_3$
	$3\text{Fe} + 4\text{H}_2\text{O} \Longrightarrow \text{Fe}_3\text{O}_4 + 4\text{H}_2$	$NaCl + H_2SO_4 \longrightarrow NaHSO_4 + HCl$
	$H_2 + I_2 \Longrightarrow 2HI$	$Zn + H_2SO_4 \longrightarrow ZnSO_4 + H_2$
		$2KClO_3 \longrightarrow 2KCl + 3O_2$
(ii)	Proceed in forward as well as	(ii) Proceed only in one direction (forward).
	backward direction.	
(iii)	To obtain reverisible reactions, if anyone of the reactant or product is in gaseous	(iii) Generally possible in open container.
	state, then the reaction should be carried	
	out in closed vessel.	
	$CaCO_3(s) \longrightarrow CaO(s) + CO_2(g) \uparrow$	
(iv)	These attain equilibrium.	(iv) These do not attain equilibrium.
(v)	Reactants are never completely	(v) Reactants are completely converted
	converted into products.	into products.
(vi)	Generally thermal decomposition in	(vi) Generally thermal decomposition in
	closed vessel.	open vessel.
	$PCl_{5(g)} \longrightarrow PCl_{3(g)} + Cl_{2}(g)$	$PCl_{5(g)} \longrightarrow PCl_{3(g)} + Cl_2(g)$

# On The Basis of Speed

	Fast Reactions	Slow Reactions
(i)	These reactions are completed in a very short	(i) These reactions take long time to complete.
	interval of time.	
	$HCl + NaOH \rightarrow NaCl + H_2O$	$H_2 + I_2 \rightarrow 2HI$
	Acid Base Salt Water	

#### On The Basis of Heat

	Exothermic Reaction	Endothermic Reaction
(i)	Heat is evolved in these chemical reaction	(i) Heat is absorbed in these chemical reaction
	$R \rightarrow P + x \text{ kcal}$	$R + x \text{ kcal} \rightarrow P$
		or $R \rightarrow P - x \text{ kcal}$
(ii)	Change in enthalpy	(ii) Change in enthalpy
	$\Delta H = (-) \text{ ve}$	$\Delta H = (+) \text{ ve}$
	$\Delta H = -x$	
	Ex.: Formation reaction	Ex. Dissociation reaction
	Exception $N_2 + O_2 \rightarrow 2NO/N_2O/NO_2$	
	$O_2 + F_2 \rightarrow O_2 F_2 / OF_2$	

Active Mass: The term active mass means the concentration of the reactants & products expressed in moles per litre (molar concentration). Active mass is usually expressed by enclosing the symbol of the reactant in square bracket [ ]

Active mass = 
$$\frac{\text{moles}}{\text{Volume in litres}}$$
  
=  $\frac{\text{grams(w)}}{\text{mol.wt.}(M_w) \times \text{Volume in litres(V)}} = \frac{\text{w} \times 1000}{M_w \times \text{V(mL)}}$ 

— The active mass of solids and pure liquids is a constant quantity (unity) and solvent (excess) is considered as one. Because there is no change in activity with the change in quantity or volume of vessel.

$$\begin{aligned} \text{Molar concentration} &= \frac{w}{M_w \times V_{lit.}} = \frac{\rho}{M_w} \; (\rho = \text{density in g/lit}) \\ &= \frac{\text{density of the substance}}{\text{molecular mass of the substance}} \end{aligned}$$

as density of pure solids and liquids is constant and molecular mass is also constant.

But this is not applicable to the substance in aqueous solution or gaseous state because their amount in a given volume can vary.

Following other names of active mass can also be use:

- (i) mole/lit.
- (ii) gram mole/lit.
- (iii) gram molecules/lit.

- (iv) molarity
- (v) Concentration
- (vi) Effective concentration

- (vii) active quantity
- (viii) n/v
- (ix) C

- (x) M
- (xi) []

#### Ex.

(a) 25.4 g of iodine is present in 2 litres of solution

then 
$$[I_2] = \frac{25.4}{254 \times 2} = 0.05$$
 mole/litre

(b) 8.5 g ammonia is present in a vessel of 0.5 litre capacity then

$$[NH_3] = \frac{8.5}{17 \times 0.5} = 1 \text{ mole / litre}$$

(c) Active mass of C (s) or S(s) or Zn(s) is equal to 1.

#### RATE OF REACTION

The change in concentration of reactants or products per mole in unit time is known as rate of the reaction.

$$Rate \ of \ reaction \ = \ \frac{(n) \ change \ in \ concentration \ of \ rectants}{time}$$
 
$$= - \bigg(\frac{dc}{dt}\bigg) \ reactants.$$

Here negative sign indicate that concentration of reactants decrease with time.

Rate of reaction = 
$$+\frac{\text{change in concentration of products}}{\text{time}} = +\left(\frac{\text{dc}}{\text{dt}}\right) \text{ products}$$

#### FACTORS AFFECTING RATES OF REACTIONS

(a) State of Matter: The decreasing order of rate of reaction in gas, liquid and solid state are-

$$g > \ell > s$$

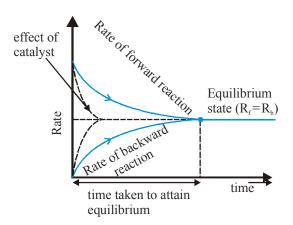
- (b) Temperature: Rate of reaction  $\alpha$  temperature
- (c) Concentration: Rate of reaction  $\alpha$  concentration.
- (d) Catalyst: Positive catalyst increases the rate of reaction.

#### **CHEMICAL EQUILIBRIUM**

The state of the reversible chemical reaction at which rate of forward reaction becomes equal to rate of backward reaction.

$$R_f$$
 $R_f$ 
 $R_b$ 
 $R_b$ 

or The state of the reversible chemical reaction at which the measurable properties of the system like temperature, concentration, colour, density etc. don't undergo any change with time at the given set of conditions is said to be chemical equilibrium conditions. Rate of forward reaction decreases as the concentration of products increases, rate of backward reaction also starts increasing.



At a certain stage, rate of forward reaction becomes equal to rate of backward reaction called equilibrium state.

#### AT EQUILIBRIUM STATE

Rate of forward reaction = Rate of backward reaction

- At this state of equilibrium forward and backward reactions proceeds with same speed.
- The stage of the reversible reaction at which the concentrations of the reactants and products do not change with time is called the equilibrium state.
- The equilibrium state is dynamic in nature.
- The reaction does not stop, but both the opposing reactions are going on continuously with same speeds.

#### **CHARACTERISTICS OF EQUILIBRIUM**

- (a) Chemical equilibrium is dynamic in nature means the reaction, although appears to be stopped, but actually takes place in both the directions with the same speed.
- (b) To obtain equilibrium, if anyone of the reactant or product is in gaseous state then the reaction should be carried out in closed vessel.
- (c) At a given temperature and pressure of equilibrium the properties like concentration, colour, density remains constant.
- (d) In a reversible chemical reaction the equilibrium state can be attained in lesser time by the use of positive catalyst.
  - A catalyst doesn't change the equilibrium state becuase it increases the rate of both forward and backward reaction simultaneously by changing the path of reaction and it helps in attaining equilibrium rapidly.
- (e) In order to prevent escape of products, equilibrium is reached in only in closed vessels in reversible reactions.
- (f) Homogeneous equilibrium is the equilibrium in which the reactants and products are in the same phase.

$$CH_3COOC_2H_5(\ell) + H_2O(\ell) \rightleftharpoons CH_3COOH(\ell) + C_2H_5OH(\ell)$$

(g) Heterogeneous equilibrium is the equilibrium in which the reactants and products are in two or more phases.

$$Zn(s) + CO_2(g) \rightleftharpoons ZnO(s) + CO(g)$$

#### **KEY POINTS**

- (i) Whenever question doesn't ask about direction, then we take forward direction only.
- (ii) In a reversible reaction if forward reaction is exothermic then the backward reaction will be endothermic and vice versa.

#### TYPES OF EQUILIBRIA

There is two types of equilibria:

#### 1. Physical Equilibria

If in a system only physical state (phase) is changed and then equilibrium is established, (i.e. there is no chemical change) the equilibrium is called physical equilibrium.

**Ex.** Fusion of ice, evaporation of water, dissolution of salts and absorption of gases in liquid etc.

Following are the types of common physical equilibria:-

- (i) Liquid-Vapour Equilibria: In a closed vessel, the vapours above the liquid are in equilibrium at given temperature.
- Ex.  $H_2O(\ell) \Longrightarrow H_2O(g)$
- (ii) Solid-Liquid Equilibria: This equilibrium can be established only at melting point of solid. At this stage solid and liquid phases exist simultaneously in equilibrium.
- Ex.  $H_2O(s) \rightleftharpoons H_2O(\ell)$  at melting point
- (iii) (Solute-Solvent), Saturated Solution Equilibria: If the rate of dissolution of solids in liquid is equal to the rate of crystallization of solid from solution i.e. solution is saturated with respect to solid then saturated solution equilibria established, provided temperature is constant.
- NaI (s)  $\stackrel{\text{H}_2\text{O}}{\longleftarrow}$  Na<sup>+</sup> (aq.) + I<sup>-</sup> (aq.)

**Note:** Above example is of solubility of sparingly soluble salt, which only depends on temperature.

- (iv) (Gas + Solvent), Saturated Solution Equilibria: In such equilibriums, solvents is saturated with respect to gas i.e. rate of entering of gas molecules in solvent is equal to rate of escaping of gas molecules from solvents. Above phenomenon can be observed in closed container at definite temperature.
- Ex. Dissolved CO<sub>2</sub> in cold drinks. Dissolved O<sub>2</sub> in water etc.

Note

- (i) The solubilities of gases in liquid is a function of pressure of gas over liquid.
- (ii) Henry's Law can be applied on such system, that states, the mass of gas dissolved in a given mass of solvent at any temperature is proportional to the pressure of the gas above the solvent.

$$\begin{split} C_{g} &\propto P_{g} \quad \text{or} \quad C_{g} = k \; P_{g} \\ \text{where} \qquad & k = \text{Henry's constant} \\ C_{g} &= \text{Solubility of gas in the solution (mol L}^{-1}) \\ P_{g} &= \text{Pressure of the gas} \end{split}$$

(iii) One should not compare it with liquid vapour equilibria.

#### 2. Chemical Equilibria

When chemical change occur in a reversible reaction i.e. reactants convert into products and products also convert into reactants under similar conditions of pressure and temperature, the reaction is said to be in chemical equilibria.

(i) 
$$H_2(g) + I_2(g) \rightleftharpoons 2HI(g)$$
 (formation of HI)

(ii) 
$$SO_2(g) + Cl_2(g) \rightleftharpoons SO_2Cl_2(g)$$
 (formation of  $SO_2Cl_2$ )

(iii) 
$$PCl_3(g) + Cl_2(g) \rightleftharpoons PCl_5(g)$$
 (formation of  $PCl_5$ )

(iv) 
$$2NH_3(g) \rightleftharpoons N_2(g) + 3H_2(g)$$
 (Decomposition of NH<sub>3</sub>)

- Ex. Chemical equilibrium is a condition:
  - (A) where all species have same concentration
  - (B) where all species have constant concentration with respect to time.
  - (C) where all species have concentration = 1
  - (D) all of above
- Sol. (B)

Chemical equilibrium defined as when all species have constant concentration with respect to time.

Example of physical equilibria, is:

$$(A) H_2(g) + I_2(g) \Longrightarrow 2HI(g)$$

(B) 
$$CaCO_3(s) \rightleftharpoons CaO(s) + CO_2(g)$$

$$(\mathbf{C}) \operatorname{H}_{2} \operatorname{O}(s) \Longrightarrow \operatorname{H}_{2} \operatorname{O}(\ell)$$

(D) 
$$PCl_5(g) \rightleftharpoons PCl_3(g) + Cl_2(g)$$

Sol. (C)

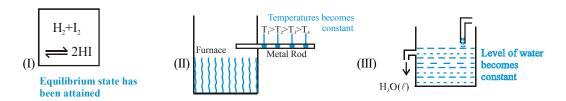
Physical equilibria does not include any chemical change.

- Ex. At equilibrium:
  - (A) the energy of system is minimum
- (B) the entropy of system is maximum
- (C) the energy of system is maximum
- (D) the entropy of system is minimum

**Sol.** (A,B)

It is the compromising stage of minimum energy and maximum entropy.

Ex. Consider the following cases—



The nature of flow of energy in case (I) is same as that in-

(A) II

**(B)** III

(C) II and III

(D) None

**Sol. (D)** None, Because in II and III, the flow of energy or matter is taking place only in one direction. While in equilibrium state, the flow of energy takes place in both directions equally. Thus (I) is a dynamic equilibrium while states in II and III are called steady state (static equilibrium).

### Law of Mass Action or Law of Chemical Equilibrium

The law of mass action is given by Guldberg and Waage.

According to them at a given temperature rate of reaction is proportional to product of active masses of reactants at that instant raised to the powers which are numerically equal to the number of their respective molecule in the stoichiometric equation describing the reaction.

Derivation of Equilibrium Constant

Consider a reversible homogeneous reaction which has attained equilibrium state at particular temperature:

$$A + B \rightleftharpoons C + D$$

Let the active masses of A, B, C and D be [A] [B] [C] & [D] are respectively.

According to Law of Mass Action

rate of forward reaction  $\alpha$  [A] [B]

rate of backward reaction  $\alpha$  [C] [D]

$$R_{\epsilon} = K_{\epsilon}[A][B]$$

$$R_b = K_b[C][D]$$

Where K<sub>f</sub> and K<sub>h</sub> are forward and backward rate constants respectively.

At equilibrium

$$R_{\rm f} = R_{\rm h}$$

$$K_{f}[A][B] = K_{b}[C][D]$$

$$\frac{K_f}{K_h} = \frac{[C][D]}{[A][B]}$$

$$K_{c} = \frac{[C][D]}{[A][B]}$$

$$K_c = \frac{K_f}{K_h}$$

K<sub>c</sub> is known as equilibrium constant K<sub>c</sub> has a definite value for every chemical reaction at particular tempera ture.

For a general reaction

$$m_1A + m_2B + m_3C \rightleftharpoons n_1M + n_2N + n_3O$$

$$r_{_{\rm f}} \propto [A]^{m_1} [B]^{m_2} [C]^{m_3}$$

$$r_f = K_f [A]^{m_1} [B]^{m_2} [C]^{m_3}$$
 [ $K_f =$ forward rate (velocity) constant]

$$r_h \propto [M]^{n_1} [N]^{n_2} [O]^{n_3}$$

$$r_b = K_b [M]^{n_1} [N]^{n_2} [O]^{n_3}$$
 [ $K_b = backward rate (velocity) constant]$ 

At equilibrium 
$$r_r = r$$

$$K_{f}[A]^{m_{1}}[B]^{m_{2}}[C]^{m_{3}} = K_{h}[M]^{n_{1}}[N]^{n_{2}}[O]^{n_{3}}$$

$$K_{c} = \frac{K_{f}}{K_{b}} = \frac{[M]^{n_{1}}[N]^{n_{2}}[O]^{n_{3}}}{[A]^{m_{1}}[B]^{m_{2}}[C]^{m_{3}}}$$

The equilibrium constant, at a given temperature, is the ratio of the rate constants of forward and backward reactions.

Write down the equilibrium constant for the following reactions. Ex.

(a) 
$$N_2 + 3H_2 \rightleftharpoons 2NH_3$$

(b) 
$$PCl_5 \rightleftharpoons PCl_3 + Cl_7$$

(c) 
$$3A + 2B \rightleftharpoons C + 4D$$

(d) 
$$CaCO_3(s) \rightleftharpoons CaO(s) + CO_2(g)$$

(e) 
$$2KClO_3(s) \rightleftharpoons 2KCl(s) + 3O_3(g)$$

(f) 
$$CH_3COOH(\ell) + C_3H_5OH(\ell) \rightleftharpoons CH_3COOC_3H_5(\ell) + H_3O(\ell)$$

(g) 
$$NH_3(aq) + H_2O \rightleftharpoons NH_4^+(aq) + OH^-(aq)$$

(h) 
$$H_2O(\ell) \rightleftharpoons H_2O(g)$$

**Ans.** (a) 
$$K = \frac{[NH_3]^2}{[N_2][H_2]^3}$$

(b) 
$$K = \frac{[PCl_3][Cl_2]}{[PCl_5]}$$

(c) 
$$K = \frac{[C][D]^4}{[A]^3[B]^2}$$

(d)  $K = [CO_2]$  (Active mass of solid is 1)

(e) 
$$K = [O_2]^3$$

(f) 
$$K = \frac{\left[CH_3COOC_2H_5\right]\left[H_2O\right]}{\left[CH_3COOH\right]\left[C_2H_5OH\right]} \text{ (here } H_2O \text{ is not in excess)}$$

(g) 
$$K = \frac{\left[NH_4^+\right]\left[OH^-\right]}{\left[NH_3\right]}$$
 (here  $H_2O$  is in excess (solvent) so its concentration doesn't change.)

(h) 
$$K = [H_2O]_{(g)}$$

$$[0 < K < \infty]$$

When K = 1

[Product] = [Reactant]

When K > 1

[Product] > [Reactant]

When K < 1

[Product] < [Reactant]

As K  $\uparrow$  stability of products  $\uparrow$  stability of reactant  $\downarrow$  time to attain equilibrium  $\downarrow$  $t \propto 1/K$ 

Stability of reactants and products

$$2XO(g) \rightleftharpoons X_2(g) + O_2(g);$$

$$K_1 = 1 \times 10^{24}$$

$$2XO_2(g) \rightleftharpoons X_2(g) + 2O_2(g);$$

$$K_2 = 2.5 \times 10^{10}$$

$$K_1 > K$$

 $K_1 > K_2$  So the stability of  $XO_2 > XO$ 

For reactants, stability increases when value of K decreases.

For products, stability increases when value of K increases.

(more is the value of equilibrium constant, more is the formation of product means more is the stability of product.) Time taken to attain equilibrium increases when value of K decreases.

### Forms of Equilibrium Constant

There are two forms.

(i) Concentration form (K<sub>c</sub>)

(ii) Partial pressure form (K<sub>p</sub>)

**Partial Pressure :** The individual pressure exerted by the gases substance of the total pressure is called partial pressure of the gases substance.

$$\begin{array}{c|cccc} & & & & & & & & \\ Gaseous & A & B & C & D \\ moles & n_1mol & n_2mol & n_3mol & n_4mol & \\ \end{array} \Rightarrow P_{\tiny total}$$

$$\begin{aligned} \text{Partial pressure} &= \frac{\text{Moles of substance}}{\text{Total moles}} \times P_{\text{total}} \\ &= \text{mole fraction} \times P_{\text{total}} \end{aligned} \Rightarrow \boxed{ \begin{bmatrix} \frac{\text{Moles of substance}}{\text{Total moles}} = \text{Mole fraction} \end{bmatrix}}$$

let 
$$n_1 + n_2 + n_3 + n_4 = N$$

$$\begin{split} P_{A} &= \frac{n_{1}}{N} P_{t} \,, \qquad \qquad P_{B} = \frac{n_{2}}{N} P_{t} \,, \qquad \qquad P_{C} = \frac{n_{3}}{N} P_{t} \,, \qquad \qquad P_{D} = \frac{n_{4}}{N} P_{t} \\ P_{A} &+ P_{B} + P_{C} + P_{D} = P_{total} \end{split}$$

Ex. A vessel contains 5 mole of A & 10 moles of B. If total pressure is 18 atm. Find out partial pressure of gases.

Sol. 
$$P_A = \frac{5}{15} \times 18 = 6 \text{ atm}$$
  
 $P_B = \frac{10}{15} \times 18 = 12 \text{ atm}$ 

When the reactants and products are in gaseous state then partial pressure can be used instead of concentration. At a definite temperature, as the partial pressure of a substance is proportional to its concentration in the gas phase.

$$m_1 A + m_2 B \rightleftharpoons n_1 C + n_2 D$$

If partial pressure of A, B, C and D at equilibrium are  $P_A$ ,  $P_B$ ,  $P_C$  and  $P_D$  respectively, then

$$K_{P} = \frac{\left(P_{c}\right)^{n_{1}} \times \left(P_{D}\right)^{n_{2}}}{\left(P_{A}\right)^{m_{1}} \times \left(P_{B}\right)^{m_{2}}}$$

## Relation Between K<sub>p</sub> and K<sub>C</sub>

This relation can be established for reaction not involving liquids because kp is not defined for liquids.

Consider a reversible reaction

$$m_1A + m_2B \iff n_1C + n_2D$$

$$K_{C} = \frac{[C]^{n_{1}}[D]^{n_{2}}}{[A]^{m_{1}}[B]^{m_{2}}}$$

$$K_{P} = \frac{(P_{C})^{n_{I}}(P_{D})^{n_{2}}}{(P_{A})^{m_{I}}(P_{B})^{m_{2}}}$$

For an ideal gas PV=nRT

$$P = \frac{n}{V} RT = active mass \times RT$$

n = number of mole and V = Volume in litre

 $\frac{n}{v}$  = molar concentration or active mass So

$$P = []RT$$

at constant temperature  $P \propto []$ 

$$P = [A] RT$$

$$P_A = [A] RT, \qquad P_B = [B] RT,$$

$$P_C = [C] RT$$

$$P_C = [C] RT, \qquad P_D = [D] RT$$

So 
$$K_p = \frac{[C]^{n_1} (RT)^{n_1} [D]^{n_2} (RT)^{n_2}}{[A]^{m_1} (RT)^{m_1} \times [B]^{m_2} (RT)^{m_2}}$$

$$K_{p} = \frac{\left[C\right]^{n_{l}} \left[D\right]^{n_{2}}}{\left[A\right]^{m_{l}} \left[B\right]^{m_{2}}} \times \frac{\left(RT\right)^{n_{1}+n_{2}}}{\left(RT\right)^{m_{1}+m_{2}}}$$

$$K_{P} = K_{C} (RT)^{(n_{1}+n_{2})-(m_{1}+m_{2})}$$

$$\Delta n = (n_1 + n_2) - (m_1 + m_2)$$

= total number of gaseous molecules of products – total number of gaseous molecules of reactants.

$$K_P = K_C (RT)^{\Delta n_g}$$

Find the values of  $K_c$  for each of the following equilibria from the value of  $K_p$ . Ex.

(a) 
$$2NOCl(g) \rightleftharpoons 2NO(g) + Cl_2(g)$$
  $K_n = 1.8 \times 10^{-2} \text{ at } 600 \text{ K}$ 

$$K = 1.8 \times 10^{-2} \text{ at } 600 \text{ K}$$

(b) 
$$CaCO_3(g) \rightleftharpoons CaO(s) + CO_2(g)$$

$$K_p = 167 \text{ at } 1173 \text{ K}$$

(a)  $2NOCl(g) \rightleftharpoons 2NO(g) + Cl_2(g)$ Sol.

$$K_p = 1.8 \times 10^{-2}$$

$$\Delta n_{_{o}} = 3 - 2 = 1$$

$$K_{\rm p} = K_{\rm c} (RT)^{\Delta n_{\rm g}}$$

$$\therefore K_{c} = \frac{K_{p}}{RT} = \frac{1.8 \times 10^{-2}}{0.0821 \times 600} = 3.65 \times 10^{-4}$$

(b)  $K_n = 167$ 

$$\Delta n_{\alpha} = 1$$

$$K_p = K_c (RT)^{\Delta n_g} = K_c \times (RT)$$

$$\therefore K_{c} = \frac{K_{p}}{RT} = \frac{167}{0.0821 \times 1173} = 1.734$$

Ex. At 540 K, 0.10 moles of PCl<sub>5</sub> are heated in 8 litre flask. The pressure of the equilibrium mixture is found to be 1.0 atm. Calculate  $K_p$  and  $K_c$  for the reaction.

Sol.  $PCl_{5}(g) \rightleftharpoons PCl_{3}(g) + Cl_{2}(g)$ 

- 0.1
- X
- (0.1-x)
- X

$$K_c = \frac{[PCl_3][Cl_2]}{[PCl_5]} = \frac{\frac{x}{8} \times \frac{x}{8}}{\left(\frac{0.1 - x}{8}\right)} = \frac{x^2}{8(0.1 - x)}$$
 .....(i)

From gas law

PV = nRT

$$\Rightarrow$$
 1 × 8 = (0.1 + x) × 0.082 × 540

From eqs. (i) and (ii)

$$K_c = \frac{0.08 \times 0.08}{8 \times (0.1 - 0.08)} = 4 \times 10^{-2} \text{ mol L}^{-1}$$

$$K_p = K_c (RT)^{\Delta n_g}$$
  $(\Delta n_g = +1)$   
=  $4 \times 10^{-2} \times (0.082 \times 540) = 1.77 \text{ atm}$ 

- At a given temperature and a total pressure of 1.0 atm for the homogeneous gaseous reaction,  $N_2O_4 \rightleftharpoons 2NO_2$ , the partial pressure of  $NO_2$  is 0.5 atm.
  - (a) Calculate the value of  $K_{n}$ .
  - (b) If the volume of the vessel is decreased to half of its original volume, at constant temperature, what are the partial pressures of the components of the equilibrium mixture?
- Sol. For equilibrium system,  $N_2O_4 \rightleftharpoons 2NO_2$ , the total pressure is 1.0 atm
  - $\Rightarrow$  The total pressure =  $P_{N_2O_4} + P_{NO_2} = 1$
  - $\Rightarrow$   $P_{N_2O_4} = 0.5$  atm and  $P_{NO_2} = 0.5$  atm

(i) 
$$K_p = \frac{(P_{NO_2})^2}{P_{N,O_4}} = \frac{(0.5)^2}{0.5} = 0.5 \text{ atm}$$

(ii) As volume is decreased to half its original volume, equilibrium is disturbed and the new initial conditions for the re-establishment of new equilibrium are

$$P_{N_2O_4} = 1.0 \text{ atm and } P_{NO_2} = 1.0 \text{ atm}$$

According to Le Chatelier's principal, when volume is decreased, the system moves in that direction where there is decrease in number of moles. Hence, the system (here will moves in reverse direction, as there is a decrease in mole ( $\Delta n = 2 - 1 = 1$ ), i.e.  $NO_2$  will be converted into  $N_2O_4$ .

Let, the decrease in pressure of NO<sub>2</sub> be x atm.

$$\begin{array}{ccc} & N_2O_4 & \Longrightarrow & 2NO_2 \\ \text{Initial pressure (atm)} & 1.0 & 1.0 \\ \text{At equilibrium} & 1+x/2 & 1-x \\ \end{array}$$

$$\Rightarrow K_p = \frac{(1-x)^2}{(1+x/2)} = 0.5 \Rightarrow 4x^2 - 9x + 2 = 0$$

 $\Rightarrow$  x = 2 or 0.25 (x  $\neq$  2 as initial pressure = 1.0)  $\Rightarrow$  x = 0.25

$$P_{N_2O_4} = 1 + \frac{x}{2} = 1.125 \text{ atm and } P_{NO_2} = 1 - x = 0.75 \text{ atm}$$

Ex. At temperature T, a compound  $AB_2(g)$  dissociates according to the reaction,  $2AB_2(g) \rightleftharpoons 2AB(g) + B_2(g)$  with degree of dissociation  $\alpha$ , which is small compared to unity. Deduce the expression for  $\alpha$  in terms of the equilibrium constant  $K_p$  and the total pressure P.

Sol. 
$$2AB_2(g) \Longleftrightarrow 2AB(g) + Br_2(g)$$
 Initial (mole) 
$$1 \qquad 0 \qquad 0$$
 At eq. (mole) 
$$1 - \alpha \qquad \alpha \qquad \alpha/2 \qquad \text{Total moles at equilibrium} = (1 + \alpha/2)$$
 At eq. (p.p) 
$$P\left(\frac{1-\alpha}{1+\alpha/2}\right) \qquad \frac{P.\alpha}{1+\alpha/2} \qquad \frac{P.\alpha/2}{(1+\alpha/2)}$$

$$K_{p} = \frac{P_{AB}^{2} P_{Br^{2}}}{P_{AB_{2}}^{2}}$$

$$K_{p} = \frac{\left(\frac{P.\alpha}{1+\alpha/2}\right)^{2} \left(\frac{P.\alpha/2}{1+\alpha/2}\right)}{P^{2} \left(\frac{1-\alpha}{1+\alpha/2}\right)^{2}} \Rightarrow K_{p} = \frac{P\alpha^{3}}{2(1-\alpha)^{2}(1+\alpha/2)}$$

But 
$$1 >> \alpha$$
 ::  $K_p = \frac{P\alpha^3}{2}$ 

$$\alpha = \left(\frac{2K_p}{P}\right)^{1/3}$$

The  $K_C$  is expressed by the units (mole lit<sup>-1</sup>)<sup> $\Delta n$ </sup> and  $K_P$  by (atm)<sup> $\Delta n$ </sup>. In terms of mole fraction, equilibrium constant is denoted by  $K_X$ .

For general reaction  $aA + bB \rightleftharpoons mC + nD$ 

$$K_{X} = \frac{(X_{C})^{m} (X_{D})^{n}}{(X_{A})^{a} (X_{B})^{b}}$$

$$K_{p} = K_{x} (RT)^{\Delta n_{g}} \qquad ......(i)$$

$$\Delta n_{g} = (m+n) - (a+b)$$
When  $\Delta n_{g} = 0$ ,  $K_{p} = K_{C} = K_{x}$ 

#### **CALCULATION OF EQUILIBRIUM CONSTANT**

(a) 
$$H_2(g) + I_2(g) \rightleftharpoons$$
 2HI (g) Initially a b 0 0
At equilibrium  $(a-x)$   $(b-x)$   $2x$ 

$$K_c = \frac{[HI]^2}{[H_2][I_2]} = \frac{(2x)^2}{(a-x)(b-x)} = \frac{4x^2}{(a-x)(b-x)}$$

$$K_{p} = \frac{(p_{HI})^{2}}{p_{H_{2}} \times p_{I_{2}}} = \frac{\frac{(2x)^{2}}{(a+b)^{2}}P^{2}}{\left(\frac{a-x}{a+b}.P\right)\left(\frac{b-x}{a+b}.P\right)} = \frac{4x^{2}}{(a-x)(b-x)}$$

So 
$$K_c = K_n$$
  $(\Delta n = 0)$ 

$$K_c = \frac{[N_2][O_2]}{[NO]^2} = \frac{x/2 \times x/2}{(a-x)^2} = \frac{x^2}{4(a-x)^2} = K_p$$
 ( $\Delta n = 0$ )

(c) 
$$\begin{array}{cccc} CH_3COOH_{(\ell)} + C_2H_5OH_{(\ell)} & \Longrightarrow & CH_3COOC_2H_{5(\ell)} + H_2O_{(\ell)} \\ Initially & a & b & 0 & 0 \\ At equilibrium & (a-x) & (b-x) & x & x \end{array}$$

$$K_c = \frac{[CH_3COOC_2H_5][H_2O]}{[CH_3COOH][C_2H_5OH]} = \frac{x^2}{(a-x)(b-x)}$$

K<sub>n</sub> should not be given for this reaction

(d) 
$$\operatorname{PCl}_{5}(g) \longrightarrow \operatorname{PCl}_{3}(g) + \operatorname{Cl}_{2}(g)$$

$$\begin{array}{cccc} \text{(d)} & & \text{PCl}_5(\text{g}) & & \longrightarrow & \text{PCl}_3(\text{g}) + \text{Cl}_2(\text{g}) \\ \text{Initially} & \text{a} & & 0 & 0 \\ \text{At equilibrium} & & \text{(a-x)} & & x & x \\ \end{array}$$

Active mass 
$$\frac{(a-x)}{v}$$
  $\frac{x}{v}$   $\frac{x}{v}$ 

$$K_{c} = \frac{[PCl_{3}][Cl_{2}]}{[PCl_{5}]} = \frac{\frac{x}{v} \times \frac{x}{v}}{\frac{(a-x)}{v}} = \frac{x^{2}}{(a-x)v}$$

$$K_{p} = \frac{p_{PCl_{3}} \times p_{Cl_{2}}}{p_{PCl_{5}}} = \frac{\left(\frac{x}{a+x}.P\right) \times \left(\frac{x}{a+x}.P\right)}{\left(\frac{a-x}{a+x}\right)P} = \frac{x^{2}P}{(a+x)(a-x)} = \frac{x^{2}P}{a^{2}-x^{2}}$$

(e) 
$$N_2(g) + 3H_2(g) \rightleftharpoons 2NH_3(g)$$

At equilibrium 
$$(a-x)$$
  $(b-3x)$   $2x$ 

Active mass 
$$\frac{(a-x)}{v}$$
  $\left(\frac{b-3x}{v}\right)$   $\left(\frac{2x}{v}\right)$ 

$$K_{c} = \frac{[NH_{3}]^{2}}{[N_{2}][H_{2}]^{3}} = \frac{\left(\frac{2x}{v}\right)^{2}}{\left(\frac{a-x}{v}\right)\left(\frac{b-3x}{v}\right)^{3}} = \frac{4x^{2}V^{2}}{(a-x)(b-3x)^{3}}$$

$$K_{p} = \frac{(p_{NH_{3}})^{2}}{p_{N_{2}} \times (p_{H_{2}})^{3}} = \frac{\left[\frac{2xP}{a+b-2x}\right]^{2}}{\left[\frac{(a-x)P}{(a+b-2x)}\right]\left[\frac{(b-3x)P}{(a+b-2x)}\right]^{3}} = \frac{4x^{2}(a+b-2x)^{2}}{(a-x)(b-3x)^{3}P^{2}}$$

In the reaction,  $H_2(g) + I_2(g) \Longrightarrow 2HI(g)$  the concentration of  $H_2$ ,  $I_2$  and HI at equilibrium are 10.0, 6.0 and 28 moles per litre respectively. What will be the equilibrium constant?

- (A) 30.61
- **(B)** 13.066
- (C) 29.40
- (D) 20.90

Sol. (B)

$$H_2(g) + I_2(g) \Longrightarrow 2HI(g)$$

Applying law of mass action,

$$K_c = \frac{[HI]^2}{[H_2][I_2]}$$

Given

$$[H_2] = 10 \text{ mol } L^{-1}$$

$$[I_2] = 6.0 \text{ mol } L^{-1}$$

$$[HI] = 28.0 \, \text{mol L}^{-1}$$

$$K_c = \frac{(28.0)^2}{(10) \times (6.0)} = 13.066$$

For a gas phase reaction at equilibrium,

 $3H_2(g) + N_2(g) \rightleftharpoons 2NH_3(g)$ , the partial pressures of  $H_2$  and  $N_2$  are 0.4 and 0.8 atmosphere respectively. The total pressure of the entire system is 2.4 atmosphere. What will be the value of  $K_p$  if all the pressures are given in atmosphere?

- (A)  $32 \text{ atm}^{-2}$
- **(B)**  $20 \text{ atm}^{-2}$
- (C) 28.125 atm<sup>-2</sup>
- **(D)**  $80 \text{ atm}^{-2}$

Sol. (C)

$$N_2(g) + 3H_2(g) \rightleftharpoons 2NH_3(g),$$

Partial pressures at equilibrium

$$[2.4 - (0.8 + 0.4) = 1.2]$$

Applying law of mass action,

$$K_{p} = \frac{[P_{NH_{3}}]^{2}}{[P_{N_{2}}][P_{H_{2}}]^{3}} = \frac{1.2 \times 1.2}{0.8 \times 0.4 \times 0.4 \times 0.4} \implies K_{p} = 28.125 \text{ atm}^{-2}$$

When ethanol and acetic acid were mixed together in equilimolecular proportion 66.6% are converted into ethyl acetate. Calculate K<sub>c</sub>. Also calculate quantity of ester produced if one mole of acetic acid is treated with 0.5 mole and 4 mole of alcohol respectively.

- (A) 4, 0.93, 0.43
- **(B)** 0.93, 4, 0.43
- **(C)** 0.43, 0.93, 4
- **(D)** 4, 0.43, 0.93

Sol. (D)

$$\operatorname{CH_3COOH} + \operatorname{C_2H_5OH} \Longrightarrow \operatorname{CH_3COOC_2H_5} + \operatorname{H_2O}$$

1 1

0

0

1-0.666 1-0.666

0.666 0.666

$$K_c = \frac{[CH_3COOC_2H_5][H_2O]}{[CH_3COOH][C_2H_5OH]} = \frac{[0.666][0.666]}{[0.333][0.333]} = 4$$

(A) Let x moles of ester is formed from 1 mole of acid and 0.5 mole of alcohol, then

$$K_c = \frac{x^2}{(1-x)(0.5-x)} \Rightarrow \frac{x^2}{(1-x)(0.5-x)} = 4 \Rightarrow x = 0.43$$

**(B)** 
$$K_c = \frac{x^2}{(1-x)(4-x)}$$
 or  $4 = \frac{x^2}{(1-x)(4-x)}$   $\Rightarrow x = 0.93$ 

Ex. Starting with 3:1 mixture of H, and N, at 450°C, the equilibrium mixture is found to be 9.6% NH<sub>3</sub>; 22.6% N, and 67.8 % H, by volume. The total pressure is 50 atm. What will be the value of  $K_{\rm p}.$  The reaction is -

$$N_2 + 3H_2 \rightleftharpoons 2NH_3$$

- (A)  $3.25 \times 10^{-5}$  atm<sup>-2</sup>
- **(B)**  $5.23 \times 10^{-5} \text{ atm}^{-2}$  **(C)**  $6.23 \times 10^{-5} \text{ atm}^{-2}$
- (D)  $8 \times 10^{-5} \text{ atm}^{-2}$

Sol.

The ratio of number of moles will be the same as the ratio of volume. According to Dalton's law, the partial pressure of a gas in a mixture is given by the product of its volume fraction and the total pressure. Therefore, the equilibrium pressure of each gas is,

$$P_{NH_3} = \frac{9.6}{100} \times 50$$
 atm = 4.8 atm

$$P_{N_2} = \frac{22.6}{100} \times 50 \text{ atm} = 11.3 \text{ atm}$$

$$P_{H_2} = \frac{67.6}{100} \times 50 \text{ atm} = 33.9 \text{ atm}$$

Total pressure = 50 atm

 $K_p = \frac{[P_{NH_3}]^2}{[P_{N_1}][P_{N_2}]^3}$ ; Substituting the values of partial pressures,

$$K_p = \frac{(4.80 \text{ atm})^2}{(11.3 \text{ atm})(33.9 \text{ atm})^3} = 5.23 \times 10^{-5} \text{ atm}^{-2}$$

 $K_p$  for the reaction  $A(g) + 2B(g) \Longrightarrow 3C(g) + D(g)$ ; is 0.01 atm. What will be its  $K_g$  at 1000 K in terms of R? Ex.

- (A)  $\frac{1.0 \times 10^{-5}}{R}$  (B)  $\frac{R}{5 \times 10^{-5}}$  (C)  $5 \times 10^{-5}$ R
- (D) none of these

Sol.

We know that

$$K_p = K_c (RT)^{\Delta n}$$
 or  $K_c = \frac{K_p}{(RT)^{\Delta n}}$ 

Here  $\Delta n = 4 - 3 = 1$ 

$$T = 1000 \text{ K}, K_p = 0.01$$

$$K_c = \frac{0.01}{(R \times 1000)^T} = \frac{1.0 \times 10^{-5}}{R}$$

- Ex. 0.5 mole of  $H_2$  and 0.5 mol of  $I_2$  react in 200 L flask at 448° C. The equilibrium constant  $K_c$  is 50 for  $H_2 + I_2 \Longrightarrow 2HI$ ,
  - (a) What is the  $K_p$ ?
  - (b) Calculate mol of I<sub>2</sub> at equilibrium.
- Sol.  $H_2 + I_2 \Longrightarrow 2HI$ 0.5 0.5 0 Initial (0.5-x) (0.5-x) 2x at equili.
  - (a) Since  $\Delta n = 0 \Rightarrow K_p = K_c$

(b) 
$$50 = \frac{4x^2}{(0.5 - x)^2}$$
 or  $\frac{2x}{0.5 - x} = \sqrt{50}$ 

$$x = 0.39$$

- $\therefore$  mol of I<sub>2</sub> = 0.5 0.39 = 0.11 mol
- Three cases may arise:
- (a) When  $\Delta n = 0$   $K_p = K_C (RT)^0 = K_C$ For example :

$$N_2 + O_2 \Longrightarrow 2NO$$
  $H_2 + I_2 \Longrightarrow 2HI$ 

- $K_C$  and  $K_P$  are unit less in this case.
- (b) When  $\Delta n = +ve$   $K_p > K_C$ For example:

$$PCl_{5} \iff PCl_{3} + Cl_{2} \qquad \begin{pmatrix} K_{C} \rightarrow \text{mole lit}^{-1} \\ K_{P} \rightarrow \text{atm} \end{pmatrix}$$

$$(\Delta n = 1)$$

$$2NH_{3} \iff N_{2} + 3H_{2} \qquad \begin{pmatrix} K_{C} \rightarrow mole^{2} lit^{-2} \\ K_{P} \rightarrow atm^{2} \end{pmatrix}$$

$$(\Delta n = 2)$$

(c) When 
$$\Delta n = -ve$$

$$K_p < K_C$$

$$N_2 + 3H_2 \Longrightarrow 2NH_3 \qquad \begin{pmatrix} K_C \to mole^{-2} lit^2 \\ K_P \to atm^{-2} \end{pmatrix}$$

$$(\Delta n = -2)$$

# **Factors Affecting Equilibrium Constant**

(a) Mode of Representation of The Reaction

$$A + B \rightleftharpoons C + D$$

The equilibrium constant for the reaction

$$K_{C} = \frac{[C][D]}{[A][B]}$$

If the reaction is reversed

$$C+D \Longrightarrow A+B$$

$$K_{c}^{1} = \frac{A \cdot B}{C \cdot D}$$

The two equilibrium constant related as  $\rightarrow K_c = \frac{1}{K_c^1}$ 

For  $N_2 + 3H_2 \rightleftharpoons 2NH_3$  if  $K_C = 5$  then find  $K_C'$  for reverse reaction.

**Ans.** 
$$K_C' = 1/5 = 0.2$$

#### (b) Stoichiometry of The Reaction

When a reversible reaction can be written with the help of two or more stoichiometric equation, the value of equilibrium constant will be numerically different.

For reaction

$$2NO_2 \rightleftharpoons N_2 + 2O_2$$

$$K_{C} = \frac{\left[N_{2}\right]\left[O_{2}\right]^{2}}{\left[NO_{2}\right]^{2}}$$

For reaction  $NO_2 \iff \frac{1}{2}N_2 + O_2$ 

$$K_{c}^{1} = \frac{\left[N_{2}\right]^{\frac{1}{2}}\left[O_{2}\right]}{\left[NO_{2}\right]}$$

The two constants are related as  $\,K_{\,c}^{1}=\sqrt{\!K_{\,C}}$ 

(c) Temperature: The value of equilibrium constant changes with the change of temperature.

If  $K_1$  and  $K_2$  be the equilibrium constants of a reaction at absolute temperatures  $T_1$  and  $T_2$  and  $\Delta H$  is the heat of reaction at constant volume, then :

$$\frac{d(\ell nk)}{dT} = \frac{\Delta H}{RT^2}$$

$$\log \frac{K_2}{K_1} = \log K_2 - \log K_1 = \frac{-\Delta H}{2.303R} \left[ \frac{1}{T_2} - \frac{1}{T_1} \right]$$
 (According to Vant Hoff equation)

(i)  $\Delta H = 0$  (neither heat is absorbed or evolved)

$$\log K_2 - \log K_1 = 0$$

$$\log K_1 = \log K_2$$

$$K_1 = K_2$$

Thus, equilibrium constant remains the same at all temperatures

If temp.  $T_2$  is higher than  $T_1$ 

$$\frac{1}{T_2} - \frac{1}{T_1} < 0 \text{ , } \log K_2 - \log K_1 = \frac{+ve\Delta H}{2.303R}$$

(ii) When  $\Delta H = +ve$  (endothermic reaction)

$$\log K_2 - \log K_1 > 0$$

or 
$$\log K_2 > \log K_1$$

$$K_2 > K_1$$

The value of equilibrium constant is higher at higher temperature in case of endothermic reactions.

$$K_C \propto T$$

When  $\Delta H = -ve$  (exothermic reaction) (iii)

$$\log K_2 - \log K_1 < 0$$
$$\log K_2 < \log K_1$$
$$K_2 < K_1$$

The value of equilibrium constant is lower at higher temperature in the case of exothermic reactions.

$$K_C \propto 1/T$$

The value of equilibrium constant is independent of the following factors:-

- Initial concentrations of reactants.
- (b) The presence of a catalyst.
- The direction from which the equilibrium has been attained. (c)
- (d) Presence of inert materials.
- Ex. For the reaction,

A  $\Longrightarrow$  B,  $\triangle$ H for the reaction is -33.0 kJ/mol.

Calculate:

- (i) Equilibrium constant K<sub>c</sub> for the reaction at 300 K
- (ii) If  $E_a(f)$  and  $E_a(r)$  in the ratio of 20 : 31, calculate  $E_a(f)$  and  $E_a(r)$  at 300 K.

Assuming pre-exponential factor same for forward and reverse reaction.

**Sol.** (i) 
$$\Delta H = E_{a(f)} - E_{a(r)} = -33 \text{ kJ}$$

$$k_f^- = Ae^{-E_{a(f)}/RT}$$

$$k_b = Ae^{-E_{a(r)/RT}}$$

$$\therefore \quad k_c = \frac{k_f}{k_b} = e^{\left[E_{a(f)} - E_{a(r)}\right]/RT} \Longrightarrow e^{\frac{33 \times 10^3}{8.314 \times 300}} = 5.572 \times 10^5 \, \text{at } 300 \, \text{K}$$

(ii) 
$$\frac{E_{a(f)}}{E_{a(f)}} = \frac{20}{31}$$
  $E_{a(f)} - E_{a(r)} = -33kJ$ 

$$E_{a(f)} - E_{a(r)} = -33kJ$$

$$\therefore E_{a(r)} - \frac{31}{20} \times E_{a(f)} = -33kJ$$

$$\therefore E_{a(f)} = \frac{33 \times 20}{11} = 60 \text{kJ}$$

$$E_{a(r)} = +93 \text{ kJ}$$



Progress of

- The equilibrium constant for the reaction  $H_2(g) + S(s) \rightleftharpoons H_2S(g)$ ; is 18.5 at 925 K and 9.25 at 1000 K Ex. respectively. The enthalpy of the reaction will be:
  - $(A) 68000.05 \,\mathrm{J} \,\mathrm{mol}^{-1}$
- **(B)**  $-71080.57 \,\mathrm{J}\,\mathrm{mol}^{-1}$
- (C)  $-80071.75 \,\mathrm{J}\,\mathrm{mol}^{-1}$  (D)  $57080.75 \,\mathrm{J}\,\mathrm{mol}^{-1}$

Sol. **(B)** 

Using the relation,

$$\log \frac{K_2}{K_1} = \frac{\Delta H}{2.303R} \left[ \frac{T_2 - T_1}{T_1 T_2} \right]$$

$$\log \frac{9.25}{18.5} = \frac{\Delta H}{2.303 \times 8.314} \times \frac{75}{925 \times 1000}$$

$$-0.301 = \frac{\Delta H \times 75}{2.303 \times 8.314 \times 925 \times 1000} \implies \Delta H = -71080.57 \text{ J mol}^{-1}.$$

- Ex. The reaction CuSO<sub>4</sub>.3H<sub>2</sub>O(s)  $\rightleftharpoons$  CuSO<sub>4</sub>.H<sub>2</sub>O(s)+2H<sub>2</sub>O (g); the dissociation pressure is  $7 \times 10^{-3}$  atm at 25°C and  $\Delta$ H° = 2750 cal. What will be the dissociation pressure at 127°C?
- **Sol.** For given reaction

$$K_p = (p_{H_2O})^2$$
  
so  $K_p (25^{\circ}C) = (7 \times 10^{-3})^2 \text{atm}^2$   
 $= 4.9 \times 10^{-5} \text{atm}^2$ 

Since  $\Delta H^{\circ} = 2750$  cal, so using Vant Hoff eq.

$$log\!\left[\frac{K_{_{P}}(127^{\circ}C)}{K_{_{P}}(25^{\circ}C)}\right]\!=\!\frac{\Delta H^{\circ}}{2.303\!\times\!R}\left[\frac{400-298}{400\!\times\!298}\right]$$

$$\log\left[\frac{K_{P}(127^{\circ}C)}{4.9\times10^{-5}}\right] = \frac{2750}{2.303\times2} \left[\frac{102}{119200}\right]$$

$$K_p(127^{\circ}C) = 3.2426 \times 4.9 \times 10^{-5} = 1.58 \times 10^{-4}$$

so 
$$p_{H_2O}$$
 at  $127^\circ = \sqrt{K_p(127^\circ C)} = \sqrt{1.58 \times 10^{-4}} = 1.26 \times 10^{-2}$  atm.

### Law of Mass Action as Applied to Heterogeneous Equilibrium

In such cases the active mass of pure solid and pure liquid is taken as unity and the value of equilibrium constant is determined by the gaseous substances only.

For Example: The dissociation of CaCO<sub>3</sub> in closed vessel.

$$CaCO_3(s) \rightleftharpoons CaO(s) + CO_2(g)$$

$$K_{C} = [CO_{2}], K_{p} = p_{CO_{2}}$$

$$PCl_s(s) \Longrightarrow PCl_s(\ell) + Cl_s(g)$$

$$K_{C} = [Cl_{2}], \qquad K_{p} = p_{Cl_{2}}$$

$$2H_2O(\ell) \Longrightarrow 2H_2(g) + O_2(g)$$

$$K_C = [H_2]^2 [O_2], K_P = (p_{H_2})^2 (p_{O_2})$$

$$3Fe(s) + 4H_2O(g) \rightleftharpoons Fe_3O_4(s) + 4H_2(g)$$

$$K_{C} = \frac{[H_{2}]^{4}}{[H_{2}O]^{4}}, K_{P} = \frac{(p_{H_{2}})^{4}}{(p_{H_{2}O})^{4}}$$

Ex. One mole of ammonium carbamate dissociate as shown below at 500 K.

$$NH_2COONH_4(s) \rightleftharpoons 2NH_3(g) + CO_2(g)$$

If the pressure exerted by the released gases is 6.0 atm, the value of  $K_p$  is -

- (A) 7 atm
- **(B)** 3 atm
- (C) 32 atm
- (D) 8 atm

Sol. (C

Applying the law of chemical equilibrium, we get

$$K_p = (P_{NH_3})^2 (P_{CO_2})$$

Since total pressure is 6 atm, the partial pressures of NH<sub>3</sub> (g) and CO<sub>2</sub> (g) are

$$(P_{NH_3}) = 6 \times \frac{2}{3} = 4 \text{ atm}$$

$$(P_{CO_2}) = 6 \times \frac{1}{3} = 2 \text{ atm}$$

$$K_n = [4.0]^2 [2.0] = 32.0 \text{ atm}$$

**Ex.** For the reaction.

 $CaCO_3$  (s)  $\rightleftharpoons$  CaO (s) +  $CO_2$  (g);  $K_p = 1.16$  atm. at 800°C. If 40 g of  $CaCO_3$  was put into a 20 L container and heated to 800°C, what percent of  $CaCO_3$  would remain unreacted at equilibrium.

**Sol.**  $K_p = P_{CO_2} = 1.16 \text{ atm}$ 

$$n(CO_2) = PV/RT = \frac{1.16 \times 20}{0.0821 \times 1073} = 0.26335 \text{ mol}$$

moles of CaCO3 initially present

$$=40/100=0.4 \text{ mol}$$

So % decomposition of 
$$CaCO_3 = \frac{0.26335}{0.4} \times 100 = 65.83$$
 % decomposed

Hence 34.17 % remain unreacted.

**Ex.** For the reaction :

$$SnO_2(s) + 2H_2(g) \Longrightarrow 2H_2O(g) + Sn(s)$$

Calculate K<sub>p</sub> at 900 K where the equilibrium steam hydrogen mixture was 35 % H<sub>2</sub> by volume.

Sol. 
$$K_p = \frac{(P_{H_2O})^2}{(P_{H_a})^2}$$

given H<sub>2</sub> is 35% by volume at constant temperature in closed vessel (P  $\propto$  V)

so 
$$P_{H_2O} = 0.65$$
 atm and  $P_{H_2} = 0.35$  atm

$$K_p = \left(\frac{0.65}{0.35}\right)^2 = 3.448$$

#### LE-CHATELIER'S PRINCIPLE

According to this principle. If a system at equilibrium is subjected to a change of concentration, pressure or temperature, the equilibrium is shifted in such a way as to nullify the effect of change.

- (a) Change in Concentration: In an equilibrium increasing the concentrations of reactants results in shifting the equilibrium in favour of products while increasing concentrations of the products results in shifting the equilibrium in favour of the reactants.
- (b) Change of Pressure: When the pressure on the system is increased, the volume decreases proportionately. The total number of moles per unit volume increases. According to Le-Chatelier's principle, the equilibrium shift in the direction in which there is decrease in number of moles.

If there is no change in number of moles of gases in a reaction, a pressure change does not affect the equilibrium.

(c) Change in Temperature: If the temperature at equilibrium is increased reaction will proceed in the direction in which heat can be used. Thus increase in temperature will favour the forward reaction for endothermic reaction.

Similarly, increase in temperature will favour the backward reaction in exothermic reactions.

#### APPLICATION OF LE-CHATELIER'S PRINCIPLE

- (A) Chemical Equilibria
  - (a) Formation of HI

$$H_2(g) + I_2(g) \rightleftharpoons 2HI(g) + 3000 \text{ Cals}$$

- (i) Effect of Concentration: When concentration of H<sub>2</sub> or I<sub>2</sub> is increased at equilibrium, the system moves in a direction in which decreases the concentration. Thus the rate of forward reaction increases thereby increasing the concentration of HI.
- (ii) Effect of Pressure: In formation of HI, there is no change in the number of moles of reactants and products ( $\Delta n = 0$ ). Thus it is not affected by the change in pressure or volume.
- (iii) Effect of Temperature: The formation of HI is exothermic reaction. Thus the backward reaction moves faster when temperature is increased, i.e. formation of HI is less.

In short favourable conditions for greater yield of HI:

High concentration of H<sub>2</sub> and I<sub>2</sub>.

Low temperature.

No effect of pressure

(b) Formation of NO

$$N_2 + O_2 \implies 2NO - 43200 \text{ cals.}$$

- (i) Effect of Concentration: When concentration of  $N_2$  or  $O_2$  is increased, the system moves in a direction in which  $N_2$  or  $O_2$  is used up or rate of forward increases.
- (ii) Effect of Pressure: The formation of NO is not affected by change in pressure.

$$(\Delta n = 0)$$
.

(iii) Temperature: The formation of NO is endothermic. Thus increase in temperature favours to forward reaction.

Favourable conditions for greater yield of NO:

High concentration of N<sub>2</sub> and O<sub>2</sub>.

High temperature.

No effect of pressure

(c) Dissociation of PCl<sub>z</sub>

$$PCl_s(g) \rightleftharpoons PCl_s(g) + Cl_s(g) - 15000 \text{ cals.}$$

- (i) Effect of Concentration: When concentration of PCl<sub>5</sub> is increased at equilibrium, the rate of forward reaction increases as to decrease the added concentration. Thus dissociation of PCl<sub>5</sub> increases.
- (ii) Effect of Pressure: The volume increases in the dissociation of PCl<sub>5</sub> when pressure is increased, the system moves in the direction in which there is decrease in volume. Thus high pressure does not favour dissociation of PCl<sub>5</sub>.
- (iii) Effect of Temperature: The dissociation of PCl<sub>5</sub> is an endothermic reaction. Thus increase of temperature favours the dissociation.

Favourable conditions for dissociation of PCl<sub>s</sub> are:-

High concentration of PCl<sub>s</sub>.

Low pressure.

High temperature.

#### (d) Synthesis of Ammonia

$$N_2(g) + 3H_2(g) \implies 2NH_3(g) + 22400 \text{ Cals.}$$

The favourable conditions for greater yield of NH, are:-

High concentration of N<sub>2</sub> and H<sub>2</sub>.

High pressure.

Low temperature.

#### (e) Formation of SO,

$$2SO_2(g) + O_2(g) \rightleftharpoons 2SO_3 + 45200 \text{ Cals.}$$

The favourable conditions for greater yield of SO<sub>3</sub> are:-

High concentration of  $SO_2$  and  $O_2$ .

High pressure.

Low temperature.

**Ex.** In reaction,

$$CO(g) + 2H_2(g) \rightleftharpoons CH_3OH(g)$$

$$\Delta H^{\circ} = -92 \text{ kJ/mol}^{-1}$$

concentrations of hydrogen, carbon monoxide and methanol become constant at equilibrium. What willhappen if:

- (A) volume of the reaction vessel in which reactants and products are contained is suddenly reduced to half?
- (B) partial pressure of hydrogen is suddenly doubled?
- (C) an inert gas is added to the system at constant pressure?
- (D) the temperature is increased?
- **Sol.** For the equilibrium,

$$CO(g) + 2H_2(g) \rightleftharpoons CH_3OH(g)$$

$$K_{c} = \frac{[CH_{3}OH]}{[CO][H_{2}]^{2}} \Rightarrow K_{p} = \frac{P_{CH_{3}OH}}{P_{CO} \times P_{H_{2}}^{2}}$$

(A) When the volume of the vessel is suddenly reduced to half, the partial pressures of various species gets

doubled. Therefore, Q\_p = 
$$\frac{2P_{\text{CH}_3\text{OH}}}{2P_{\text{CO}} \times \left(2P_{\text{H}_2}\right)^2} = \frac{1}{4} \, K_p$$

Since Q<sub>p</sub> is less than K<sub>p</sub>, the equilibrium shift in the forward direction producing more CH<sub>3</sub>OH.

(B) When partial pressure of hydrogen is suddenly doubled,  $Q_p$  changes and is no longer equal to  $K_p$ .

$$Q_{p} = \frac{P_{CH_{3}OH}}{P_{CO} \times (2P_{H_{2}})^{2}} = \frac{1}{4}K_{p}$$

Equilibrium will shift from left to right.

- (C) When an inert gas is added to the system at constant pressure, equilibrium shifts from lower number of moles to higher number of moles (in backward direction).
- (D) By increasing the temperature, K<sub>n</sub> will decrease and equilibrium will shift from right to left.

#### **KEY POINTS**

- (1) Irreversible reaction proceeds in one direction and completed with time while reversible reaction proceeds in both direction and are never completed.
- (2) Equilibrium is defined as the point at which the rate of forward reaction is equal to the rate of backward reaction.
- (3) Chemical equilibrium is dynamic in nature and equilibrium state can be approached from both sides.
- (4) Active mass is molar concentration of the substance. Active mass of solid and pure liquid is taken as unity.
- (5) Equilibrium constant has definite value for every chemical reaction at a given temperature. It is independent of concentration and catalyst.
- (6) If a reaction can be expressed as the sum of two or more reactions then overall  $K_C$  will be equal to the product of the equilibrium constant of individual reaction.

Ex. 
$$SO_2(g) + \frac{1}{2} O_2(g) \rightleftharpoons SO_3(g) \rightarrow K_1$$
  $NO_2(g) \rightleftharpoons NO(g) + \frac{1}{2} O_2(g) \rightarrow K_2$  then  $SO_2(g) + NO_2(g) \rightleftharpoons SO_3(g) + NO(g) \rightarrow K$   $K = K_1 \times K_2$ 

- (7) Change in temperature, pressure or concentration favours one of the reactions and thus shift the equilibrium point in one direction.
- (8) A catalyst ables the system to reach a state of equilibrium more quickly.
- (9) Pressure and volume has no effect on the reaction in which there is no change in the number of moles.
- (10) If the concentration of reactants is increased and product is removed, the reaction will take place in forward direction.
- (11) Free energy change

$$\Delta G = \Delta G^{\circ} + 2.303 \text{ RT log } Q$$
 At equilibrium  $\Delta G = 0$ , (T is in Kelvin),  $Q = K$  so  $\Delta G^{\circ} = -2.303 \text{ RT log } K$ , where K is equilibrium constant.

Ex.  $\Delta G^{\circ}$  for  $\frac{1}{2}$   $N_2 + \frac{3}{2}$   $H_2 \rightleftharpoons$   $NH_3$  is -16.5 kJ mol $^{-1}$ . Find out  $K_p$  for the reaction at 25°C. Also report  $K_p$  and  $\Delta G^{\circ}$  for  $N_2 + 3H_2 \rightleftharpoons$   $2NH_3$  at 25°C.

Sol. 
$$\log K_p = -\frac{\Delta G^{\circ}}{2.303 \,\text{RT}} = \frac{+16.5 \times 10^3}{2.303 \times 8.314 \times 298} = 2.8917$$

$$K_p = antilog(2.8917) = 779.41$$

Now given reaction  $N_2 + 3H_2 \Longrightarrow 2NH_3$  can be obtained by multiplying eq.  $1/2 N_2 + 3/2 H_2 \Longrightarrow NH_3$  by 2. so  $K_p' = (779.41)^2 = 6.07 \times 10^5$  and  $\Delta G^\circ = -2.303 \text{ RT log } K_p' = -2.303 \times 8.314 \times 298 \log (6.07 \times 10^5) \text{ J}$   $\Delta G^\circ = -32.998 \text{ kJ mol}^{-1}$ .

For the gaseous reaction  $CO + H_2O \rightleftharpoons CO_2 + H_2$ , the following thermodynamics data are given. Ex.

$$\Delta H_{300 \text{ K}}^{\circ} = -41.16 \text{ kJ mol}^{-1}$$
;  $\Delta S_{300 \text{ K}}^{\circ} = -0.0424 \text{ kJ mol}^{-1}$ .

$$\Delta H_{1200 \, K}^{\circ} = -32.93 \text{ kJ mol}^{-1}$$
;  $\Delta S_{1200 \, K}^{\circ} = -0.0296 \text{ kJ mol}^{-1}$ .

Assuming partial pressure of each component at 1 atm. determine the direction of spontaneous reaction at (i) 300 K

(ii) 1200 K. Also calculate K<sub>p</sub> for the reaction at each temperature.

Sol. Using  $\Delta G^{\circ} = \Delta H^{\circ} - T\Delta S^{\circ}$ 

$$\Delta G^{\circ}_{300 \,\mathrm{K}} = -41.16 - 300 \,(-0.0424)$$

$$=-28.44 \text{ kJ mol}^{-1}$$

so reaction is spontaneous in given direction since  $\Delta G^{\circ}$  is negative

$$CO + H_2O \rightleftharpoons CO_2 + H_2$$

at 1200 K

$$\Delta G^{\circ}_{1200 \,\mathrm{K}} = -32.93 - 1200 \,(-0.0296)$$

$$= 2.56 \text{ kJ mol}^{-1}$$

so reaction will not be spontaneous in given direction, but reverse reaction spontaneous i.e.

$$CO + H$$
,  $\rightleftharpoons$   $CO + H$ ,  $O$ 

We know 
$$\Delta G^{\circ} = -2.303 \text{ RT log K}_{p}$$

so 
$$K_p(300 \, K)$$

= antilog 
$$\left(\frac{-28.44 \times 10^3}{-2.303 \times 8.314 \times 300}\right) = 8.8 \times 10^4$$

$$K_p = (1200 \, \text{K})$$

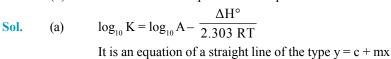
= antilog 
$$\left(\frac{+2.59 \times 10^3}{-2.303 \times 8.314 \times 1200}\right)$$
 = 0.77

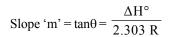
Variation of equilibrium constant K with temperature T is given by van't Hoff equation,  $\log K = \log A - \frac{\Delta H^{\circ}}{2.202 \text{ p.t.}}$ Ex.

$$\log K = \log A - \frac{\Delta H^{\circ}}{2.303 \text{ RT}}$$

A graph between log K and  $T^{-1}$  was a straight line as shown in the figure and having  $\theta = \tan^{-1}(0.5)$  and OP = 10. Calculate:

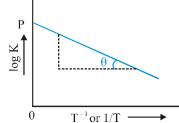
- (a)  $\Delta H^{\circ}$  (standard heat of reaction) when T = 300 K,
- (b) A (pre-exponential factor),
- (c) Equilibrium constant K, at 300 K,
- (d) K at 900 K if  $\Delta H^{\circ}$  is independent of temperature.





$$0.5 = \frac{\Delta H^{\circ}}{2.303 \times 8.314}$$

$$\Delta H^{\circ} = 9.574 \,\mathrm{J} \,\mathrm{mol}^{-1}$$



(b) Intercept 'c' = 
$$\log_{10} A = 10$$
 :  $A = 10^{10}$ 

(c) 
$$\log K = 10 - \frac{9.574}{2.303 \times 8.314 \times 298}$$
  
 $K = 9.96 \times 10^9$ 

(d) 
$$\log \left(\frac{K_2}{K_1}\right) = \frac{\Delta H}{2.303 R} \left\{\frac{1}{T_1} - \frac{1}{T_2}\right\}$$

$$\log \frac{K_2}{9.96 \times 10^9} = \frac{9.574}{2.303 \times 8.314} \left\{ \frac{1}{298} - \frac{1}{798} \right\}$$

On solving 
$$K_2 = 9.98 \times 10^9$$

(b) 
$$A = 1010$$
;

(c) 
$$9.96 \times 109$$
;

(d) 
$$9.98 \times 109$$

### REACTION QUOTIENTAND EQUILIBRIUM CONSTANT

Consider the following reversible reaction

$$A+B \rightleftharpoons C+D$$

The reaction quotient  $(Q_c)$  is ratio of the product of active masses of the products and product of active masses of the reactants, at any given time.

$$\therefore Q_{C} = \frac{[C][D]}{[A][B]}$$

The concentration are not necessarily equilibrium concentration.

[At equilibrium 
$$Q_C = K_C$$
]

#### Case I

If  $Q_C < K_C$  Then: [Reactants] > [Products]

then the system is not at equilibrium

The value of 
$$\frac{[Product]}{[Reactant]}$$
 is small

∴ For establishment of equilibrium the reaction will go in forward direction. [Reactants → Products]

#### Case II

If  $Q_c = K_c$  Then: The system is at equilibrium and the concentration of the species C,D,B,A are at equilibrium.

Case III

If 
$$Q_C > K_C$$
 Then: [Product] > [Reactants]

The system is not at equilibrium.

The value of 
$$\frac{[Product]}{[Reactant]}$$
 is large

∴ For establishment of equilibrium the reaction will go in backward direction. [Products → Reactants]

A mixture of 4.2 moles of  $N_2$ , 2.0 moles of  $H_2$  and 10.0 moles of  $NH_3$  is introduced into a 10.0 L reaction vessel at 500

K. At this temperature, equilibrium constant K  $_c$  is  $1.7 \times 10^2$ , for the reaction  $N_2(g) + 3H_2(g) \Longrightarrow 2NH_3(g)$ 

- (i) is the reaction mixture at equilibrium?
- (ii) if not, what is the direction of the reaction?

**Sol.** 
$$[N_2] = \frac{4.2}{10} = 0.42 \text{ M}$$

$$[H_2] = \frac{2.0}{10} = 0.2 \,\mathrm{M}$$

$$[NH_3] = \frac{10}{10} = 0.1 \text{ M}$$

For these concentration, reaction quotient (Q) for the reaction

$$N_2(g) + 3H_2(g) \Longrightarrow 2NH_3(g)$$
 is

$$Q = \frac{[NH_3]^2}{[N_2][H_2]^3} = \frac{(0.1)^2}{(0.42) \times (0.2)^3} = 2.976$$

But 
$$K_c = 1.7 \times 10^2$$

- (i) Since  $Q \neq K_c$ , hence reaction is not at equilibrium.
- (ii) Also  $Q < K_c$ , the reaction will proceed from left to right.
- Ex. For the reaction NOBr (g)  $\rightleftharpoons$  NO(g) +  $\frac{1}{2}$  Br<sub>2</sub>(g)

 $K_p = 0.15$  atm at 90°C. If NOBr, NO and Br<sub>2</sub> are mixed at this temperature having partial pressures 0.5 atm, 0.4 atm and 0.2 atm respectively, will Br<sub>2</sub> be consumed or formed?

Sol. 
$$Q_P = \frac{\left[P_{Br_2}\right]^{1/2} \left[P_{NO}\right]}{\left[P_{NOBr}\right]} = \frac{\left[0.2\right]^{1/2} \left[0.4\right]}{\left[0.50\right]} = 0.36$$

$$K_p = 0.15$$

$$Q_p > K_p$$

Hence, reaction will shift in backward direction

.. Br, will be consumed

# **Predicting The Extent of The Reaction**

$$K = \frac{\left[Product\right]_{eq}}{\left[R\,eactant\right]_{eq}} \\ \\ Negligible \\ reaction \\ hardly \\ proceeds \\ \\ Negligible \\ reaction \\ 10^3 \\ 1 \\ 10^{13} \\ Both \ reaction \\ and \ products \\ are \ significant \\ } \\ Very \ large \\ Very \ large \\ very \ large \\ reaction \\ proceeds \\ almost \ to \ completion \\ large \\ very \ large \\ very$$

#### Case-I

If K is large ( $K > 10^3$ ) then product concentration is very very larger than the reactant ([Product] >>[Reactant]) Hence concentration of reactant can be neglected with respect to the product. In this case, the reaction is product favourable and equilibrium will be more in forward direction than in backward direction.

#### Case-II

If K is very small ( $K < 10^{-3}$ )

[Product] << [Reactant]

Hence concentration of Product can be neglected as compared to the reactant.

In this case, the reaction is reactant favourable.

The  $K_p$  values for three reactions are  $10^{-5}$ , 20 and 300 then what will be the correct order of the percentage composition of the products.

Sol. Since  $K_p$  order is  $10^{-5} < 20 < 300$  so the percentage composition of products will be greatest for  $K_p = 300$ .

### CALCULATION OF DEGREE OF DISSOCIATION FROM VAPOUR DENSITY MEASUREMENT:

### **Degree of Dissociation**

Degree of dissociation of a substance at a particular temperature is defined as the fraction of total number of moles dissociated into simpler molecules at that particular temperature.

Degree of dissociation (
$$\alpha$$
) =  $\frac{\text{No. of moles dissociated}}{\text{Total no. of moles taken}}$ 

Degree of dissociation can be calculated from vapour density measurements for those substance which are accompanied by change in the number of moles.e.g.

dissociation

Total number of moles =  $1 - \alpha + \alpha + \alpha = (1 + \alpha)$ 

Let, volume occupied by the vapour per mole = V litres.

Initial vapour density = D

Vapour density after dissociation = d

As, vapour density 
$$\propto \frac{1}{V}$$

$$\therefore D \propto \frac{1}{V}$$

$$d \propto \frac{1}{(1+\alpha)V}$$

$$\therefore \frac{D}{d} = \frac{1/V}{\frac{1}{(1+\alpha)V}} = (1+\alpha)$$

$$\Rightarrow \alpha = \frac{D}{d} - 1 = \frac{(D - d)}{d}$$

As, mol. wt. =  $2 \times \text{vapour density}$ 

Also, 
$$\alpha = \frac{M_t - M_o}{M_o}$$

 $M_{\star}$  = theoretical molecular mass

M<sub>o</sub> = observed (experimental) molecular mass

M<sub>o</sub> can be calculated from the mass of definite volume of the vapour at particular temperature.

Also, 
$$PV = nRT = \frac{W}{M_0}RT$$

$$M_o = \frac{W}{v} \times \frac{RT}{P} = \frac{\rho RT}{P}$$

where  $\rho$  = density of the vapour.

In general, if one mole dissociates to give n moles of products, then

 $\begin{array}{ccc}
A & \longrightarrow & nB \\
1 & 0 \\
(1-\alpha) & n\alpha
\end{array}$ 

Total no. of moles =  $1 - \alpha + n\alpha = 1 + (n-1)\alpha$ 

$$\therefore \ \frac{D}{d} = 1 + (n-1) \times \alpha \ \Rightarrow \ \alpha = \frac{(D-d)}{(n-1) \times d}$$

Also, 
$$\alpha = \frac{M_t - M_o}{(n-1) \times M_o}$$

Let us, consider the reaction,  $2NH_3(g) \rightleftharpoons N_2(g) + 3H_2(g)$ 

If the initial moles of NH, (g) be 'a' and x moles of NH, dissociated at equilibrium.

 $2NH_3(g) \Longrightarrow N_2(g) + 3H_2(g)$ Initial moles  $a \qquad 0 \qquad 0$ At equilibrium  $a - x \qquad \frac{x}{2} \qquad \frac{3x}{2}$ 

Degree of dissociation (α) of NH<sub>3</sub> is defined as the number of moles of NH<sub>3</sub> dissociated per mole of NH<sub>3</sub>.

 $\therefore$  If x moles dissociate from 'a' moles of NH<sub>3</sub> then, the degree of dissociation of NH<sub>3</sub> would be  $\frac{x}{a}$ .

We can also look at the reaction in the following manner.

 $2NH_3(g) \Longrightarrow N_2(g) + 3H_2(g)$  Initial moles  $a \qquad 0 \qquad 0$  At equilibrium  $a(1-\alpha) \qquad \frac{a\alpha}{2} \qquad \frac{3a\alpha}{2}$  or  $a-2x' \qquad x' \qquad 3\ x'$ 

where  $\alpha = \frac{2x'}{a}$ 

Here, total number of moles at equilibrium is a - 2x' + x' + 3x' = a + 2x'

Mole fraction of NH<sub>3</sub> =  $\frac{a - 2x'}{a + 2x'}$ 

Mole fraction of  $N_2 = \frac{x'}{a + 2x'}$ 

Mole fraction of  $H_2 = \frac{3x'}{a + 2x'}$ 

The expression of  $K_p$  is

$$K_{p} = \frac{\left(\frac{x'}{a + 2x'}\right) P_{T} \times \left(\frac{3x'}{a + 2x'}\right)^{3} \times P_{T}^{3}}{\left(\frac{a - 2x'}{a + 2x'}\right)^{2} \times P_{T}^{2}} = \frac{27x'^{4}}{(a - 2x')^{2}} \times \frac{P_{T}^{2}}{(a + 2x')^{2}}$$

In this way, you should find the basic equation. So, it is advisable to follow the below mentioned steps while solving the problems.

Write the balanced chemical reaction (mostly it will be given).

Under each component write the initial number of moles.

Do the same for equilibrium condition.

Then derive the expression for K<sub>n</sub> and K<sub>s</sub> accordingly.

Vapour density of the equilibrium mixture NO, and N<sub>2</sub>O<sub>4</sub> is found to be 42 for the reaction, Ex.

$$N_2O_4 \Longrightarrow 2NO_2$$
. Find

- (a) Abnormal molecular weight
- (b) Degree of dissociation
- (c) Percentage of NO, in the mixture
- (a) For the reaction,  $N_2O_4 \Longrightarrow 2NO_7$ Sol.

Observed value of vapour density = 42

Abnormal molecular weight =  $42 \times 2$ (d=42)

(b) Theoretical molecular weight = 92

$$2 \times D = 92$$

$$D = \frac{92}{2} = 46$$

$$\alpha = \frac{D-d}{d} = \frac{46-42}{42} = 0.095$$

$$(c) N_2O_4 \Longrightarrow 2NO_7$$

$$(1-\alpha)$$
  $2\alpha$ 

Total moles at equilibrium =  $1 + \alpha = 1 + 0.095$ 

$$\therefore$$
 % of NO<sub>2</sub>=  $\frac{2\alpha}{(1+\alpha)} \times 100 = \frac{0.19}{1.095} \times 100 = 17.35 \%$ 

Ex. The equilibrium constant of the reaction  $A_2(g) + B_2(g) \implies 2AB(g)$  at 50°C is 50. If one litre flask containing one mole of A<sub>2</sub> is connected to a two litre flask containing two moles of B<sub>2</sub>, how many moles of AB will be formed at 323 K.

Sol. 
$$A_2(g) + B_2(g) \rightleftharpoons 2AB(g); K_c = 50$$

Initial mole

At eq. mole

$$1-x$$
  $2-x$ 

At eq. conc.

$$\frac{1-x}{3}$$
  $\frac{2-x}{3}$   $\frac{2x}{3}$ 

$$\frac{2x}{3}$$

$$K_c = \frac{\left(\frac{2x}{3}\right)^2}{\left(\frac{1-x}{3}\right)\left(\frac{2-x}{3}\right)} = 50 \implies 23x^2 - 75x + 50 = 0$$

x = 0.934 or 2.326

Only 0.934 values is permissible

So, moles of AB = 1.868

- Calculate the % age dissociation of  $H_2S(g)$  if 0.1 mole of  $H_2S$  is kept in a 0.4 L vessel at 900 K. The value of  $K_c$  for the reaction,  $2H_2S(g) \Longrightarrow 2H_2(g) + S_2(g)$ , is  $1.0 \times 10^4$ .
- Sol.  $2H_2S \Longrightarrow 2H_2 + S_2$

Volume of vessel = V = 0.4 L

Let, x be the degree of dissociation

Moles 
$$2H_2S \Longrightarrow 2H_2 + S_2$$
Initially  $0.1 \qquad 0 \qquad 0$ 
At equilibrium  $0.1-0.1x \qquad 0.1x \qquad 0.1x/2$ 

$$K_{c} = \frac{[H_{2}]^{2}[S_{2}]}{[H_{2}S]^{2}} = \frac{\left(\frac{0.01x}{v}\right)^{2} \left(\frac{0.01}{2v}\right)}{\left(\frac{0.01 - 0.01x}{v}\right)^{2}} = 10^{4} \implies x = 0.02 \text{ or } 2\% \text{ dissociation of } H_{2}S$$

- Ex. The degree of dissociation of HI at a particular temperature is 0.8. Find the volume of 1.5 M sodium thiosulphate solution required to react completely with the iodine present at equilibrium in acidic condition, when 0.135 mol each of H, and I, are heated at 440 K in a closed vessel of capacity 2.0 L.
- **Sol.** First find the value of K<sub>c</sub> for dissociation of HI from its degree of dissociation

2HI  $\longrightarrow$  H<sub>2</sub> + I<sub>2</sub> (degree of dissociation is 0.8)

Concentrations 
$$2HI \iff H_2 + I_2$$
  
Initially  $1.0 0 0$   
At new equilibrium  $1.0$ – $0.8 0.4 0.4$ 

$$K_c = \frac{[H_2][I_2]}{[HI]^2} = \frac{(0.4)(0.4)}{(0.2)^2} = 4$$

Now, we have to start with 0.135 mol each of H, and I, and the following equilibrium will be established.

$$H_2 + I_2 \rightleftharpoons 2HI \text{ with } K_c = \frac{1}{4}$$

$$\Rightarrow K_c = \frac{[HI]^2}{[H_2][I_2]} = \frac{(2x)^2}{(0.135 - x)(0.135 - x)} = \frac{1}{4}$$

$$\Rightarrow$$
 x = 0. 135/5 = 0.027 moles

Now, find the moles of I, left unreacted at equilibrium.

$$n_{L_0} = 0.135 - 0.027 = 0.108$$
 moles

I<sub>2</sub> reacts with sodium thiosulphate (Na<sub>2</sub>S<sub>2</sub>O<sub>3</sub>) as follows:

$$2Na_2S_2O_3 + I_2 \Longrightarrow Na_2S_4O_6 + 2NaI$$

Applying mole concept, we have 2 moles of  $Na_2S_2O_3 = 1$  mole of  $I_2$ 

- $\Rightarrow$  0.108 moles of  $I_2 = 2 \times 0.108 = 0.216$  moles of  $Na_2S_3O_3$  are used up
- $\Rightarrow$  Moles =  $MV_n$  (M = Molarity,  $V_n$  = volume in litres)
- $\Rightarrow$  0.216 = 1.5 V
- $\Rightarrow$  V = 0.144 lt = 144 mL.
- Ex. 102 g of solid NH<sub>4</sub>HS is taken in the 2L evacuated flask at 57°C. Following two equilibrium exist simultaneously  $NH_4HS(s) \Longrightarrow NH_3(g) + H_2S(g)$

$$NH_3(g) \Longrightarrow \frac{1}{2} N_2(g) + \frac{3}{2} H_2(g)$$

one mole of the solid decomposes to maintain both the equilibrium and 0.75 mole of H, was found at the equilibrium then find the equilibrium concentration of all the species and K<sub>C</sub> for both the reaction.

**Sol.** Moles of 
$$NH_4HS = \frac{102}{51} = 2$$

$$NH_4HS(s) \Longrightarrow NH_3(g) + H_2S(g)$$
  $K_{C_1}$   
 $\begin{pmatrix} 2 & 0 & 0 \\ 1 & 1-x & 1 \end{pmatrix}$ 

$$NH_{3}(g) ~ \stackrel{\textstyle \longrightarrow}{\longleftarrow} ~ \frac{1}{2} ~ N_{2}(g) + \frac{3}{2} ~ H_{2}(g) ~ ~ \mathsf{K}_{\mathsf{C}_{2}}$$

$$1-x$$
  $\frac{x}{2}$   $\frac{3x}{2}$ 

Given that moles of 
$$H_2 = \frac{3x}{2} = 0.75 \implies x = \frac{1}{2}$$

$$K_{C_1} = \frac{1}{2} \frac{(1-x)}{2} = \frac{1}{8}$$
 [Since V = 2 L]

$$K_{c_2} = \frac{\left(\frac{3x}{4}\right)^{3/2} \left(\frac{x}{4}\right)^{\frac{1}{2}}}{\left(\frac{1-x}{2}\right)} = \frac{\left(\frac{3}{8}\right)^{3/2} \left(\frac{1}{8}\right)^{\frac{1}{2}}}{\frac{1}{4}} = (3)^{3/2} \frac{1}{64} \times \frac{4}{1} = \frac{(3)^{3/2}}{16}$$

S. No.	Reaction	Δn		Relation b/w Kp and Kc	values of Ho	values of K <sub>o</sub>	Unit of Ke	Unit of Kp	Relation b/w amount of dissociation (volume and pressure)	ΔН	Conditions for obtaining 3 more product 3
-	H2 뉴 선 + 대	0	$K_p = K_c (RT)^0$	$K_p = K_c$	$\frac{4x^2}{(a-x)(b-x)}$	$\frac{4x^2}{(a-x)(b-x)}$	Nonc	None	None	-ve (exothermic)	Low temperature, no pressure, high concentration
2	2HI ⇌ H2 + l2	0	$K_p = K_e (RT)^0$	$K_p = K_c$	$\frac{x^2}{4(1-x)^2}$	$\frac{x^2}{4(1-x)^2}$	Nome	Мопе	None	+ve(endothermic)	High temperature, no pressure, high concentration
ίς.	$PG_{\delta} \rightleftharpoons PG_{\delta} + G_{\Sigma}$	7	$K_p = K_c (RT)^1$	$K_p > K_c$	$\frac{x^2}{(1-x)v}$	$\frac{x^2p}{(1-x^2)}$	gram mo[	(Atm Pressure) <sup>1</sup>	$ \begin{array}{c} x \alpha \sqrt{v} \\ \text{or } x \alpha \frac{1}{\sqrt{p}} \end{array} $	-ve(endothermic)	Higher temperatuare, Low pressure, High concentration
৸	N2O4 ⇌ 2NO2	7	$K_{\rho} = K_{c} (RT)^{1}$	Kr > Kc	$\frac{4x^2}{(1-x)y}$	$\frac{4x^2p}{(1-x^2)}$	grammol iii	(Atm Pressure) <sup>-1</sup>	$x \alpha \sqrt{v}$ or $x \alpha \frac{1}{\sqrt{p}}$	-ve(endothermic)	Higher temperatuare, Low pressure, High concentration
ς,	2NH3 ⇌ N½ + 3H2	7	$K_p = K_c (RT)^2$	Kp > KC	$\frac{27x^4}{4(1-x)^2v^2}$	$\frac{27x^4p^2}{16(1-x)^2(1+x)^2}$	gram mol lit	(Atm. Pressure) <sup>2</sup>	$\mathbf{x} \alpha \sqrt{\mathbf{v}}$ or $\mathbf{x} \alpha \frac{1}{\sqrt{\mathbf{p}}}$	-ve(endothermic)	Higher temperatuere, Low pressure, t High concentration
9	N <sub>2</sub> + 3H <sub>2</sub> ⇌ 2NH <sub>3</sub>	-7	$K_{\boldsymbol{p}} = K_{c} \left( \mathbb{R} T \right)^{-2}$	K <sub>P</sub> < K <sub>C</sub>	$\frac{4x^2v^2}{27(1+x)^4}$	$\frac{16x^2(2-x)^2}{27(1-x)^4p^2}$	gram moJ <sup>2</sup> lit	(Atm Pressure) <sup>-2</sup>	x oc v −1 0r x ∞ p	-vc (exothermic)	Low temperature, high pressure, high concentration
7	PCl₃ + Cl₂ ⇒ PCl₅	-1-	$K_{\mathbf{p}} = K_{\mathbf{c}} (RT)^{-1}$	Kp < Kc	$\frac{xv}{(1-x)^2}$	$\frac{x(2-x)}{(1-x)^2p}$	gram mof <sup>l</sup> lit	(Atm. Pressure)	$\mathbf{x} \propto \mathbf{v}^{-1}$ or $\mathbf{x} \propto \mathbf{p}$	-ve (exothermic)	Low temperature, high pressure, high concentration
œ	2\$02 + 02 ⇌ 2\$03	T	$K_{\mathbf{p}} = K_{\mathbf{c}} (RT)^{-1}$	Kr < Kc	$\frac{x^2V}{(1-x)^3}$	$\frac{x^2(3-x)}{(1-x)^3p}$	grammol <sup>1</sup> jii	(Atm Pressure) <sup>-1</sup>	$\begin{array}{c} x \propto \frac{1}{\sqrt{v}} \\ \text{or } x \propto \sqrt{p} \end{array}$	-ve (exothermic)	Low temperature, high pressure, n high concentration

# tips

- Law of Mass Action. It was put forward by Guldberg and Waage. It states that the rate at which a substance reacts is
  directly proportional to its active mass and hence the rate at which substances react together is directly proportional
  to the product of their active masses. Active mass means molar concentration.
- 2. Law of Chemical Equilibrium. For the reaction  $aA + bB \rightleftharpoons xX + yY$ ,  $\frac{[X]^x[Y]^y}{[A]^a[B]^b} = K$ , called equilibrium constant which is constant for a reaction at constant temperature.
- 3. Equilibrium Constant in Terms of Concentrations (Kc) is  $K_c = \frac{[X]^x [Y]^y}{[A]^a [B]^b}$ .

It has units =  $(\text{mol } L^{-1})^{(x+y)-(a+b)}$ 

Equilibrium Constant in Terms of Pressures is 
$$K_p = \frac{P_X^x P_Y^y}{P_a^A P_B^b}$$

It has units =  $(atm)^{(x+y)-(a+b)}$ 

Expressed in terms of activities (in place of molar concentration), equilibrium constant is dimensionless.

4. Relation between Kp and Kc.  $K_p$  and  $K_c$  are related to each other as  $K_p = K_c (RT)^{\Delta n_g}$ 

Where  $\Delta n_g = (n_p - n_r)$  gaseous

- 5. Concentration Quotient Condition or Reaction Quotient (Q). For the reaction  $aA + bB \rightleftharpoons xX + yY$ , at any other than the stage of equilibrium, the expression  $\frac{[X]^x[Y]^y}{[A]^a[B]^b} = Q$  is called concentration quotient or reaction quotient.
  - (i) If Q = K, the reaction is in equilibrium.
  - (ii) If Q < K, Q will tend to increase till it becomes equal to K. Hence, reaction proceeds in the forward direction.
  - (iii) If Q > K, Q will tend to decrease. As a result, the reaction will proceed in the backward direction.
- **6.** Effect of Temperature on K. For aA+bB  $\xrightarrow{k_f}$  C+D, K =  $\frac{k_f}{k_b}$ .

For exothermic reaction, k, decreases with increase of temperature, so K decreases.

For endothermic reaction, k, increases with increase of temperature, so K increases.

- 7. Effect of Adding Inert Gas at Equilibrium.
  - (i) For reactions in which  $n_p = n_r$ , there is no effect of adding an inert gas at constant volume or at constant pressure on the equilibrium.
  - (ii) For reaction in which  $n_p > n_r$  (e.g.  $PCl_5 \rightleftharpoons PCl_3 + Cl_2$ ), there is no effect of adding inert gas on the equilibrium at constant volume but at constant pressure, equilibrium shifts in the forward direction.
- 8. Le Chatelier's Principle states that "if a system in equilibrium is subjected to a change of concentration, temperature or pressure, the equilibrium shifts in a direction so as to undo the effect of the change imposed."
- 9. Van't Hoff Reaction Isotherm. It is an equation which gives the relationship between standard free energy change  $(\Delta G^{\circ})$  of a reaction and its equilibrium constant  $(K_p)$ ,

i.e. 
$$\Delta G^{\circ} = -RT \ln K_{n}$$

This equation helps to calculate  $\Delta G^{\circ}$  of a reaction at temperature T if its equilibrium constant at this temperature is known or vice-versa.

10. Van't Hoff Equation. This equation gives the variation of equilibrium constant of a reaction with temperature. The equation is

$$\frac{dlnK_p}{dT} = \frac{\Delta H^{\circ}}{RT^2}$$

The integrated form of this equation is

$$\log \frac{K_2}{K_1} = \frac{\Delta H^{\circ}}{2.303R} \left[ \frac{T_2 - T_1}{T_1 T_2} \right]$$

where  $\Delta H^{\circ}$  = enthalpy change of the reaction (assumed to the constant in the temperature range  $T_1$  to  $T_2$ ).

- 11. Units of equilibrium const. =  $(\text{mol } L^{-1})^{(x+y)-(a+b)}$  or  $(\text{atm})^{(x+y)-(a+b)}$
- 12. Degree of dissociation of PCl<sub>5</sub> or N<sub>2</sub>O<sub>4</sub> is given by  $\infty = \frac{D-d}{d} = \frac{M_t M_o}{M_o}$

where D = theoretical vapour density and d = vapour density after dissociation (observed V.D.),  $M_t$  = theoretical (calculated) molecular mass and  $M_0$  = observed molecular mass.

13. From integrated form of van't Hoff equation, viz.

$$\log \frac{K_2}{K_1} = \frac{\Delta H^{\circ}}{2.303R} \left[ \frac{T_2 - T_1}{T_1 T_2} \right]$$

We may conclude that

- (i) If  $\Delta H^{\circ} = 0$ , i.e. no heat is evolved or absorbed in the reaction.  $\log (K_2/K_1) = 0$ , i.e.  $K_2/K_1 = 1$  or  $K_2 = K_1$ . So, equilibrium constant does not change with temperature.
- (ii) If  $\Delta H^{\circ}$  = +ve, i.e. heat is absorbed in the reaction, then  $\log (K_2/K_1) = +\text{ve or } \log K_2 > \log K_1 \text{ or } K_2 > K_1.$  So, equilibrium constant increases with increase in temperature.
- (iii) If  $\Delta H^{\circ}$  = -ve, i.e. heat is evolved in the reaction, then  $\log (K_2/K_1) = -\text{ve, i.e. } \log K_2 < \log K_1 \text{ or } K_2 < K_1.$  So, equilibrium constant decreases with increase in temperature.

