

Unit 12(Introduction To Three Dimensional Geometry)

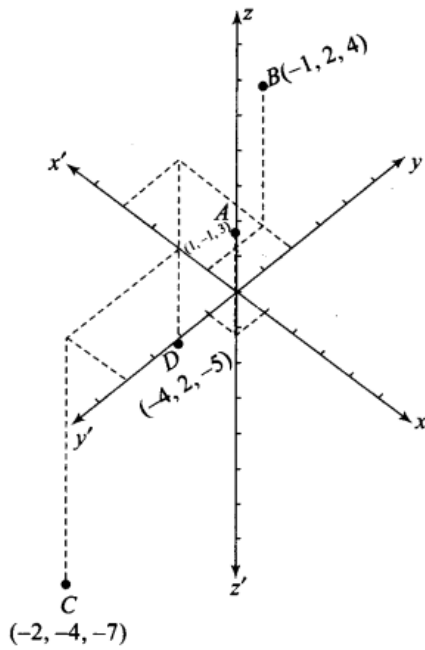
Short Answer Type Questions

Q1. Locate the following points:

- (i) $(1, -1, 3)$,
- (ii) $(-1, 2, 4)$
- (iii) $(-2, -4, -7)$
- (iv) $(-4, 2, -5)$

Sol: Given, coordinates

- (i) $(1, -1, 3)$,
- (ii) $(-1, 2, 4)$
- (iii) $(-2, -4, -7)$
- (iv) $(-4, 2, -5)$



Q2. Name the octant in which each of the following points lies.

- (i) $(1, 2, 3)$
- (ii) $(4, -2, 3)$
- (iii) $(4, -2, -5)$
- (iv) $(4, 2, -5)$
- (v) $(-4, 2, 5)$
- (vi) $(-3, -1, 6)$
- (vii) $(2, -4, -7)$
- (viii) $(-4, 2, -5)$

Sol: We know that the sign of the coordinates of a point determine the octant in which the point lies. The following table shows the signs of the coordinates in eight octants.

Octants	Coordinates	I	II	III	IV	V	VI	VII	VIII
	x	+	-	-	+	+	-	-	+
	y	+	+	-	-	+	+	-	-
	z	+	+	+	+	-	-	-	-

- (i) (1, 2, 3) lies in first quadrant (ii) (4, -2, 3) lies in fourth octant
 (iii) (4, -2, -5) lies in eighth octant (iv) (4, 2, -5) lies in fifth octant.
 (v) (-4, 2, 5) lies in second octant (vi) (-3, -1, 6) lies in third octant
 (vii) (3, -4, -7) lies in eighth octant (viii) (-4, 2, -5) lies in sixth octant.

Q3. Let A, B, C be the feet of perpendiculars from a point P on the x, y, z-axes respectively. Find the coordinates of A, B and C in each of the following where the point P is:

- (i) (3,4,2)
 (ii) (-5,3,7)
 (iii) (4,-3,-5)

Sol: We know that, on x-axis, $y, z = 0$, on y-axis, $x, z = 0$ and on z-axis, $x, y = 0$. Thus, the feet of perpendiculars from given point P on the axis are as follows.

- (i) A(3,0,0), B(0,4,0), C(0,0,2)
 (ii) A(-5, 0, 0), B(0, 3, 0), C(0, 0, 7)
 (iii) A(4, 0, 0), B(0, -3, 0), C(0,0, -5)

Q4. Let A, B, C be the feet of perpendiculars from a point P on the xy, yz and zx- planes respectively. Find the coordinates of A, B, C in each of the following where the point P is

- (i) (3,4,5)
 (ii) (-5,3,7)
 (iii) (4,-3,-5).

Sol: We know that, on xy-plane $z = 0$, on yz-plane, $x = 0$ and on zx-plane, $y = 0$. Thus, the coordinates of feet of perpendicular on the xy, yz and zx-planes from the given point are as follows:

- (i) A(3,4,0), B(0,4, 5), C(3,0,5)
 (ii) A(-5, 3,0), B(0, 3, 7), C(-5, 0, 7)
 (iii) A(4, -3, 0), B(0, -3, -5), C(4,0, -5)

Q5. How far apart are the points (2,0, 0) and (-3, 0, 0)?

Sol: Given points are A (2, 0, 0) and B(-3,0, 0).

$$AB = |2 - (-3)| = 5$$

Q6. Find the distance from the origin to (6, 6, 7).

Sol: Distance from origin to the point (6, 6, 7)

$$= \sqrt{(0-6)^2 + (0-6)^2 + (0-7)^2} = \sqrt{36 + 36 + 49} = \sqrt{121} = 11$$

7. Show that if $x^2 + y^2 = 1$, then the point $(x, y, \sqrt{1-x^2-y^2})$ is at a distance 1 unit from the origin.

Sol. Given that, $x^2 + y^2 = 1$

\therefore Distance of the point $(x, y, \sqrt{1-x^2-y^2})$ from origin is given as

$$d = \sqrt{x^2 + y^2 + (\sqrt{1-x^2-y^2})^2} = \sqrt{x^2 + y^2 + 1 - x^2 - y^2} = 1$$

Q8. Show that the point A(1, -1, 3), B(2, -4, 5) and C(5, -13, 11) are collinear.

Sol: Given points are A(1, -1, 3), B(2, -4, 5) and C(5, -13, 11).

$$AB = \sqrt{(1-2)^2 + (-1+4)^2 + (3-5)^2} = \sqrt{1+9+4} = \sqrt{14}$$

$$BC = \sqrt{(2-5)^2 + (-4+13)^2 + (5-11)^2} = \sqrt{9+81+36} = 3\sqrt{14}$$

$$AC = \sqrt{(1-5)^2 + (-1+13)^2 + (3-11)^2} = \sqrt{16+144+64} = 4\sqrt{13}$$

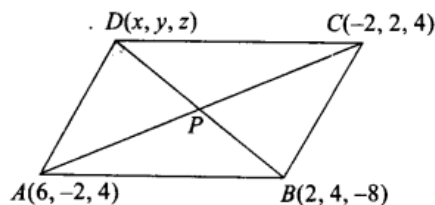
$$\text{Now, } AB + BC = \sqrt{14} + 3\sqrt{14} = 4\sqrt{14} = AC$$

Therefore, the points A, B and C are collinear.

Q9. Three consecutive vertices of a parallelogram ABCD are A(6, -2, 4), B(2, 4, -8), C(-2, 2, 4).

Find the coordinates of the fourth vertex.

Sol: Let the coordinates of the fourth vertex D be (x, y, z).



Mid-point of diagonal AC is $P\left(\frac{6-2}{2}, \frac{-2+2}{2}, \frac{4+4}{2}\right) \equiv P(2, 0, 4)$

Also, mid-point of BD is $P\left(\frac{x+2}{2}, \frac{y+4}{2}, \frac{z-8}{2}\right)$.

Now, $P\left(\frac{x+2}{2}, \frac{y+4}{2}, \frac{z-8}{2}\right) \equiv P(2, 0, 4)$

On equating coordinates, we get

$$\frac{x+2}{2} = 2 \Rightarrow x = 2;$$

$$\frac{y+4}{2} = 0 \Rightarrow y = -4;$$

$$\frac{z-8}{2} = 4 \Rightarrow z = 16$$

So, the coordinate of fourth vertex D are given as $(2, -4, 16)$.

Q10. Show that the triangle ABC with vertices $A(0,4,1)$, $B(2,3,-1)$ and $C(4,5,0)$ is right angled.

Sol: The vertices of ΔABC are $A(0,4,1)$, $B(2,3,-1)$ and $C(4,5,0)$.

$$\text{Now, } AB = \sqrt{(0-2)^2 + (4-3)^2 + (1+1)^2} = \sqrt{4+1+4} = 3$$

$$BC = \sqrt{(2-4)^2 + (3-5)^2 + (-1-0)^2} = \sqrt{4+4+1} = 3$$

$$AC = \sqrt{(0-4)^2 + (4-5)^2 + (1-0)^2} = \sqrt{16+1+1} = \sqrt{18}$$

$$\text{Clearly, } AC^2 = AB^2 + BC^2$$

Therefore, ΔABC is a right angled triangle.

Q11. Find the third vertex of triangle whose centroid is origin and two vertices are $(2,4,6)$ and $(0,-2,-5)$.

Sol: Let the third or unknown vertex of ΔABC be $A(x, y, z)$.

Other vertices of triangle are $B(2,4,6)$ and $C(0,-2,-5)$.

The centroid is $G(0, 0, 0)$.

$$\therefore (0, 0, 0) \equiv \left(\frac{2+0+x}{3}, \frac{4-2+y}{3}, \frac{6-5+z}{3}\right)$$

On comparing coordinates, we get

$$\frac{2+x}{3} = 0, \frac{2+y}{3} = 0 \text{ and } \frac{1+z}{3} = 0$$

$$\Rightarrow x = -2, y = -2 \text{ and } z = -1$$

Q12. Find the centroid of a triangle, the mid-point of whose sides are $D(1,2,-3)$, $E(3,0,1)$ and $F(-1,1,-4)$.

Sol: Given that, mid-points of sides of ΔABC are $D(1,2,-3)$, $E(3,0,1)$ and $F(-1,1,-4)$.

Now from the geometry of centroid, we know that the centroid of ΔDEF is same as the centroid of ΔABC .

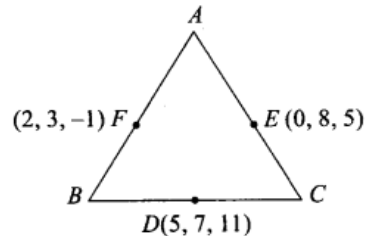
$$\therefore \text{Centroid of } \Delta ABC \text{ is } G\left(\frac{1+3-1}{3}, \frac{2+0+1}{3}, \frac{-3+1-4}{3}\right) \equiv G(1, 1, -2)$$

13. The mid-points of the sides of a triangle are $(5, 7, 11)$, $(0, 8, 5)$ and $(2, 3, -1)$. Find its vertices.

Sol. Given that mid points of the sides of $\triangle ABC$ are $D(5, 7, 11)$, $E(0, 8, 5)$ and $F(2, 3, -1)$.

Let the vertices of triangle be $A(x_1, y_1, z_1)$, $B(x_2, y_2, z_2)$ and $C(x_3, y_3, z_3)$.

Mid-point of AC is E .



$$\therefore \left(\frac{x_1 + x_3}{2}, \frac{y_1 + y_3}{2}, \frac{z_1 + z_3}{2} \right) \equiv (0, 8, 5)$$

$$\text{So, } C(x_3, y_3, z_3) \equiv C(-x_1, 16 - y_1, 10 - z_1) \quad \text{(i)}$$

Mid-point of AB is F .

$$\therefore \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}, \frac{z_1 + z_2}{2} \right) \equiv (2, 3, -1)$$

$$\text{So, } B(x_2, y_2, z_2) \equiv B(4 - x_1, 6 - y_1, -2 - z_1) \quad \text{(ii)}$$

Mid-point of BC is D

$$\therefore \frac{-x_1 + 4 - x_1}{2} = 5, \frac{16 - y_1 + 6 - y_1}{2} = 7, \frac{10 - z_1 - 2 - z_1}{2} = 11$$

$$\Rightarrow x_1 = -3, y_1 = 4 \text{ and } z_1 = -7$$

$$\therefore A \equiv (-3, 4, -7)$$

$$\text{So, } B \equiv (7, 2, 5)$$

$$\text{and } C \equiv (3, 12, 17)$$

[Using (ii)]

[Using (i)]

- Q14. Three vertices of a Parallelogram $ABCD$ are $A(1, 2, 3)$, $B(-1, -2, -1)$ and $C(2, 3, 2)$. Find the fourth vertex

Sol: Let the fourth vertex of the parallelogram $D(x, y, z)$.

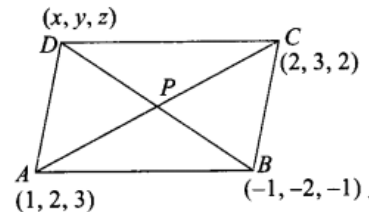
Mid-point of BD

$$\therefore \left(\frac{1 + x}{2}, \frac{2 + y}{2}, \frac{3 + z}{2} \right) \equiv \left(\frac{-1 + 2}{2}, \frac{-2 + 3}{2}, \frac{-1 + 2}{2} \right)$$

$$\therefore \frac{3}{2} = \frac{x - 1}{2} \Rightarrow x = 4;$$

$$\frac{5}{2} = \frac{y - 2}{2} \Rightarrow y = 7; \text{ and}$$

$$\frac{5}{2} = \frac{z - 1}{2} \Rightarrow z = 6$$



So, the coordinates of fourth vertex are $(4, 7, 6)$.

- Q15. Find the coordinate of the points which trisect the line segment joining the points $A(2, 1, -3)$ and $B(5, -8, 3)$.

Sol. Let $P(x_1, y_1, z_1)$ and $Q(x_2, y_2, z_2)$ trisect line segment AB .



Since point P divides AB in the ratio $1 : 2$ internally, we have

$$\begin{aligned} P(x_1, y_1, z_1) &\equiv P\left(\frac{1(5) + 2(2)}{1 + 2}, \frac{1(-8) + 2(1)}{1 + 2}, \frac{1(3) + 2(-3)}{1 + 2} \right) \\ &\equiv P(3, -2, -1) \end{aligned}$$

Since point Q divides AB in the ratio $2 : 1$ internally, we have

$$\begin{aligned} Q(x_2, y_2, z_2) &\equiv Q\left(\frac{2(5) + 1(2)}{2 + 1}, \frac{2(-8) + 1(1)}{2 + 1}, \frac{2(3) + 1(-3)}{2 + 1} \right) \\ &\equiv Q(4, -5, 1) \end{aligned}$$

- Q16. If the origin is the centroid of a triangle ABC having vertices $A(a, 1, 3)$, $B(-2, b, -5)$ and

C(4, 7, c), find the values of a, b, c.

Sol: Vertices of AABC are A(a, 1, 3), B(-2, b, -5) and C(4, 7, c).

Also, the centroid is G(0, 0, 0).

$$\therefore G(0, 0, 0) \equiv G\left(\frac{a-2+4}{3}, \frac{1+b+7}{3}, \frac{3-5+c}{3}\right)$$

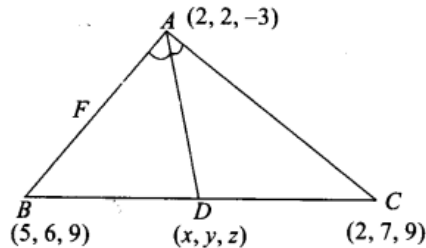
$$\therefore 0 = \frac{a+2}{3} \Rightarrow a = -2;$$

$$0 = \frac{b+8}{3} \Rightarrow b = -8; \text{ and}$$

$$0 = \frac{c-2}{3} \Rightarrow c = 2$$

Q17. Let A(2, 2, -3), B(5, 6, 9) and C(2, 7, 9) be the vertices of a triangle. The internal bisector of the angle A meets BC at the point D. Find the coordinates of D.

Sol. Let the coordinates of D be(x, y, z).



$$AB = \sqrt{(5-2)^2 + (6-2)^2 + (9+3)^2} = \sqrt{9+16+144} = \sqrt{169} = 13$$

$$AC = \sqrt{(2-2)^2 + (7-2)^2 + (9+3)^2} = \sqrt{0+25+144} = \sqrt{169} = 13$$

Thus, ABC is isosceles triangle with AB = AC.

So, angle bisector AD bisects BC or we can say that D is mid-point of BC.

$$\therefore D \equiv \left(\frac{5+2}{2}, \frac{6+7}{2}, \frac{9+9}{2}\right) \equiv \left(\frac{7}{2}, \frac{13}{2}, 9\right)$$

Long Answer Type Questions

Q18. Show that the three points A(2, 3, 4), B(-1, 2, -3) and C(-4, 1, -10) are collinear and find the ratio in which C divides

Sol: Given points are A(2, 3, 4), B(-1, 2, -3) and C(-4, 1, -10)

$$AB = \sqrt{(2+1)^2 + (3-2)^2 + (4+3)^2} = \sqrt{9+1+49} = \sqrt{59}$$

$$BC = \sqrt{(-1+4)^2 + (2-1)^2 + (-3+10)^2} = \sqrt{9+1+49} = \sqrt{59}$$

$$AC = \sqrt{(2+4)^2 + (3-1)^2 + (4+10)^2} = \sqrt{36+4+196} = \sqrt{236} = 2\sqrt{59}$$

$$\text{Now, } AB + BC = \sqrt{59} + \sqrt{59} = 2\sqrt{59} = AC$$

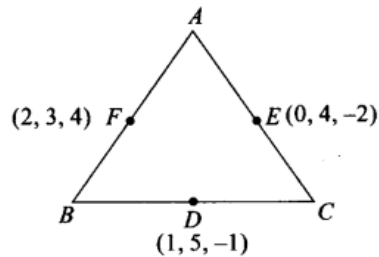
Hence, the points A, B and C are collinear.

$$\text{Also, } AC : BC = 2\sqrt{59} : \sqrt{59} = 2 : 1$$

So, C divides AB in the ratio 2 : 1 externally.

Q19. The mid-point of the sides of a triangle are (1, 5, -1), (0, 4, -2) and (2, 3, 4). Find its vertices. Also, find the centroid of the triangle.

Sol: Given that mid-points of the sides of AABC are D(1, 5, -1), E(0, 4, -2) and F(2, 3, 4).



Let the vertices of triangle be $A(x_1, y_1, z_1)$, $B(x_2, y_2, z_2)$ and $C(x_3, y_3, z_3)$.

Mid-point of AC is E .

$$\therefore \left(\frac{x_1 + x_3}{2}, \frac{y_1 + y_3}{2}, \frac{z_1 + z_3}{2} \right) \equiv (0, 4, -2)$$

$$\text{So, } C(x_3, y_3, z_3) \equiv C(-x_1, 8 - y_1, -4 - z_1) \quad \text{(i)}$$

Mid-point of AB is F .

$$\therefore \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}, \frac{z_1 + z_2}{2} \right) \equiv (2, 3, 4)$$

$$\text{So, } B(x_2, y_2, z_2) \equiv B(4 - x_1, 6 - y_1, 8 - z_1) \quad \text{(ii)}$$

Mid-point of BC is D .

$$\therefore \frac{-x_1 + 4 - x_1}{2} = 1, \frac{8 - y_1 + 6 - y_1}{2} = 5, \frac{-4 - z_1 + 8 - z_1}{2} = -1$$

$$\Rightarrow x_1 = 1, y_1 = 2 \text{ and } z_1 = 3$$

$$\therefore A \equiv (1, 2, 3)$$

$$\text{So, } B \equiv (3, 4, 5) \quad \text{[Using (ii)]}$$

$$\text{and } C \equiv (-1, 6, -7) \quad \text{[Using (i)]}$$

$$\text{Centroid, } G \equiv \left(\frac{1+3-1}{3}, \frac{2+4+6}{3}, \frac{3+5-7}{3} \right) \equiv \left(1, 4, \frac{1}{3} \right)$$

Q20. Prove that the points $(0, -1, -7)$, $(2, 1, -9)$ and $(6, 5, -13)$ are collinear. Find the ratio in which the first point divides the join of the other two.

Sol: Given points are $A(0, -1, -7)$, $B(2, 1, -9)$ and $C(6, 5, -13)$.

$$AB = \sqrt{(0-2)^2 + (-1-1)^2 + (-7+9)^2} = \sqrt{4+4+4} = 2\sqrt{3}$$

$$BC = \sqrt{(2-6)^2 + (1-5)^2 + (-9+13)^2} = \sqrt{16+16+16} = 4\sqrt{3}$$

$$AC = \sqrt{(0-6)^2 + (-1-5)^2 + (-7+13)^2} = \sqrt{36+36+36} = 6\sqrt{3}$$

$$\text{Now, } AB + BC = 2\sqrt{3} + 4\sqrt{3} = 6\sqrt{3} = AC$$

Hence, the points A , B and C are collinear,

$$AB:AC = 2\sqrt{3}:6\sqrt{3} = 1:3$$

So, point A divides BC in $1 : 3$ externally.

Q21. What are the coordinates of the vertices of a cube whose edge is 2 units, one of whose vertices coincides with the origin and the three edges passing through the origin, coincides with the positive direction of the axes through the origin?

Sol: The coordinate of the cube whose edge is 2 units, are:

$(2, 0, 0)$, $(2, 2, 0)$, $(0, 2, 0)$, $(0, 2, 2)$, $(0, 0, 2)$, $(2, 0, 2)$, $(0, 0, 0)$ and $(2, 2, 2)$

Objective Type Questions

Q22. The distance of point $P(3, 4, 5)$ from the yz -plane is

- (a) 3 units
- (b) 4 units
- (c) 5 units
- (d) 550

Sol: (a) Given point is $P(3, 4, 5)$.

Distance of P from yz -plane = $|x$ coordinate of $P| = 3$

Q23. What is the length of foot of perpendicular drawn from the point P(3,4, 5) on y-axis?

- (a) $\sqrt{41}$ (b) $\sqrt{34}$ (c) 5 (d) none of these

Sol. (b) We know that, on the y-axis $x = 0$ and $z = 0$.

\therefore Point $A \equiv (0, 4, 0)$

$$\therefore PA = \sqrt{(0-3)^2 + (4-4)^2 + (0-5)^2} = \sqrt{9+0+25} = \sqrt{34}$$

Q24. Distance of the point (3,4, 5) from the origin (0, 0, 0) is

- (a) $\sqrt{50}$ (b) 3 (c) 4 (d) 5

Sol. (a) Given points are P(3, 4, 5) and O(0, 0, 0).

$$\therefore OP = \sqrt{(0-3)^2 + (0-4)^2 + (0-5)^2} = \sqrt{9+16+25} = \sqrt{50}$$

Q25. If the distance between the points (a,0,1) and (0,1,2) is $\sqrt{27}$, then the value of a is

- (a) 5
(b) ± 5
(c) -5
(d) none of these

Sol. (b) Given points are A(a, 0, 1) and B(0, 1, 2).

$$\therefore AB = \sqrt{(a-0)^2 + (0-1)^2 + (1-2)^2} = \sqrt{27} \quad (\text{given})$$

$$\Rightarrow 27 = a^2 + 2 \quad \Rightarrow a^2 = 25 \quad \Rightarrow a = \pm 5$$

Q26. x-axis is the intersection of two planes

- (a) xy and xz
(b) yz and zx
(c) xy and yz
(d) none of these

Sol: (a) We know that, on the xy and xz-planes, the line of intersection is x-axis.

Q27. Equation of Y-axis is considered as

- (a) $x = 0, y = 0$
(b) $y = 0, z = 0$
(c) $z = 0, x = 0$
(d) none of these

Sol:(c) On the y-axis, $x = 0$ and $z = 0$.

Q28. The point (-2, -3, -4) lies in the

- (a) First octant
(b) Seventh octant
(c) Second octant
(d) Eighth octant

Sol: (b) The point (-2, -3, -4) lies in seventh octant.

Q29. A plane is parallel to yz-plane so it is perpendicular to

- (a) x-axis
(b) y-axis
(c) z-axis
(d) none of these

Sol: (a) A plane parallel to yz-plane is perpendicular to x-axis.

Q30. The locus of a point for which $y = 0, z = 0$ is

- (a) equation of x-axis

- (b) equation of y-axis
- (c) equation at z-axis
- (d) none of these

Sol: (a) We know that, equation of the x-axis is: $y = 0, z = 0$ So, the locus of the point is equation of x-axis.

Q31. The locus of a point for which $x = 0$ is

- (a) xy-plane
- (b) yz-plane
- (c) zx-plane
- (d) none of these

Sol: (b) On the yz-plane, $x = 0$, hence the locus of the point is yz-plane.

Q32. If a parallelepiped is formed by planes drawn through the points (5,8,10) and (3, 6, 8) parallel to the coordinate planes, then the length of diagonal of the parallelepiped is

- (a) $2\sqrt{3}$
- (b) $3\sqrt{2}$
- (c) $\sqrt{2}$
- (d) $\sqrt{3}$

Sol. (a) Given parallelepiped passes through $A(5, 8, 10)$ and $B(3, 6, 8)$

\therefore Length of the diagonal,

$$AB = \sqrt{(5-3)^2 + (8-6)^2 + (10-8)^2} = \sqrt{4+4+4} = 2\sqrt{3}$$

Q33. L is the foot of the perpendicular drawn from a point $P(3, 4, 5)$ on the xy-plane. The coordinates of point L are

- (a) (3,0,0)
- (b) (0,4,5)
- (c) (3, 0, 5)
- (d) none of these

Sol: (d) We know that on the xy-plane, $z = 0$.

Hence, the coordinates of the points L are (3,4, 0).

Q34. L is the foot of the perpendicular drawn from a point (3, 4, 5) on x-axis. The coordinates of L are

- (a) (3,0,0)
- (b) (0,4,0)
- (c) (0, 0, 5)
- (d) none of these

Sol: (a) On the x-axis, $y = 0$ and $z = 0$.

Hence, the required coordinates are (3, 0,0).

Fill in the Blanks Type Questions

Q35. The three axes OX, OY, OZ determine_____.

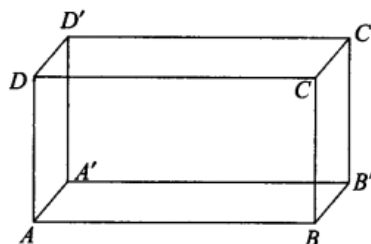
Sol: The three axes OX, OY and OZ determine three coordinate planes.

Q36. The three planes determine a rectangular parallelepiped which has____ of rectangular faces.

Sol.

As shown in the figure rectangular parallelepiped is determined by three planes $ABB'A', AA'D'D, A'B'C'D'$.

In this parallelepiped we have three pairs of rectangular faces, viz., ($ABB'A', DCC'D'$), ($ABCD, A'B'C'D'$), ($ADD'A', BCC'B'$)



Q37. The coordinates of a point are the perpendicular distance from the _____ on the respective axes.

Sol: Given points

Q38. The three coordinate planes divide the space into _____ parts.

Sol: Eight

Q39. If a point P lies in yz-plane, then the coordinates of a point on yz-plane is of the form_____.

Sol: We know that, on yz-plane, $x = 0$. So, the coordinates of the required point are $(0, y, z)$.

Q40. The equation of yz-plane is _____ .

Sol: On yz-plane for any point x-coordinate is zero.

So, yz-plane is locus of point such that $x = 0$, which is its equation.

Q41. If the point P lies on z-axis, then coordinates of P are of the form_____.

Sol: On the z-axis, $x = 0$ and $y = 0$.

So, the required coordinates are of the form $(0, 0, z)$.

Q42. The equation of z-axis, are _____.

Sol: Any point on the z-axis is taken as $(0, 0, z)$.

So, for any point on z-axis, we have $x = 0$ and $y = 0$, which together represents its equation.

Q43. A line is parallel to xy-plane if all the points on the line have equal_____.

Sol: A line is parallel to xy-plane if each point $P(x, y, z)$ on it is at same distance from xy-plane.

Distance of point P from xy plane is 'z'

So, line is parallel to xy-plane if all the points on the line have equal z-coordinate.

Q44. A line is parallel to x-axis if all the points on the line have equal _____.

Sol: A line is parallel to x-axis if each point on it maintains constant distance from y-axis and z-axis.

So, each point has equal y and z-coordinates. .

Q45. $x = a$ represents a plane parallel to .

Sol: Locus of point $P(x, y, z)$ is $x = a$.

Therefore, each point P has constant x-coordinate.

Now, x is distance of point P from yz-plane.

So, here plane $x = a$ is at constant distance 'a' from yz-plane and parallel to yz-plane.

Q46. The plane parallel to yz-plane is perpendicular to_____ .

Sol: The plane parallel to yz-plane is perpendicular to x-axis.

Q47. The length of the longest piece of a string that can be stretched straight in a rectangular room whose dimensions are 10, 13 and 8 units are_____ .

Sol: Given dimensions are: $a = 10$, $b = 13$ and $c = 8$.

Required length of the string = $\sqrt{a^2 + b^2 + c^2} = \sqrt{100 + 169 + 64} = \sqrt{333}$

Q48. If the distance between the points $(a, 2, 1)$ and $(1, -1, 1)$ is 5, then a_____ .

Sol: Given points are $(a, 2, 1)$ and $(1, -1, 1)$.

$$\begin{aligned} \therefore \sqrt{(a-1)^2 + (2+1)^2 + (1-1)^2} &= 5 \text{ (Given)} \\ \Rightarrow (a-1)^2 + 9 + 0 &= 25 \Rightarrow a^2 - 2a - 15 = 0 \Rightarrow (a-5)(a+3) = 0 \\ \therefore a &= 5 \text{ or } -3 \end{aligned}$$

Q49. If the mid-points of the sides of a triangle AB; BC; CA are $D(1, 2, -3)$, $E(3, 0, 1)$ and $F(-1, -4)$, then the centroid of the triangle ABC is_____ .

Sol: Given that, mid-points of sides of ΔABC are $D(1, 2, -3)$, $E(3, 0, 1)$ and $F(-1, 1, -4)$.

Now, from the geometry of centroid, we know that the centroid of ΔDEF is same as the centroid of ΔABC .

$$\therefore \text{Centroid of } \Delta ABC \equiv G\left(\frac{1+3-1}{3}, \frac{2+0+1}{3}, \frac{-3+1-4}{3}\right) \equiv G(1, 1, -2)$$

Matching Column Type Questions

Q50. Match each item given under the column C_1 to its correct answer given under column C_2 .

Column C_1		Column C_2	
(a)	In xy-plane	(i)	1st octant
(b)	Point (2, 3,4) lies in the	(ii)	yz-plane
(c)	Locus of the points having x coordinate 0 is	(iii)	z-coordinate is zero
(d)	A line is parallel to x-axis if and only	(iv)	z-axis
(e)	If $x = 0, y = 0$ taken together will represent the	(v)	plane parallel to xy-plane
(f)	$z = c$ represent the plane	(vi)	if all the points on the line have equal y and z-coordinates.
(g)	Planes $x = a, y = b$ represent the line	(vii)	from the point on the respective axis.
(h)	Coordinates of a point are the distances from the origin to the feet of perpendiculars	(viii)	parallel to z-axis
(i)	A ball is the solid region in the space	(ix)	disc
(j)	Region in the plane enclosed by a circle is known as a	(x)	sphere

Sol: (a) In xy-plane, z-coordinate is zero.

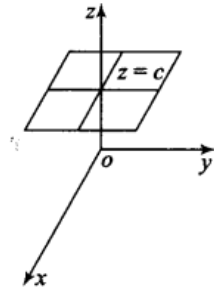
(b) The point (2, 3,4) lies in 1st octant.

(c) Locus of the points having x-coordinate zero is yz-plane.

(d) A line is parallel to x-axis if and only if all the points on the line have equal y and z-coordinates.

(e) $x = 0, y = 0$ represent z-axis

(f) $z = c$ represents the plane parallel to xy-plane.



(g) The plane $x = a$ is parallel to yz -plane.

Plane $y = b$ is parallel to xz -plane.

So, planes $x = a$ and $y = b$ is line of intersection of these planes.

Now, line of intersection of yz -plane and xz -plane is z -axis.

So, line of intersection of planes $x = a$ and $y = b$ is line parallel to z -axis.

(h) Coordinates of a point are the distances from the origin to the feet of perpendicular from the point on the respective axis.

(i) A ball is the solid region in the space enclosed by a sphere.

(j) The region in the plane enclosed by a circle is known as a disc.

Hence, the correct matches are:

(a) – (iii), (b) – (i), (c) – (ii), (d) – (vi), (e) – (iv),

(f) – (v), (g) – (viii), (h) – (vii), (i) – (x), (j) – (ix),